



Dr.SNS RAJALAKSHMI COLLEGE OF ARTS AND SCIENCE

(AUTONOMOUS)

COIMBATORE-2241049

**Accredited by NAAC(Cycle III) with “A+” Grade
Recognised by UGC, Approved by AICTE, New Delhi and
Affiliated to Bharathiar University, Coimbatore.**



DEPARTMENT OF COMPUTER SCIENCE

Computer System Architecture

I YEAR - I SEM

Unit II – Digital Logic Circuit



Boolean Laws



Commutative law

(i) $A.B=B.A$

(ii) $A+B=B+A$

Associative law

(i) $A.(B.C)=(A.B).C$

(ii) $A+(B+C)=(A+B)+C$

Distributive law

$$A.(B+C)=(A.B)+(A.C)$$

AND law

(i) $A.0=0$ (ii) $A.1=A$ (iii) $A.1=A$ (iii) $A.A' =0$

OR law

(i) $A+0=A$ (ii) $A+1=1$ (iii) $A.+A=A$ (iii) $A+A' =1$

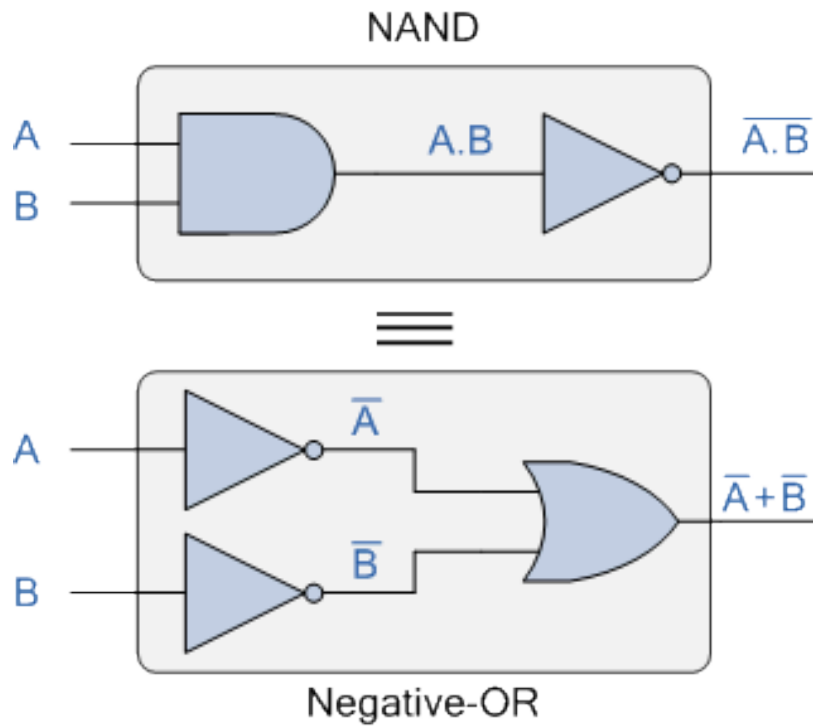
INVERSION law

$$\overline{\overline{A}} = A$$

DeMorgan's Law

(i) $\overline{A \cdot B} = \overline{A} + \overline{B}$

Logic Diagram



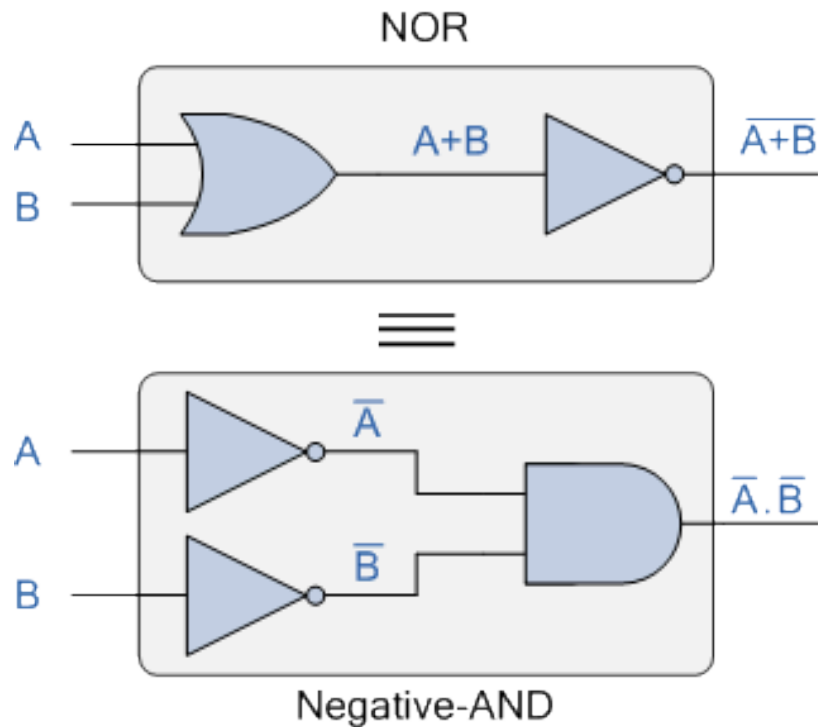
Truth Table

Inputs		Truth Table Outputs For Each Term					
B	A	$A \cdot B$	$\overline{A \cdot B}$	\overline{A}	\overline{B}	$\overline{A} + \overline{B}$	
0	0	0	1	1	1	1	
0	1	0	1	0	1	1	
1	0	0	1	1	0	1	
1	1	1	0	0	0	0	

DeMorgan's Law

$$(ii) \overline{A+B} = \overline{A} \cdot \overline{B}$$

Logic Diagram



Truth Table

Inputs		Truth Table Outputs For Each Term					
B	A	A+B	$\overline{A+B}$	\overline{A}	\overline{B}	$\overline{A} \cdot \overline{B}$	
0	0	0	1	1	1	1	
0	1	1	0	0	1	0	
1	0	1	0	1	0	0	
1	1	1	0	0	0	0	



Boolean Expression Simplification



1. Simplify: $C + BC$

<u>Expression</u>	<u>Rule(s) Used</u>
$C + BC$	Original Expression
$C + (B + C)$	DeMorgan's Law.
$(C + C) + B$	Commutative, Associative Laws.
$T + B$	Complement Law.
T	Identity Law.

2. Simplify: $AB(A + B)(B + B)$

<u>Expression</u>	<u>Rule(s) Used</u>
$AB(A + B)(B + B)$	Original Expression
$AB(A + B)$	Complement law, Identity law.
$(A + B)(A + B)$	DeMorgan's Law
$A + BB$	Distributive law.
A	Complement, Identity.



Boolean Expression Simplification



3. Simplify: $(A + C)(AD + AD) + AC + C$

Expression

$$(A + C)(AD + AD) + AC + C$$

$$(A + C)A(D + D) + AC + C$$

$$(A + C)A + AC + C$$

$$A((A + C) + C) + C$$

$$A(A + C) + C$$

$$AA + AC + C$$

$$A + (A + T)C$$

$$A + C$$

Rule(s) Used

Original Expression

Distributive.

Complement, Identity.

Commutative, Distributive.

Associative, Idempotent.

Distributive.

Idempotent, Identity, Distributive.

Identity, twice.



Thank You