



Dr.SNS RAJALAKSHMI COLLEGE OF ARTS AND SCIENCE

(AUTONOMOUS)

COIMBATORE-641049

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DEPARTMENT OF COMPUTER SCIENCE

Computer System Architecture

I YEAR - I SEM

UNIT 1 – Data Representation



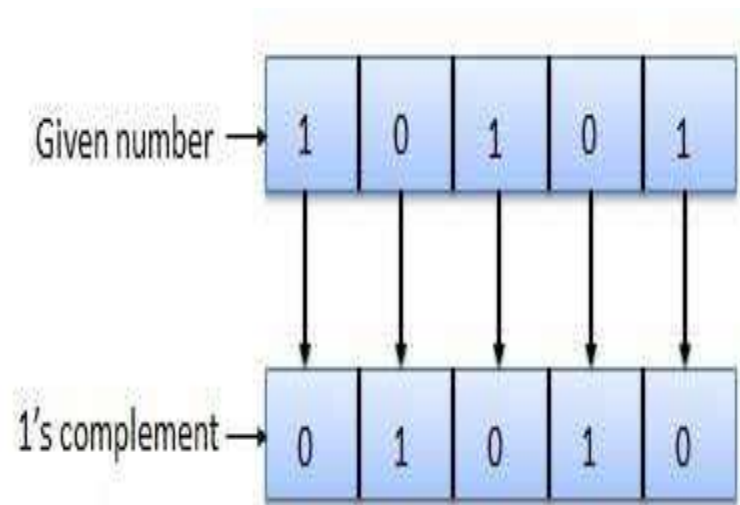
Complements

Complements are used in the digital computers in order to simplify the subtraction operation and for the logical manipulations.

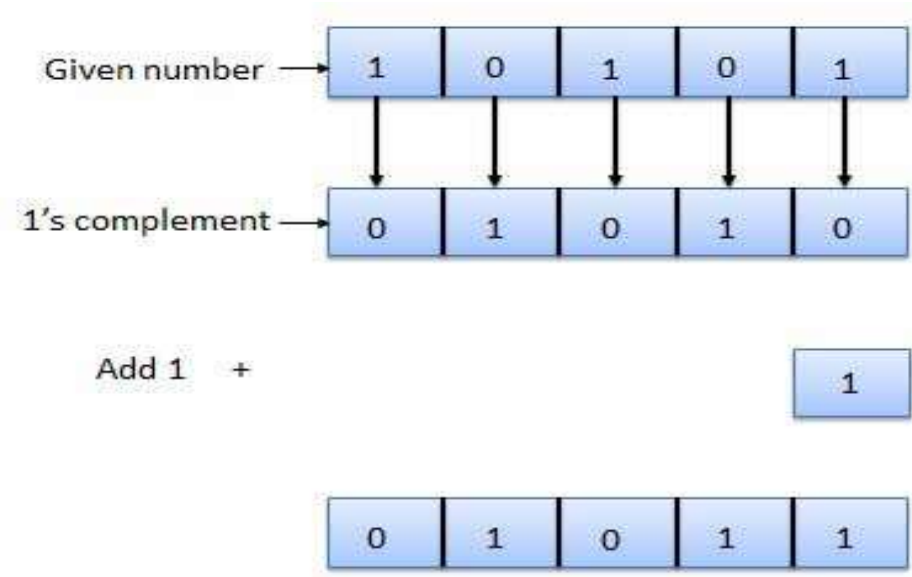
S.No.	Complement	Description
1	Radix Complement	The radix complement is referred to as the r 's complement
2	Diminished Radix Complement	The diminished radix complement is referred to as the $(r-1)$'s complement

Complements

1's complement



2's complement



Binary Addition

Example: $0011010 + 001100$
 (26) (12)

0011010 (26)
 0001100 (12)

 0100110 (38)

Case	A	+	B	Sum	Carry
1	0	+	0	0	0
2	0	+	1	1	0
3	1	+	0	1	0
4	1	+	1	0	1

Binary Subtraction

Case	A	-	B	Subtract	Borrow
1	0	-	0	0	0
2	1	-	0	1	0
3	1	-	1	0	0
4	0	-	1	0	1

Example: $0011010 - 001100$
 (26) (12)

11 Borrow

~~0011010~~ (26)

0001100 (12)

0001110 (14)

Binary Subtraction using 1's Complement

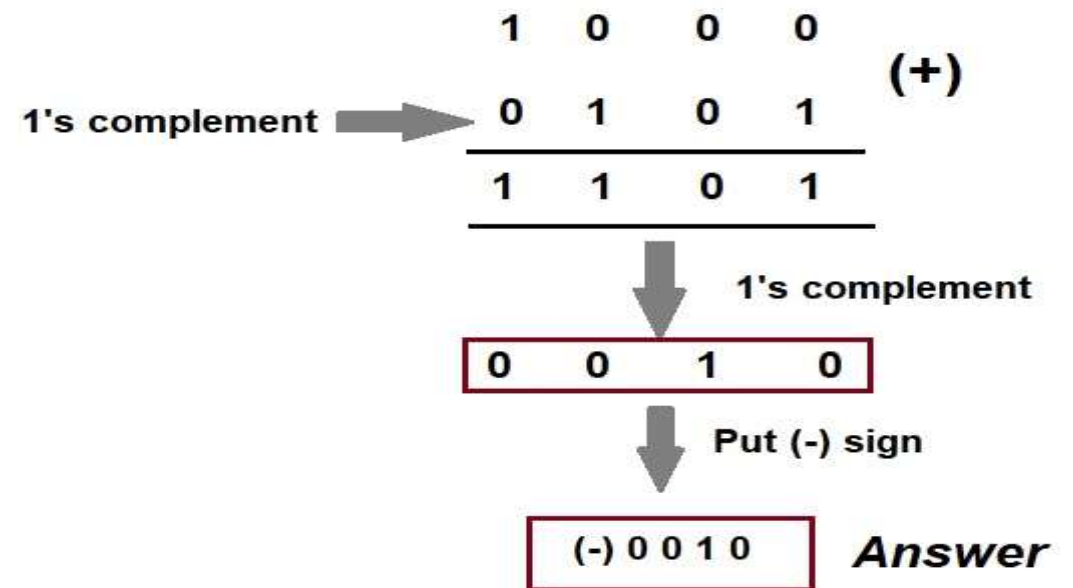
Step-1: Determine the 1's complement of the larger number.

Step-2: Add this to the smaller number.

Step-3: The answer is the 1's complement of the true result and opposite in sign. There is no carry.

Example: Subtract $(1010)_2$ from $(1000)_2$

$$\begin{array}{r}
 (10) \qquad \qquad \qquad (8) \\
 (1010)_2 - (1000)_2 = -0010_2 \\
 \qquad \qquad \qquad \qquad \qquad \qquad (-2)
 \end{array}$$



Binary Subtraction using 2's Complement

Step-1: Determine the 2's complement of the smaller number

Step-2: Add this to the larger number.

Step-3: Omit the carry. Note that, there is always a carry in this case.

Subtract $(1010)_2$ from $(1111)_2$
 (10) (15)

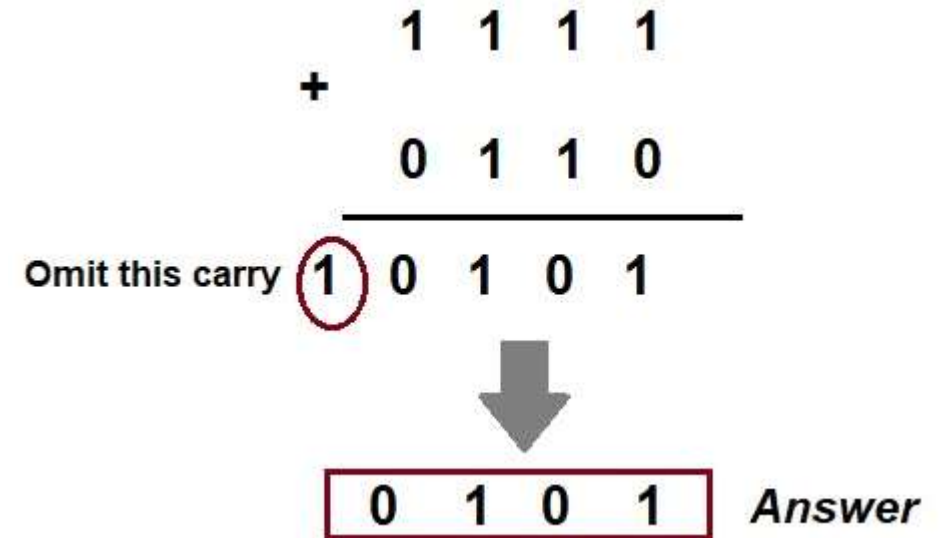
1's complement of 1010 = 0101

 Add 1 = 1

2's complement of 1010 = 0110

$(1111)_2 - (1010)_2 = 0101_2$

(5)



Binary Subtraction using 2's Complement

Step-1: Determine the 2's complement of the largest number

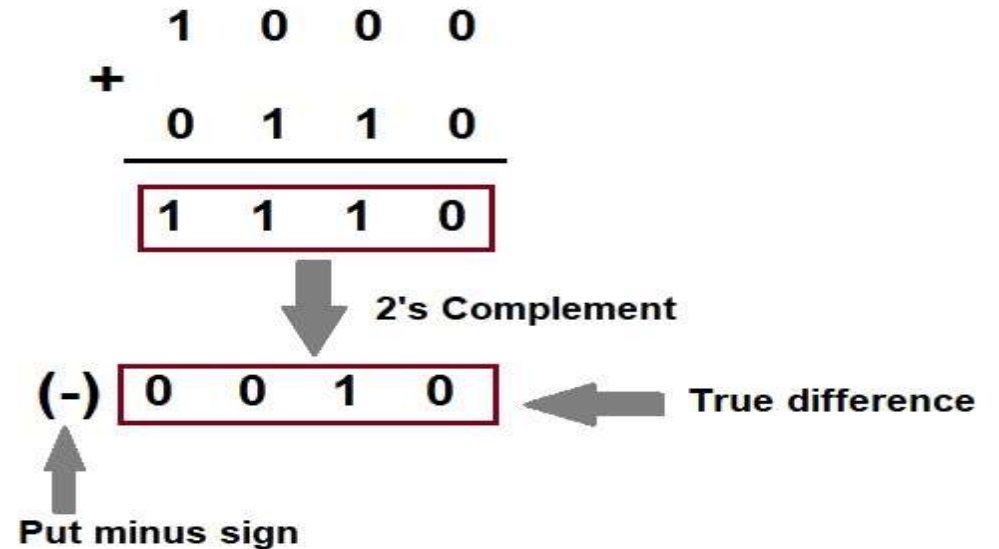
Step-2: Add this to the smaller number.

Step-3: There is no carry in this case. The result is in 2's complement form and is negative.

Step-4: To get answer in true form, take 2's complement and change its sign.

Example: Subtract $(1010)_2$ from $(1000)_2$

$$\begin{array}{r}
 (1010)_2 - (1000)_2 = -0010_2 \\
 \text{(6)} \qquad \qquad \text{(8)} \qquad \qquad \text{(-2)}
 \end{array}$$



9's and 10's Complement

Example 1: 1423

$$9999 - 1423 = 8576$$

9's Complement of 1423 is 8576

Add 1 in the Result $8576 + 1 = 8577$

10's Complement of 1423 is 8577

Example 2 : 456

9's

10's

999

543

(-) 456

(+) 1

543

544

Decimal digit	9's complement
0	9
1	8
2	7
3	6
4	5
5	4
6	3
7	2
8	1
9	0

Subtraction using 9's Complement

When subtrahend is smaller than the minuend

General Subtraction

$$\begin{array}{r} 841 \\ - 329 \\ \hline 512 \end{array}$$

Subtraction using 9's Complement

$$\begin{array}{r} 841 \\ + 670 \leftarrow (9's \text{ Complement of } 329) \\ \hline \textcircled{1}511 \\ + 1 \\ \hline 512 \end{array}$$

When subtrahend is greater than the minuend

General Subtraction

$$\begin{array}{r} 841 \\ - 983 \\ \hline -142 \end{array}$$

Subtraction using 9's Complement

$$\begin{array}{r} 841 \\ + 016 \leftarrow (9's \text{ Complement}) \\ \hline 857 \text{ (No carry indicates -ve value)} \\ \downarrow \\ -142 \text{ (9's Complement of result)} \end{array}$$

Subtraction using 10's Complement

When subtract end is smaller than the minuend

When subtract end is greater than the minuend

When subtrahend is smaller than the minuend

General Subtraction

$$\begin{array}{r} 821 \\ - 413 \\ \hline 408 \end{array}$$

Subtraction using 10's Complement

$$\begin{array}{r} 821 \\ + 587 \text{ (10's Complement of 413)} \\ \hline 1408 \text{ (ignore the carry)} \\ \downarrow \\ 408 \end{array}$$

General Subtraction

$$\begin{array}{r} 325 \\ - 641 \\ \hline -316 \end{array}$$

Subtraction using 10's Complement

$$\begin{array}{r} 325 \\ + 359 \text{ ← (10's Complement of 641)} \\ \hline 684 \text{ ← (No carry indicate negative -ve value)} \\ \downarrow \\ -316 \text{ ← (10's Complement of result)} \end{array}$$



Thank You