

SNS COLLEGE OF TECHNOLOGY (An Autonomous Institution)



Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Cauchy's Linear Differential Equation



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UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

(1)
$$\int \left[b^{12} - b^{1} + b^{1} + 4 \right] y = x Sin z$$

$$\left[b^{12} + 4 \right] y = x Sin x$$

$$AE \qquad n^{3} = -4 \qquad n = \pm 2i$$

$$CF = A \cos x^{3}x + B Sin x^{3}$$

$$FI = \frac{1}{b^{12} + 4} x Sin x$$

$$= x - \frac{1}{b^{12} + 4} Sin x - \frac{2b'}{(b^{1} + 4)^{2}} Sin x$$

$$= x - \frac{1}{(-1 + 4)} Sin x - \frac{x \cos x}{(-1 + 4)^{2}} \quad b^{12} - a^{2}$$

$$= \frac{x Gin x}{3} - \frac{x \cos x}{9}$$

$$The Solids is$$

$$y = cF + PF$$

$$y = A \cos x(\log x) + B Sin x - \frac{x (\log x)}{3} - \frac{x \cos x}{9}$$

$$= A \cos x(\log x) + B Sin x - \frac{x (\log x)}{3} - \frac{x \cos x}{9}$$

$$HJ. Solve (x^{2} B - xp + t) y = \log x$$

$$Solids (x^{2} B - xp + t) y = \log x$$

$$x = \log x$$

$$x = b g x$$

$$x = b f$$



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UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

(i)
$$\Rightarrow (p^{12} - p' - p' + i) \quad y = x$$

$$(p^{2} - 2p' + i) \quad y = x$$

AE

$$m^{3} - am + i = 0$$

$$(m + i) (m - i) = 0$$

$$m = 1, i$$

$$\therefore CF = (A + Bx) e^{x}$$

PI = $\frac{1}{p^{12} - 2p^{1} + 1} = [i + (p^{12} - 2p^{1})]^{-1} = x$

$$= [i - (p^{12} - 2p^{1}) + (p^{12} - 2p^{1})^{2} - \cdots] = x$$

$$= x - p^{13} = x + 2p^{1}(x)$$

PI = $x + 2$

$$\therefore Tbe Soln. \quad Sol. \quad y = cF + PT$$

$$y = (A + Bz)e^{z} + z + 2$$

$$y = (A + Blog = x) = x + log = x + 2$$

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