

SNS COLLEGE OF TECHNOLOGY

Coimbatore-21 An Autonomous Institution



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DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

19ECT212 – CONTROL SYSTEMS

II YEAR/ IV SEMESTER

UNIT III – FREQUENCY RESPONSE ANALYSIS

TOPIC 6,7- LEAD, LAG COMPENSATORS

19ECT212/Linear Control Systems/Unit 3/Dr.Swamynathan.S.M/ASP/ECE







•REVIEW ABOUT PREVIOUS CLASS

•INTRO-LEAD COMPENSATORS

•RULES TO DESIGN PHASE LEAD COMPENSATION

•LEAD COMPENSATORS-REALIZATION, FREQUENCY RESPONSE

•ACTIVITY

•INTRO-LAG COMPENSATORS

•LAG COMPENSATORS-REALIZATION, FREQUENCY RESPONSE

•DETERMINATION OF $\omega_{m} \, \varphi_{m}$ •SUMMARY



INTRO-LEAD & LAG COMPENSATORS



•The **lead compensator** is an electrical network which produces a sinusoidal output having phase **lead** when a sinusoidal input is applied. ... So, in order to produce the phase **lead** at the output of this **compensator**, the phase angle of the transfer function should be **positive**.

•The **Lag Compensator** is an electrical network which produces a sinusoidal output having the phase **lag** when a sinusoidal input is applied. ... So, in order to produce the phase **lag** at the output of this **compensator**, the phase angle of the transfer function should be **negative**



INTRO-LEAD COMPENSATORS



Three design rules for cascade compensator:

1. The system is stable with satisfactory steady-state error, but dynamic performance is not good enough.

Compensator is used to change medium and high frequency parts to change crossover frequency and phase margin.

2. The system is stable with satisfactory transient performance, but the steady-state error is large.

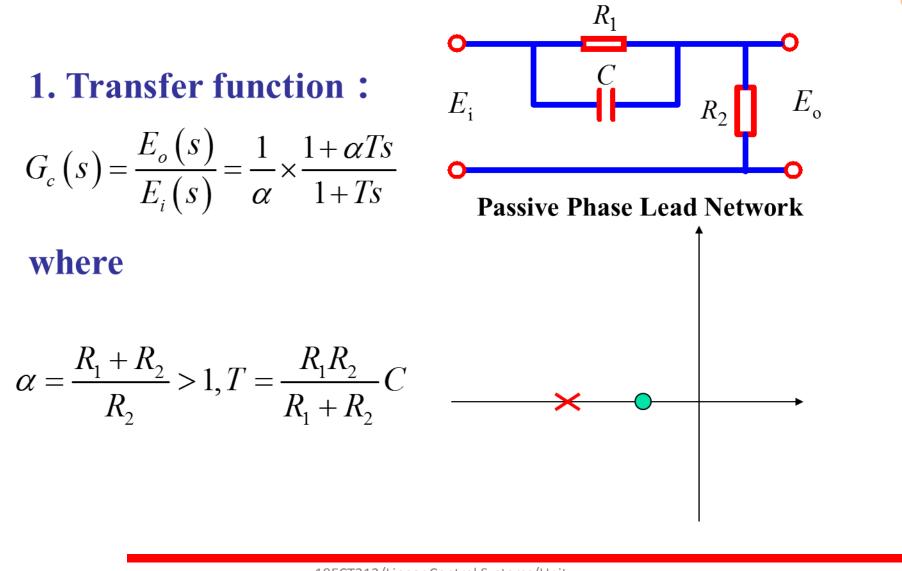
Compensator is used to increase gain and change lower frequency part, but keep medium and higher frequency parts unchanged.

3. If the steady-state and transient performance are either unsatisfactory, the compensator should be able to increase gain of the lower frequency part and change the medium and higher frequency parts.



INTRO-LEAD COMPENSATORS







RULES TO DESIGN PHASE LEAD COMPENSATION



(1) Determine K to satisfy steady-state error constraint

(2) Determine the uncompensated phase margin γ_0

(3) estimate the phase margin φ_m in order to satisfy the transient response performance constraint

(4) Determine α

(5) Calculate ω_m

(6) Determine *T*

(7) Confirmation



LEAD COMPENSATOR :



6

* A compensator having the characteristics of a lead new. * Lead compensation increases the bandwidth, which improves the speed of response. * It improves the transient response but small change is skady state acuracy. * Bosically a high poro filler. S-plane representation: nu Gec(s) = stac = (s+1/5) Stpc (St tr) The zero of comp, Zc = 115. The pole of comp. pc = bet. T= 1/2c + 1x = te

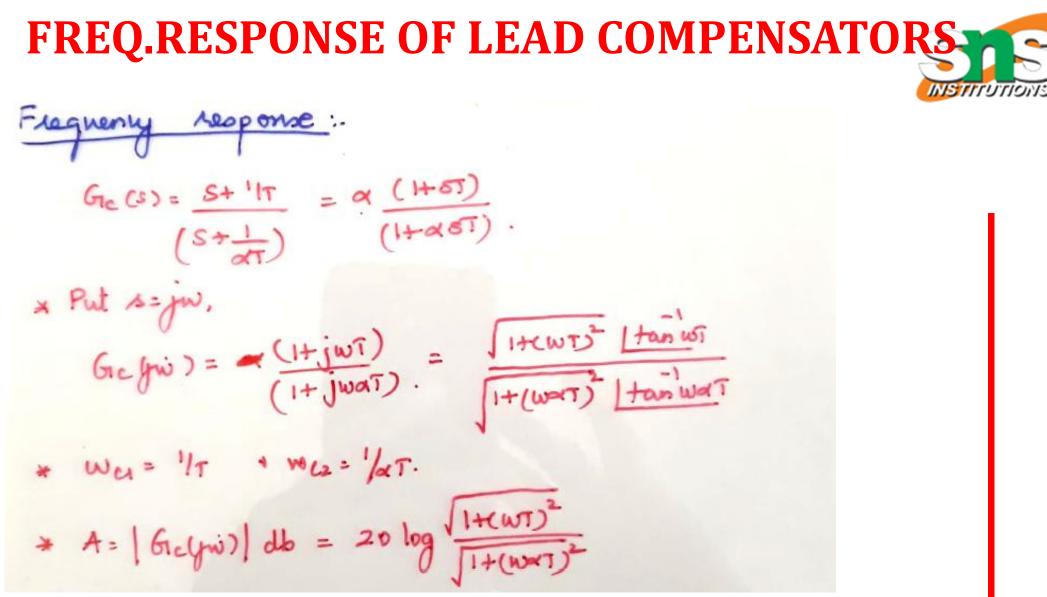


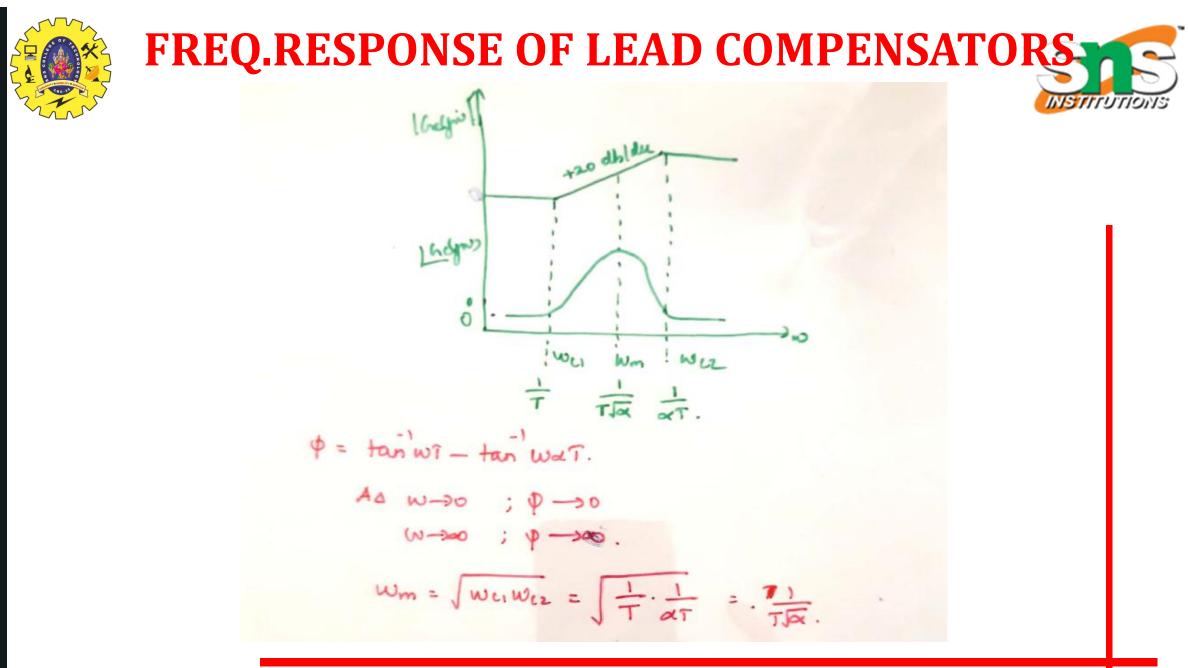
REALIZTION OF LEAD COMPENSATORS



| THE HOW OF FEAD COMPLENS |
|--|
| Realization of Lead Compensator: $F_{0}(s) = F_{0}(s) \frac{R_{2}}{R_{2}} + \frac{(R_{1} \times \frac{1}{S_{c}})}{(R_{1} + \frac{1}{S_{c}})} + \frac{(R_{1} \times \frac{1}{S_{c}})}{(R_{1} \times \frac{1}{S_{c}})} + \frac{(R_{1} \times \frac{1}{S_{c}}$ |
| $\frac{E_0(s)}{E_0(s)} = \frac{S^{**} R_2(R_1 C_s + 1)}{[R_1 R_2 C_s + R_2 + R_1]}$ |
| $\frac{\overline{E_0}(4)}{\overline{E_i}(4)} = \frac{S + \frac{1}{R_1C}}{\left[\frac{S + \left(\frac{1}{R_2}/(R_1 + R_2)\right) \cdot \frac{1}{R_1C}\right]}\right]}$ |
| where, T= Ric d x = R2 RitR2. |







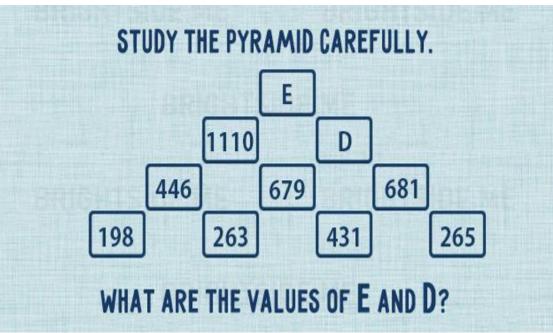


FREQ.RESPONSE OF LEAD COMPENSATORS

Determination of
$$um \neq pm$$
:
* $p = tain'wT - tain w w
* Diff p w.r.t. $w \Rightarrow equating dp = 0$.
 $wm = \frac{1}{T\sqrt{x}}$.
 $p_m = tain' \frac{1-\alpha}{2\sqrt{x}}$.$



Which way this bus is driving?





ACTIVITY-PUZZLES-ANSWERS



1. The bus is moving to the left because the door is on the other side.

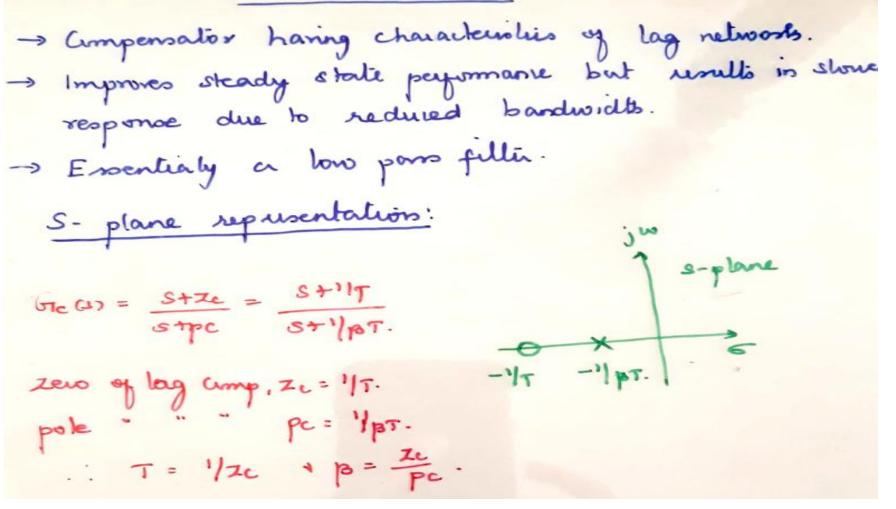
2.Answer: D = 1345; E = 2440.

The bottom numbers are connected to the upper level. First, add the numbers in the bottom line: 198 + 263 = 461.

Now you see that the number you got is greater than its neighbor above: 461 > 446. Subtract these numbers: 461 - 446 = 15.

If you check the rest of the pyramid, you'll get 15 in each case.











Realization of Lag compensator: RI Eo 4) = Ei 4) (R2 + 1/sc) m (Ri+R2+ /sc) Eou Eiu $\frac{E_0(s)}{E_1(t)} = \frac{CR_2\left(s + \frac{1}{CR_2}\right)}{C(R_1 + R_2)\left[s + \frac{1}{UR_1 + R_2}\right]}.$ T= R2C St - R2C E. (4) = $\beta = \frac{R_1 + R_2}{R_2}$ $\left(\frac{R_1 \# R_2}{R_2}\right) \begin{bmatrix} s \neq -1 \\ I(R_1 \# R_2) \end{bmatrix} \begin{bmatrix} s \neq -1 \\ I(R_1 \# R_2) \end{bmatrix} \begin{bmatrix} s \neq -1 \\ R_2 \end{bmatrix} \end{bmatrix} \begin{bmatrix} s \neq -1 \\ R_2 \end{bmatrix} \begin{bmatrix} s \neq -1 \\ R_2 \end{bmatrix} \end{bmatrix} \begin{bmatrix} s \neq -1 \\ R_2 \end{bmatrix} \begin{bmatrix} s \neq -1 \\ R_2 \end{bmatrix} \begin{bmatrix} s \neq -1 \\ R_2 \end{bmatrix} \end{bmatrix} \begin{bmatrix} s \neq -1 \\ R_2 \end{bmatrix} \begin{bmatrix} s \neq -1 \\ R_2 \end{bmatrix} \end{bmatrix}$





Frequency Response of Lag Compensation:

$$G_{c}(s) = \frac{(s+i)T}{(s+\frac{1}{pT})} = p \frac{(1+sT)}{(1+spT)}.$$
Put $s=jw$,

$$G_{c}(jw) = \frac{1}{p} \frac{(1+jwT)}{(1+jwpT)}.$$
+ le dc gave of compensation is not desirable, p can
be eliminated

$$G_{c}(jw) = \frac{1+(wT)^{2}}{(1+(wpT)^{2} + tan)^{2}wpT}.$$

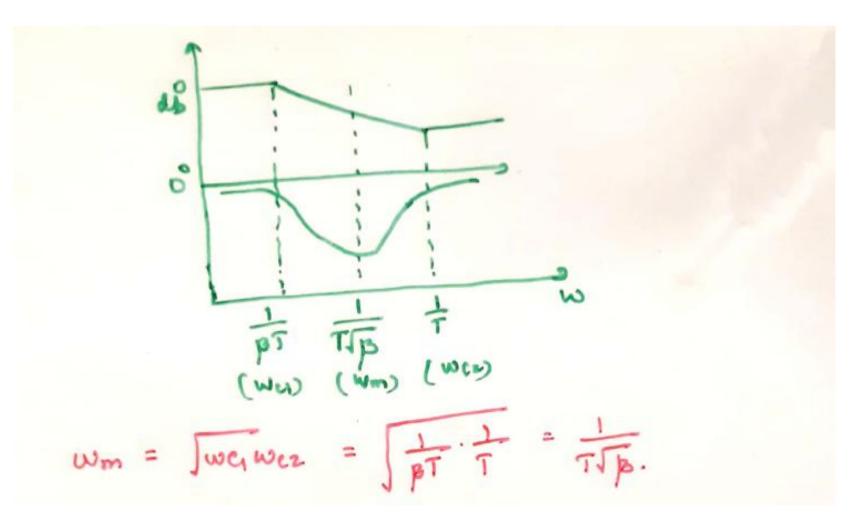


*
$$w_{c1} = \frac{1}{pT}$$
 * $w_{c2} = \frac{1}{2}T$.
* $A = |G_{c}(pw)\rangle = 20 \log \sqrt{\frac{14(wpT)^2}{14(wpT)^2}}$.
* At two fug. $wT < c_1 + wpT < c_1$.
: $A \approx 20 \log 1 = 0$.
* Frug. range from white were, $wT < c_1 + wpT > 0$.
: $A \approx 20 \log \frac{1}{\sqrt{(wpT)^2}} = 20 \log \frac{1}{\sqrt{0pT}}$.
: $A \approx 20 \log \frac{1}{\sqrt{(wpT)^2}} = 20 \log \frac{1}{\sqrt{0pT}}$.
* At high fug. $wT > 0$ + $wpT > 0$.
$P = \tan^2 wT - \tan^2 wpT$.
$P = \tan^2 wT - \tan^2 wpT$.











Determination of won 9 Pm. * The fug. wom can be detirmined by diff. I w.r.t. w a equating do I dw =0. [Gre (più) = q = tan wT-tan wpT. $\begin{bmatrix} d(tom e) = 1\\ de \end{bmatrix}$ $\frac{d\varphi}{dw} = \frac{1}{1+(wT)^2} T - \frac{1}{1+(wpT)^2} P^T.$ * when w > wm dp = 0. $\frac{T}{1+(wmT)^2} = \frac{BT}{1+(wmBT)^2}.$ $I+(wmpT)^2 = p[I+(wmT)^2].$ wm= 1 TJp



we know that, P= tan wi - tan war. tang = tan [tan'wi - tan' wp]. tan (A-B) = tan A-tan B It tan Atan B. $\frac{\tan \varphi}{1+\omega^2 \tau^2} = \frac{\omega \tau - \omega \beta \tau}{1+\beta(\omega \tau)^2}$ Ao w-swon to q-sqm. $\tan qm = \frac{WmT(1-p)}{1+p(WmT)^2}.$ $\Psi_m : tan \left(\frac{1-\beta}{2 \Gamma \beta} \right)$









