

SNS COLLEGE OF TECHNOLOGY



Coimbatore-21
An Autonomous Institution

Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A++' Grade Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

19ECT212 - CONTROL SYSTEMS

II YEAR/ IV SEMESTER

UNIT III – FREQUENCY RESPONSE ANALYSIS

TOPIC 6,7- LEAD, LAG COMPENSATORS



OUTLINE



- •REVIEW ABOUT PREVIOUS CLASS
- •INTRO-LEAD COMPENSATORS
- •RULES TO DESIGN PHASE LEAD COMPENSATION
- •LEAD COMPENSATORS-REALIZATION, FREQUENCY RESPONSE
- ACTIVITY
- •INTRO-LAG COMPENSATORS
- •LAG COMPENSATORS-REALIZATION, FREQUENCY RESPONSE
- •DETERMINATION OF $\omega_{m_{\iota}} arphi_{m}$
- •SUMMARY



INTRO-LEAD & LAG COMPENSATORS



•The **lead compensator** is an electrical network which produces a sinusoidal output having phase **lead** when a sinusoidal input is applied. ... So, in order to produce the phase **lead** at the output of this **compensator**, the phase angle of the transfer function should be **positive**.

•The **Lag Compensator** is an electrical network which produces a sinusoidal output having the phase **lag** when a sinusoidal input is applied. ... So, in order to produce the phase **lag** at the output of this **compensator**, the phase angle of the transfer function should be **negative**

INTRO-LEAD COMPENSATORS



Three design rules for cascade compensator:

1. The system is stable with satisfactory steady-state error, but dynamic performance is not good enough.

Compensator is used to change medium and high frequency parts to change crossover frequency and phase margin.

2. The system is stable with satisfactory transient performance, but the steady-state error is large.

Compensator is used to increase gain and change lower frequency part, but keep medium and higher frequency parts unchanged.

3. If the steady-state and transient performance are either unsatisfactory, the compensator should be able to increase gain of the lower frequency part and change the medium and higher frequency parts.

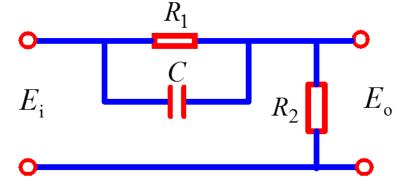


INTRO-LEAD COMPENSATORS



1. Transfer function:

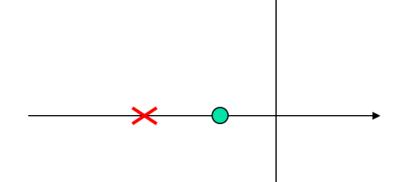
$$G_c(s) = \frac{E_o(s)}{E_i(s)} = \frac{1}{\alpha} \times \frac{1 + \alpha Ts}{1 + Ts}$$



Passive Phase Lead Network

where

$$\alpha = \frac{R_1 + R_2}{R_2} > 1, T = \frac{R_1 R_2}{R_1 + R_2} C$$





RULES TO DESIGN PHASE LEAD COMPENSATION



- (1) Determine K to satisfy steady-state error constraint
- (2) Determine the uncompensated phase margin γ_0
- (3) estimate the phase margin φ_m in order to satisfy the transient response performance constraint
- (4) Determine α
- (5) Calculate ω_m
- (6) Determine *T*
- (7) Confirmation





LEAD COMPENSATOR :

- * A compensator having the characteristics of a lead now.
- * Lead compensation increases the bandwidth, which improves the speed of response.
- * It improves the transient response but small change in skady state accuracy.
- * Bosically a high pass filler.

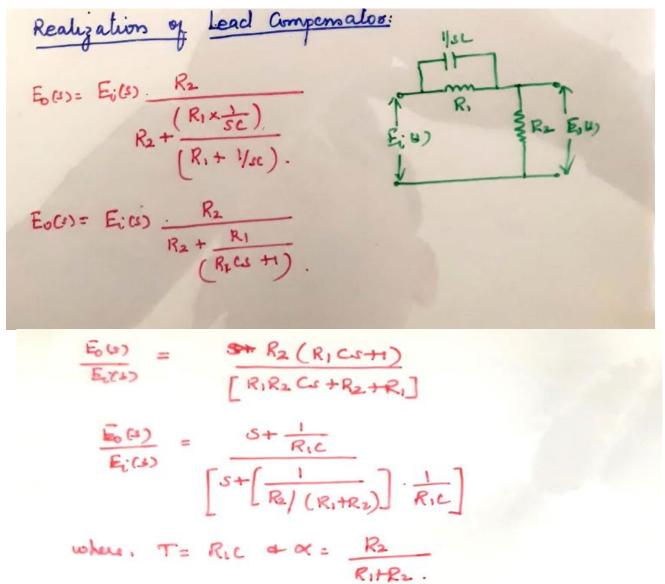
S-plane representation:

The zero of comp, Zc = "IT. - "/LT. -"IT



REALIZTION OF LEAD COMPENSATORS







FREQ.RESPONSE OF LEAD COMPENSATORS

Frequency Assponse:

$$G_{c}(s) = \frac{S + 1}{1} = \alpha \frac{(1 + \delta T)}{(1 + \alpha \delta T)}.$$

$$x \text{ Put } s = jw,$$

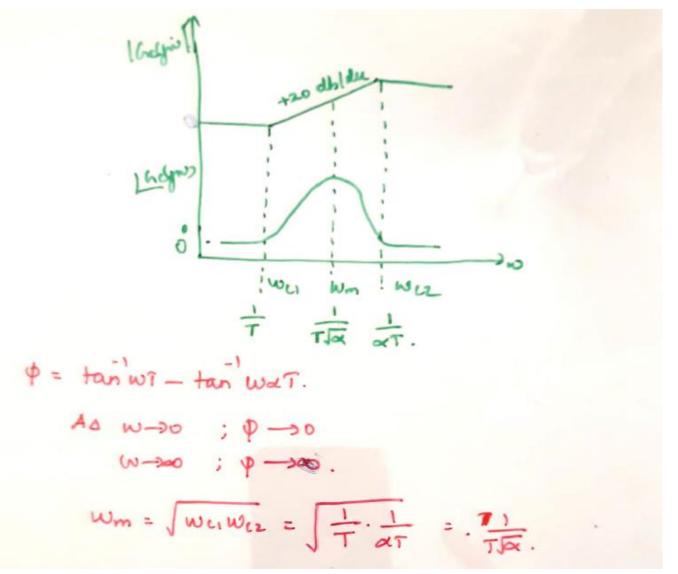
$$G_{c}(jw) = \alpha \frac{(1 + jwT)}{(1 + jwaT)} = \frac{1 + (wT)^{2} \left[+ \tan wT \right]}{1 + (waT)^{2} \left[+ \tan wT \right]}$$

$$wu = \frac{1}{1} + wu = \frac{1}{4}T.$$

$$x \text{ A} = \left[G_{c}(jw) \right] db = 20 \log \frac{1 + (wT)^{2}}{1 + (wT)^{2}}$$

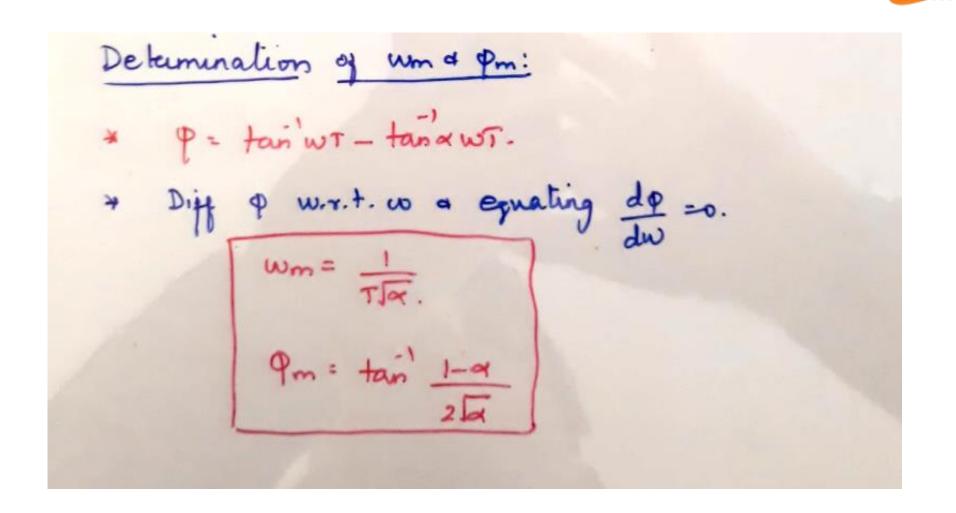


FREQ.RESPONSE OF LEAD COMPENSATORS





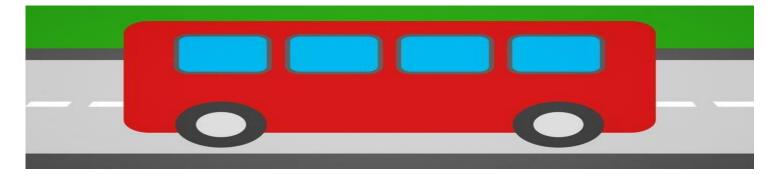
FREQ.RESPONSE OF LEAD COMPENSATORS



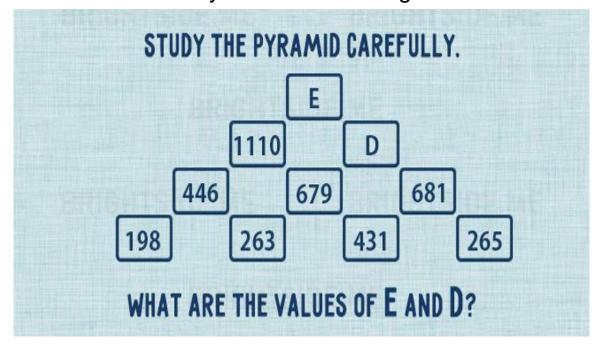


ACTIVITY-PUZZLES





Which way this bus is driving?





ACTIVITY-PUZZLES-ANSWERS



1. The bus is moving to the left because the door is on the other side.

2.Answer: D = 1345; E = 2440.

The bottom numbers are connected to the upper level. First, add the numbers in the bottom line: 198 + 263 = 461.

Now you see that the number you got is greater than its neighbor above: 461 > 446. Subtract these numbers: 461 - 446 = 15.

If you check the rest of the pyramid, you'll get 15 in each case.





LAG COMPENSATOR

- -> Compensator having characteristics of lag networks.
- -> Improves steady state performance but usults in shower response due to reduced bandwidts.
- -> Essentialy a low pors fillin.

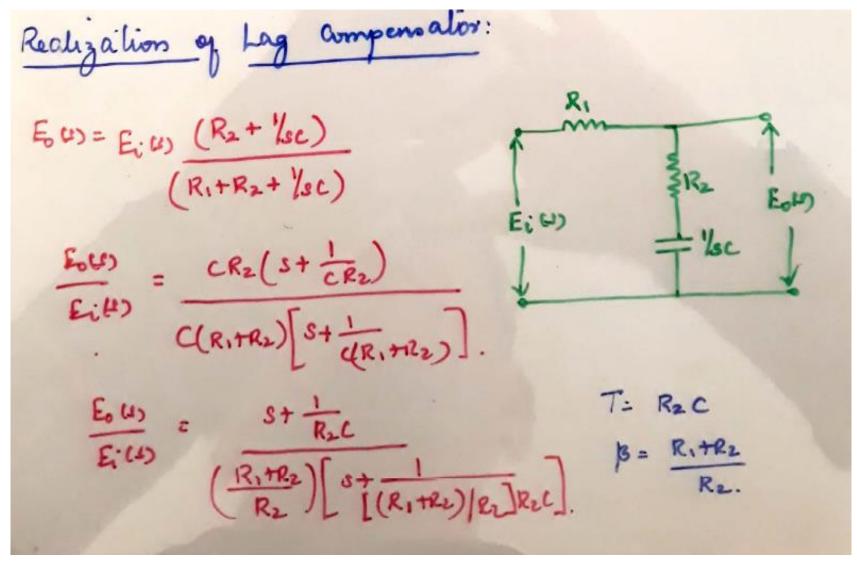
S- plane representation:

zero of lag comp, Zc = 1/T.

-1/T -1/pT.











Frequency Response of Lag Compensator:

$$G_{c(s)} = \frac{(s+it)}{(s+\frac{1}{pT})} = p \frac{(1+sT)}{(1+spT)}.$$

Put s=pw,

$$G_{c(pw)} = \frac{p (1+jwT)}{(1+jwpT)}.$$

* If clc gain of compensator is not desirable, p can be eliminated

$$G_{c(pw)} = \frac{1+(wT)^{2}}{1+(wpT)^{2}} \frac{1}{tan^{2}} wpT.$$





*
$$W_{C2} = \frac{1}{7}$$

* $A = |G_{C}(pi)| = 20 \log \frac{\sqrt{1+(wp)^2}}{\sqrt{1+(wp)^2}}$

* At low fug. $wT \ge 1$ + $wpT \ge 1$.

.: $A \approx 20 \log 1 = 0$.

* Fug. range from wer to wc_2 , $wT \ge 1$.

.: $A \approx 20 \log \frac{1}{\sqrt{(wp)^2}} = 20 \log \frac{1}{\sqrt{wp}}$.

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At high fug. $wT > 1$ + $wpT > 1$.

A $\approx 20 \log \frac{\sqrt{(wp)^2}}{\sqrt{(wp)^2}} = 20 \log \frac{1}{\sqrt{p}}$.

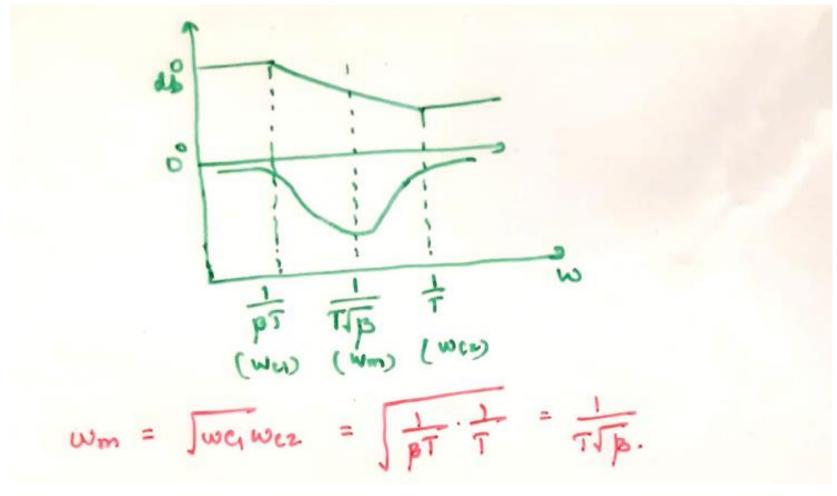
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We know that,

$$\varphi = \tan^2 w I - \tan^2 w g I.$$

$$\tan \varphi = \tan \left[\tan^2 w I - \tan^2 w g I \right].$$

$$\tan (A-13) = \frac{\tan A - \tan B}{1 + \tan A + \tan B}.$$

$$\tan \varphi = \frac{w I - w g I}{1 + w^2 I^2} = \frac{w I (1-\beta)}{1 + p(w I)^2}.$$

$$\Delta_0 w \rightarrow w m \Rightarrow \varphi \rightarrow \varphi m.$$

$$\tan \varphi m = \frac{w m I (1-\beta)}{1 + p(w m I)^2}.$$

$$\varphi m : \tan^2 \left(\frac{1-\beta}{2 \cdot \beta} \right)$$





SUMMARY

