

$$= I l B_2 a_y$$

Two current flow in same direction  
 → attractive force

$$\therefore F_1 = L I_1 \frac{\mu I_2}{2\pi D} a_y$$

Opposite direction  
 → repulsive force

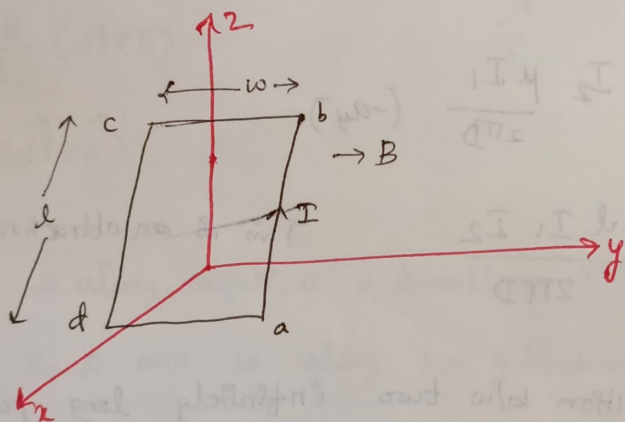
$$|F_1| = \frac{\mu I_1 I_2 l}{2\pi D}$$

$F$  is along +ve  $y$  direction. This is also an attractive force

$$|F_1| = |F_2|$$

Torque on a loop carrying current  $I$

force that tends to  
 cause rotation  
 (rotation force) / twisting force



Force =  $B I l$  (on the sides  $ab$  &  $cd$ )

Force = 0 (on the sides  $da$  &  $bc$ ) since  $I$  &  $B$  are parallel to each other.

Torque is the tangential force multiplied by the radial distance at which the force acts.

Total torque on the loop  $abcd$

$$= 2 \times \text{Torque on each side}$$

$$= 2 \times \text{Force} \times \text{Distance from axis of rotation}$$

$$= 2 \times B I l \times w/2$$

$$\tau = B I l \omega$$

vector form :-  

$$\vec{\tau} = \vec{m} \times \vec{B} \quad (\text{N/m})$$

$$\tau = B I A$$

If there are  $N$  turns then torque

$$\tau = N B I A$$

Note:

1) If  $B$  is at an angle of  $\theta$  with the axis of rotation then the tangential component of force is given by

$$F_t = F \cos \theta$$

$$\therefore \tau = B I A \cos \theta$$

2) If  $B$  is perpendicular to plane of the loop then  $\theta = 90^\circ$

$$\tau = 0$$

Torque is a function of position of coil.

$$\tau = B M \cos \theta$$

where  $M = I A \rightarrow$  magnetic dipole moment.

3) If  $\theta = 0$

$$\text{then } \tau = B M$$

$$M = \frac{I A}{B}$$

Thus magnetic moment is defined as maximum torque on the loop per unit magnetic induction.

$$\cos \theta = \frac{F_t}{F}$$

