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DEPARTMENT OF MATHEMATICS UNIT – IV INTERPOLATION, NUMERICAL DIFFERENTLATION AND NUMERICAL INTEGRATION

LAGRANGIAN INTERPOLATION

Let y = f(x) be a function which takes the values $y_0, y_1, y_2, \dots, y_n$ corresponding Then Lagrangian interpolation form is to x0, x1, 24, 20 y = f(x)Mutcher Fren gars & Annet = (x-x1)(x-x2)....(x-xn) yo + (x0-x1)(x0-x2)...(x1-xn) $(\chi - \chi_0) (\chi - \chi_2) \dots (\chi - \chi_n)$ $(\chi_1 - \chi_0)(\chi_1 - \chi_2) - \cdots - (\chi_1 - \chi_n)$ Real superior Concoled in and a month of mark an $\frac{(\chi - \chi_{0})(\chi - \chi_{1})\cdots(\chi - \chi_{n-1})}{(\chi_{n} - \chi_{0})(\chi_{n} - \chi_{1})\cdots(\chi_{n-1}\chi_{n-1})} y_{n}$



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Find the polynomial f(x) by using Lagrange's
Jornula and thence find f(3) for

$$\chi: 0 = 1 = 2, 3, 5$$

 $\chi(x): 2, 3 = 12, 147$
Soln: $\chi_0 = 0; y_0 = 2$
 $\chi_1 = 1: y_1 = 3$
 $\chi_2 = 2; y_2 = 12$
 $\chi_3 = 5; y_3 = 147$
By Lagrange's Priteipolation Jornula, we have

$$\begin{aligned} y &= -\frac{1}{2}(n) = \frac{(n-n_1)(n-n_2)(n-n_3)}{(n_0-n_1)(n_0-n_2)(n_0-n_3)} y_0 + \\ \frac{(n-n_0)(n-n_2)(n_0-n_3)}{(n_1-n_0)(n_1-n_2)(n_1-n_3)} y_1 + \\ \frac{(n-n_0)(n-n_1)(n-n_3)}{(n_2-n_1)(n_2-n_3)} y_2 + \\ \frac{(n-n_0)(n-n_1)(n-n_2)}{(n_2-n_1)(n_2-n_3)} y_2 + \\ \end{aligned}$$

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$$= \frac{(n-1)(n-2)(n-5)}{(n-1)(n-2)(n-5)}(2) + \frac{(n-0)(n-2)(n-5)}{(1-0)(1-2)(1-5)}(3)$$

$$+ \frac{(n-0)(n-1)(n-5)}{(2-0)(2-1)(2-5)}(12) + \frac{(n-0)(n-1)(n-2)}{(5-0)(5-1)(5-2)}(147)$$

$$= \frac{(n-1)(n-2)(n-5)}{-10}(2) + \frac{n(n-2)(n-5)}{4}(3)$$

$$+ \frac{n(n-1)(n-5)}{-10}(12) + \frac{n(n-1)(n-2)}{60}(147)$$

$$= \frac{n^{2}+n^{2}-6}{-6}(2) + \frac{3(3-2)(3-5)}{4}(3) + \frac{3(3-2)(3-5)}{4}(3) + \frac{3(3-1)(3-2)}{4}(147)$$

$$= \frac{8}{10} - \frac{18}{4} + \frac{24}{4} + \frac{147}{60} - 35$$



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The process of finding a value of x for
the conserponding value of y is called inverse
Interpolation
2nverse interpolation Jaimula is

$$x = (y-y_1)(y-y_2) - (y-y_n)$$
 $x_0 + (y_0-y_1)(y_0-y_2) - (y_0-y_n)$
 $((y-y_0)(y-y_2) - (y_0-y_n)) = ((y-y_n))$
 $((y-y_0)(y-y_2) - (y_0-y_n)) = ((y-y_n))$
 $((y-y_0)(y-y_2) - (y_0-y_n)) = ((y-y_0))$



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) Find the age corresponding to the annihity value 13.6
cylinen the table
Age (x): 30 35 40 45 50
Annihity value(y): 15.9 14.9 14.1 13.3 12.5
30/1:
$$\chi = (Y - Y_1) + (Y - Y_2)(Y - Y_3)(Y - Y_4)$$

 $(Y_0 - Y_1)(Y_0 - Y_2)(Y_0 - Y_3)(Y - Y_4)$
 $(Y - Y_0)(Y - Y_2)(Y_1 - Y_3)(Y - Y_4)$
 $(Y - Y_0)(Y - Y_1)(Y - Y_2)(Y - Y_4)$
 $(Y - Y_0)(Y - Y_1)(Y - Y_2)(Y - Y_4)$
 $(Y - Y_0)(Y - Y_1)(Y - Y_2)(Y - Y_4)$
 $(Y - Y_0)(Y - Y_1)(Y - Y_2)(Y - Y_4)$
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 $(Y - Y_0)(Y - Y_1)(Y - Y_2)(Y - Y_3)$
 $(Y - Y_0)(Y - Y_1)(Y - Y_2)(Y - Y_3)$
 $(Y - Y_0)(Y - Y_1)(Y - Y_2)(Y - Y_3)$



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$$= \frac{(13.6 - 14.9)(13.6 - 14.1)(13.6 - 13.3)(13.6 - 12.5)}{(15.9 - 14.9)(15.9 - 14.1)(15.9 - 14.1)(15.9 - 12.5)} \times 30 + \frac{(15.9 - 14.9)(15.9 - 14.1)(15.9 - 12.5)}{(14.9 - 15.9)(14.9 - 14.1)(13.6 - 13.3)(13.6 - 12.5)} \times 35 + \frac{(13.6 - 15.9)(14.9 - 14.9)(13.6 - 13.3)(13.6 - 12.5)}{(14.1 - 15.9)(14.1 - 14.9)(14.9 - 13.3)(14.1 - 12.5)} \times 40 + \frac{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.6 - 12.5)}{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.8 - 12.5)} \times 45 + \frac{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.8 - 12.5)}{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.8 - 12.5)} \times 45 + \frac{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.8 - 12.5)}{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.8 - 12.5)} \times 45 + \frac{(13.6 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.6 - 13.3)}{(12.5 - 15.9)(13.6 - 14.9)(13.6 - 14.1)(13.6 - 13.3)} \times 50 = 43$$