

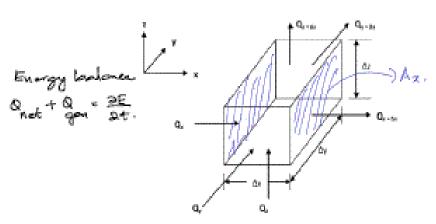


DEPARTMENT OF MECHANICAL ENGINEERING

16ME306/ Heat and Mass Transfer – UNIT I - CONDUCTION

Topic - General Differential equation of Heat Conduction -Cartesian Coordinates

General 3D-Conduction equation in contesion. condition



X-direction:

Heat entang the element = Qx ->0

Heat exiting the element = Q2+Ax) -> @

From the taylor) series;
$$Q_{x+ax} = Q_x + \frac{\partial Q_x}{\partial x} \Delta x + \frac{\partial^2 Q_x}{\partial x^2} \frac{\Delta x^2}{2!} + \frac{\partial^2 Q_x}{\partial x^2} \frac{\Delta x^2}{2!} \dots]$$

Neglecting higher order tome

Not heat flow is given by: Qz-Qx+4x = Qx-Qx+2Qx Ax).

From fourier las Qz = - Kz Az 2T





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Similar expressions can be obtained from yez

Qz-Qz+Az=Kz. 327. Da. Dy. Az -> 6

Net heat flow in all three directions [44,2].

Heat generated from the volume.

From the first law of thermodynamics;

Quet + Quen = Rate of change of energy transfer.





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Care-1: Instropic material
$$k = k_z = k_y = k_z$$
.

$$K \left[\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right] + Q^{N} = JQ \cdot \frac{\Delta T}{\partial t}.$$

$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} + \frac{\partial^2 T}{\partial z^$$

3T + 3T + 2T + 2T - 2 - 1 AT - 0

[Fourier-Rist equation]

Care-2: 9"=0 [No heat generation and instropic].

\[
\frac{3T}{2x^2} + \frac{3T}{2y^3} + \frac{3T}{2z^2} = \frac{1CF}{K} \frac{AT}{2T}
\]

$$\frac{3^2T}{3x^2} + \frac{3^2T}{3y^2} + \frac{3^2T}{3z^2} = \frac{1}{2} \cdot \frac{\Delta T}{3t} \longrightarrow 12$$

[Diffuron equation].

Care-z: AT =0 [Steady state and isotropic]

Care-4: 9"=0 & AT =0 [Steady state, no heat
generation and isotropic]

[Laplace equation].





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