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Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Solve
$$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + 4y = \log x$$
 Sin($\log x$)

Soln.

Given $\left[x^2 D^2 + x D + 4\right] y = \log x$ Sin($\log x$)

Take $x = e^x$

$$\log x = x$$

$$xD = D \quad ; \quad x^2 D^2 = D \cdot (D - 1)$$

$$= D \cdot \int_{-\infty}^{\infty} x^2 D^2 = D \cdot (D - 1)$$



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(1)
$$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{x} + D^{x} + D^{x} + A \int_{-\infty}^{\infty} y = x \operatorname{Sin} x$$

$$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{x} + A \int_{-\infty}^{\infty} y = x \operatorname{Sin} x$$

$$\int_{-\infty}^{\infty} e^{x} + A = 0$$

$$\int_{-\infty}^{\infty} e^{$$





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(1)
$$\Rightarrow$$
 ($D^{12} - D^{1} - D^{1} + 1$) $y = x$
($D^{2} - 2D^{1} + 1$) $y = x$
AE $m^{3} - am + 1 = 0$
($m + 1$) ($m - 1$) $= 0$
 $m = 1$, 1
 \therefore $CF = (A + Bx) e^{x}$
PI = $\frac{1}{D^{12} - 2D^{1} + 1} = \frac{1}{D^{12} - 2D^{1}$



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