

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)
Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

CamScanner

Cauchy's Linear Differential Equation

J. Solve
$$x^{2}y'' + pxy' = 0$$

Solp

(Aven $(x^{2}p^{2} + pxy)y = 0 \rightarrow 7(1)$)

Take $x = e^{x}$
 $x = log x$
 $x = D = D'$
 $x^{2}D^{2} = D'(D'-1) = D^{1/2} - D'$

Subs. the above $90(1)$,

 $[D^{1/2} + D]y = 0$
 $[D^{1/2} + D^{1/2} + D^{1/2}$



SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)
Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Cauchy's Linear Differential Equation

$$CF = (A+Bx)e^{2x}$$

$$CF = [A+B\log x]x^{2}$$

$$PI = \frac{1}{b^{2}-AD'+4} e^{x} S^{2}n x$$

$$= e^{x} \frac{1}{(D'+1)^{2}-A(D'+1)+A} S^{2}n x$$

$$= e^{x} \frac{1}{D^{2}+1+2D'-AD-A+A} S^{2}n x$$

$$= e^{x} \frac{1}{D'^{2}-2D'+1} S^{2}n x$$

$$= e^{x} \frac{1}{-1-2D'+1} S^{2}n x$$

$$= e^{x} \frac{1}{-2D'} S^{2}n x$$

$$= \frac{e^{x}}{-2} [-\cos x]$$

$$PI = \frac{e^{x}}{2} (\cos x) \Rightarrow PI = \frac{x \log(\log x)}{2}$$

$$x^{2} = cF + PI$$

$$S Canned V = [A+B\log x]x^{2} + x \frac{\cos(\log x)}{2}$$

$$CamScanner$$