



(An Autonomous Institution) Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Method of variation of parameters

2]. Solve
$$\frac{d^2y}{dx^2} + y = esc x$$
 using method of variation of parameters.

General (D+1)
$$y = CSC \times .$$

AE

 $M^2 + 1 = 0$
 $M^2 = -1$
 $M =$

 $= \int \cos x \, x \, \frac{1}{\text{Sqn } x} \, dx = \int \cot x \, dx$





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$$= \int \frac{\cos^{9}x}{8\pi n x} dx$$

$$= \int \frac{1 - 89n^{2}x}{89n x} dx$$

$$= \int [cscx - 89nx] dx$$

$$= \int cscx dx - \int 89nx dx$$

$$= \int cscx dx - \int 89nx dx$$

$$= -\log [cscx + \cos x] + \cos x$$

$$\therefore PI = -89nx \cos x + \log (cscx + \cot x) + \cos x$$
The general sdn. 9s,
$$y = cf + PI$$

$$= c_{1}\cos x + c_{2}\sin x - 89nx \cos x + \log (cscx + \cot x)$$

$$+ 69nx \cos x$$

$$= c_{1}\cos x + c_{2}\sin x + \log (cscx + \cot x)$$

4]. Solve (p3+a3) y = Sec ax using method of variation of Parameters. Soln.

Gren
$$(D^3 + a^3)y = Sec qx$$

$$m^3 + a^3 = 0$$

$$m^3 = -a^3$$

$$m = \pm a i$$

$$Cf = C_1 \cos qx + C_2 \sin qx$$

$$Here f_1 = \cos qx \qquad | f_2 = \sin qx$$

$$f_1 = -a \sin qx \qquad | f_3 = a \cos qx$$

$$\omega = f_1 f_2 - f_1 f_3$$

$$= \cos qx (a \cos qx) + a \sin qx \sin qx$$

$$= a \cos^2 qx + a \sin^2 qx$$

$$= a [\cos^2 qx + \sin^2 qx] = a(i) = a$$
Scanned with CamScanner $\Rightarrow \omega = a$





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PI = Pf₁ + 8f₂

$$P = -\int \frac{f_2 \times d_M}{\omega} d_M$$

$$= -\int \frac{Sf_0 \times Sec \times d_M}{a} d_M$$

$$= -\frac{1}{a} \int \frac{Sf_0 \times d_M}{a} d_M = -\frac{1}{a} \int \frac{f_0 \times f_0}{a} d_M$$

$$= +\frac{1}{a} \int \frac{f_0 \times f_0}{a} d_M d_M$$

$$= \int \frac{f_1 \times f_0}{\omega} d_M d_M$$

$$= \int \frac{\cos a \times Sec \times f_0}{a} d_M$$

$$= \frac{1}{a} \int \frac{f_0 \times f_0}{a} d_M$$

$$= \frac{f_0 \times f_0}{a} d_M$$

$$= \frac{1}{a} \int \frac{f_0 \times f_0}{a} d_M$$

$$= \frac{f_0 \times f_0}{a}$$