

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution) Coimbatore-641035.

UNIT-I VECTOR CALCULUS

DIVERGENCE AND CURL OF A VECTOR FIELD

Peoblems:

Caren
$$\vec{F} = x^2 + y^2 + z^2 + \vec{x}$$

$$\nabla \cdot \vec{F} = \frac{\partial}{\partial x} (x^2) + \frac{\partial}{\partial y} (y^2) + \frac{\partial}{\partial z} (z^2)$$

$$= 2x + 2y + 2z$$

$$\nabla \cdot \vec{F} = 2(x + y + z)$$

and
$$\nabla x \vec{r} = \begin{vmatrix} \vec{r} & \vec{r} & \vec{r} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \end{vmatrix}$$

$$= \overrightarrow{r} \left[\frac{\partial}{\partial y} (x^{2}) - \frac{\partial}{\partial z} (y^{2}) \right] - \overrightarrow{J} \left[\frac{\partial}{\partial z} (x^{2}) - \frac{\partial}{\partial z} (x^{2}) \right] \\ + \overrightarrow{R} \left[\frac{\partial}{\partial y} (y^{2}) - \frac{\partial}{\partial y} (x^{2}) \right]$$

$$= 07^{\circ} + 07^{\circ} + 08^{\circ}$$

$$\nabla \times F = 0^{\circ}$$

I petermane the constant 'a' so that the F= (x+z)+ (3x+ay)]+ (x-57) F & Such that "its devergence is zero. 80/n.

Now
$$\frac{\partial}{\partial x}(x+x) + \frac{\partial}{\partial y}(3x + \alpha y) + \frac{\partial}{\partial x}(x-5x) = 0$$

$$+a-5=0$$

$$\sqrt{a=4}$$





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Solve
$$\nabla \cdot \left(\frac{1}{\gamma} \overrightarrow{\gamma}\right)$$

Solve $\overrightarrow{r} = x\overrightarrow{r} + y\overrightarrow{j} + x\overrightarrow{k}$
 $\frac{1}{\delta} \overrightarrow{r} = \frac{x}{\delta} \overrightarrow{r} + \frac{y}{3} \overrightarrow{j} + \frac{x}{\delta} \overrightarrow{k}$
 $\frac{1}{\delta} \overrightarrow{r} = \frac{x}{\delta} \overrightarrow{r} + \frac{y}{3} \overrightarrow{j} + \frac{x}{\delta} \overrightarrow{k}$
Noco, $\nabla \cdot \left(\frac{1}{\gamma}\overrightarrow{r}\right) = \left(\overrightarrow{r} \frac{\partial}{\partial x} + \overrightarrow{j} \frac{\partial}{\partial y} + \overrightarrow{k} \frac{\partial}{\partial x}\right) \cdot \left(\frac{x}{\delta} \overrightarrow{r} + \frac{y}{3} \overrightarrow{j} + \frac{x}{\gamma} \overrightarrow{k}\right)$
 $= \frac{\partial}{\partial x} \left(\frac{x}{\delta}\right) + \frac{\partial}{\partial y} \left(\frac{y}{\delta}\right) + \frac{\partial}{\partial x} \left(\frac{x}{\delta}\right)$
 $= \frac{1}{\gamma \partial} \left[x - x(\frac{x}{\gamma}) + x - y(\frac{y}{\gamma}) + x - x(\frac{x}{\gamma})\right]$
 $= \frac{1}{\gamma \partial} \left[3x - \frac{x}{\delta} - \frac{y^2}{\delta} - \frac{x^2}{\delta}\right]$
 $= \frac{1}{\gamma \partial} \left[3x - \frac{1}{\gamma} x^2 + y^2 + x^2\right]$
 $= \frac{1}{\gamma \partial} \left[3x - \frac{1}{\gamma} x^2 + \frac{x^2}{\delta}\right]$
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