

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)
Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Cauchy's Linear Differential Equation

Solve
$$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + 4y = \log x$$
 Sin($\log x$)

Soln.

Given $\left[x^2 D^2 + x D + 4\right] y = \log x$ Sin($\log x$)

Take $x = e^x$

$$\log x = x$$

$$xD = D'; x^2 D^2 = D'(D'-1)$$

$$= 2D'^2 D'$$



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(D)
$$[D'^{2} - D' + D' + A]y = x S f n Z$$

$$[D'^{2} + A]y = x S f n Z$$

$$[D'^{2} + A]y = x S f n Z$$

$$M^{2} = -4$$

$$m = \pm 2i$$

$$CF = A \cos 2x + B S f n Z Z$$

$$PT = \frac{1}{D'^{2} + A} x S f n Z$$

$$= x \frac{1}{D'^{2} + A} S f n Z - \frac{2D'}{(D^{2} + A)^{2}} S f n Z$$

$$= x \frac{1}{-1 + A} S f n Z - \frac{a \cos Z}{(-1 + A)^{2}}$$

$$= \frac{z S f n Z}{3} - \frac{a \cos Z}{3}$$

$$The Solve is$$

$$S = A \cos 2x + B S f n Z + \frac{x S f n Z}{3} - \frac{a \cos Z}{3}$$

$$= A \cos 2(\log x) + B S f n Z + \frac{x S f n Z}{3} - \frac{a \cos Z}{3}$$

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$$= A \cos 2(\log x) + B S f n Z +$$



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(1)
$$\Rightarrow$$
 ($D^{12} - D^{1} - D^{1} + 1$) $y = x$
($D^{2} - 2D^{1} + 1$) $y = x$
AE $m^{3} - am + 1 = 0$
($m + 1$) ($m - 1$) $= 0$
 $m = 1$, 1
 \therefore $CF = (A + Bx) e^{x}$
PI = $\frac{1}{D^{12} - 2D^{1} + 1}$
= $[1 + (D^{2} - 2D^{1})]^{-1} x$
= $[-(D^{12} - 2D^{1})]^{-1} x$
= $x - D^{13} x + aD^{1}(x)$
PI = $x + 2$
 \therefore The Soln. $\%$ $y = CF + PT$
 $y = (A + Bx)e^{x} + x + 2$
Scanned with $(A + B \log x) x + \log x + 2$
CamScanner