

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

SNS COLLEGE OF TECHNOLOGY



Cauchy's Linear Differential Equation

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J. Solve  $x^2 y'' + 2xy' = 0$ Soln Gaven  $(x^2 D^2 + 2 \times D)y = 0 \longrightarrow (1)$ Take 2=02 z = log 2 x D = D' $a^2 D^2 = D' (D' - I) = D'^2 - D'$ Subs. the above 90 (1), JD2- D'+2D]y= 0  $\int D'^2 + D]y = 0$  $m^2 + m = 0$   $D' \rightarrow m$ AE m(m+1) = 0m=0, m=-1CF = Aeox + Be- X = A + Bet .'. The soln. PS, y = CF = A + Be - log x  $\overrightarrow{R}. \text{ Solve } x^2 \frac{d^2 y}{dx^2} = 3x \frac{dy}{dx} + 4y = x SPD(log x).$ Given  $(z^2 b^2 - 3z b + 4) y = z Sin(\log z)$   $\downarrow(i)$ 801n. Take z=ez  $x = \log x$ x D = D' $x^2 D^2 = D'(D' - I) = D'^2 - D'$ Subs. the above 9n(1)  $\left[D^{\prime 2} - D^{\prime} - 3D^{\prime} + 4Jy = e^{\chi} SPn \chi\right]$  $\int D'^2 - 4D' + 4 ] Y = e^{\chi} SPh \chi$  $m^2 - 4m + 4 = 0$ AE  $(m_{-2})^2 = 0$ m = 2, 2Scanned with CamScanner



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Cauchy's Linear Differential Equation

$$CF = (A + Bz) e^{\frac{2}{3}z}$$

$$CF = [A + B \log x] z^{\frac{2}{3}}$$

$$PI = \frac{1}{p!^{2} - Ap' + 4} e^{\frac{z}{3}} S^{n} z$$

$$= e^{\frac{z}{3}} \frac{1}{(p' + l)^{2} - A(p' + l) + 4} S^{n} z$$

$$= e^{\frac{z}{3}} \frac{1}{(p' + l)^{2} - A(p' + l) + 4} S^{n} z$$

$$= e^{\frac{z}{3}} \frac{1}{p'^{2} - 2p' + l} S^{n} z$$

$$= e^{\frac{z}{3}} \frac{1}{p'^{2} - 2p' + l} S^{n} z$$

$$= e^{\frac{z}{3}} \frac{1}{p'^{2} - 2p' + l} S^{n} z$$

$$= e^{\frac{z}{3}} \frac{1}{(-2p' + l)} S^{n} z$$

$$= e^{\frac{z}{3}} \frac{1}{(-2p' + l)} S^{n} z$$

$$= e^{\frac{z}{3}} \frac{1}{(-2p' + l)} S^{n} z$$

$$= \frac{e^{\frac{z}{3}}}{-\frac{2}{2}} \left[ \frac{1}{p'} S^{n} z \right]$$

$$= \frac{e^{\frac{z}{3}}}{-\frac{2}{3}} \left[ \frac{1}{p'} S^{n} z \right]$$

$$FI = \frac{e^{\frac{z}{3}} (\cos z)}{2} \Rightarrow PI = \frac{z \log(\log z)}{2}$$

$$S = Scanne^{\frac{z}{3}} vz^{\frac{1}{3}} + B \log z \right] z^{\frac{2}{3}} + \frac{z (\cos(\log z))}{2}$$