



(An Autonomous Institution) Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS Homogeneous Linear ODE with constant coefficients

UPP# - I

Differential Equation.

An eqn. Throlving differentfal coefficients on descriptions is called differential agn.

advancy differential egn.

A defected egn. which depends on only one Prolopondent voulable is called orderwy differential egn.

order and degree:

* The order of the bighest descriptive occurring in the grn. ogn is called the order of a defficiented ogn.

* The degree of the beginst desirvative occurring In the grn. egn. Is called the degree of a defferented egn.

Second order Penear ODE with constant wefficients: The general 19 noas O.D. with constant wetter cents is of the form

 $a_0 \frac{d^h y}{dx^h} + a_1 \frac{d^{h-1} y}{dx^{h-1}} + a_2 \frac{d^{h-2} y}{dx^{h-2}} + \dots + a_{h-1} y = f(x)$

where ap, a,, ... an are constants and

f(x) & a junction of x.

when f(n)=0 90 (1) se called homogeneous ODE & If f(N) to 9n (1) is called non-homogeneous ODE.





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This agn. can be written as, [ao Dh + a, Dh-1 + az Dh-2 + ... + an) y = f(x) where D = d

Solution = CF+ PI = Complementary function + Partiquilar lote

TO find EF:

Roots

CF

1). Roots are real & deferent mit ma i

`n). Roots are real & Same $m_1 = m_2 = m$

Roots are maginary.

(or complex) exx [A cor px + B 59n p: m= a± iB

TO fend pI:

 $PI = \frac{1}{f(D)} f(x)$

RHS = 0

J. Solve (D-5D+6)=0 Boln.

The auxiliary egg. 38 $(m^2 - 5m + 6 = 0)$ (m-3)(m-2)=0

m=2,3

i. The 9100HS are speal and althornent.





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CF =
$$Ae^{0x} + Be^{3x}$$
 $\therefore y = Cf = Ae^{0x} + Be^{3x}$
 $\exists J$. Solve $\frac{d^3y}{dx^2} - 6\frac{dy}{dx} + 9y = 0$

Soln.

($B^2 - 6D + 9$) $y = 0$

The Auxiliary eqn g_0
 $M^2 - 6m + 9 = 0$
 $(m-3)^2 = 0$
 $m = 3$, 3

The Looks are real and same.

 $cf = (A + Bx)e^{3x}$
 $\therefore y = cF = (n + Bx)e^{3x}$
 $\exists J$. Solve $(B^2 + 1)^2y = 0$

Soln.

The Auxiliary eqn. B $(m^2 + 1)^2 = 0$
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$$(m^{2})^{2} - 1^{2} = 0$$

$$(m^{2}+1) (m^{2}-1) = 0$$

$$m^{2}+1 = 0 \quad |m^{2}-1| = 0$$

$$m^{2}=-1 \quad |m^{2}=1|$$

$$m=\pm i \quad |m=\pm 1|$$

$$m=\pm i \quad |m=\pm 1|$$

$$i. cf = Ae^{2} + Be^{-2} + c \cos x + D Sin x$$