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Giauss Seidel method : Solve by Gauss Seider method : $\chi + 4 + 5 + 2 = 110$ a7x + 6y - 5z = 856x + 15y + 2z = 72soln: Let us rearrange the equations, 27x+6y-5z=85-70 $6x + 15y + 2z = 72 \rightarrow 2$ $x + y + 54z = 110 \rightarrow 3$. 27/7 161+15) 115/ > 161 +121 (54) > 111+111 $(i) = \alpha = \frac{85 - 6y + 5z}{27}$ $(a) =) \quad y = \frac{7a - 6x - az}{15}$ $(3) \rightarrow Z = \underbrace{110 - x - y}_{54.}$

Let y = z = o

Theration No	$X = \frac{85 - 6y + 5z}{27}$	$y = \frac{7a - 6x - az}{15}$	$Z = \frac{110 - \varkappa - 5}{54}$
	3.148	3.541	1.913
2	2.432	3.572	1.926
3	2.426	3.573	1.926
4	2.425	3.573	1.926
5	2-425	3.573	1.926





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$$Z = \frac{1}{10} (24 - 0.9933 - 3 \times 1.5070) = 1.8486$$

Fifth iteration :

$$\begin{aligned} \chi &= \frac{1}{28} \left(32 - 4 \times 1.5070 + 1.8486 \right) = 0.9936 \\ Y &= \frac{1}{17} \left(35 - 2 \times 0.9936 - 4 \times 1.8486 \right) = 1.50696 \\ Z &= \frac{1}{10} \left(24 - 0.9936 - 3 \times 1.50696 \right) = 1.8486 \end{aligned}$$
th iteration:

Sixth iteration:

$$\alpha = \frac{1}{28} \left(32 - 4 \times 1.50696 + 1.8486 \right) = 0.9936$$

 $y = \frac{1}{17} (35 - 2 \times 6.9936 - 4 \times 1.848) = 1.50696$ $z = \frac{1}{10} (a_4 - 0.9936 - 3 \times 1.50696) = 1.8486$

The solution is,
$$\chi = 0.9936$$
, $y = 1.50696$ & $Z = 1.8486$

(4) Solve the following system by Gauss-Seidel method: $9\chi - y + 2\chi = 9$ $\chi + 10y - 2\chi = 15$ $2\chi - 2y - 13\chi = -17$ Solution: The given system of equations are,

$$qx - y + 2z = 9 \longrightarrow (1)$$

$$x + 10y - 2z = 15 \longrightarrow (2)$$

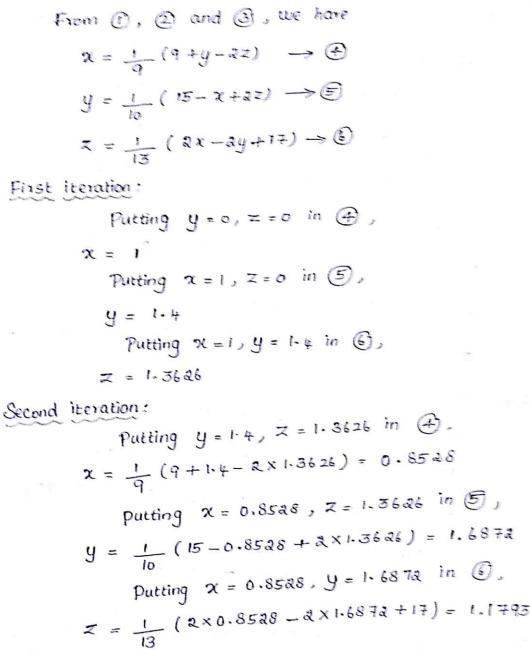
$$2x - 2y - 13z = -17 \longrightarrow (3)$$

Clearly the coefficient matrix is diagonally dominant, we can apply Gauss-Seider method.



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Third iteration: $\chi = \frac{1}{9} (9 + 1.6872 - 2 \times 1.1793) = 0.9254$ $y = \frac{1}{10} (15 - 0.9254 + 2 \times 1.1793) = 1.6433$



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$$Z = \frac{1}{13} (2 \times 0.9254 - 2 \times 1.6433 + 17) = 1.1972$$

Fourth iteration:

$$X = \frac{1}{9} (9 + 1.6433 - 2 \times 1.1972) = 0.9165$$

$$Y = \frac{1}{10} (15 - 0.9165 + 2 \times 1.1972) = 1.6478$$

$$Z = \frac{1}{13} (2 \times 0.9165 - 2 \times 1.6478 + 17) = 1.1952$$

Fifth iteration:

$$\begin{aligned} \chi &= \frac{1}{9} \left(9 + 1.6478 - 2 \times 1.1952 \right) = 0.9175 \\ y &= \frac{1}{10} \left(15 - 0.9175 + 2 \times 1.1952 \right) = 1.6473 \\ z &= \frac{1}{13} \left(2 \times 0.9175 - 2 \times 1.6473 + 17 \right) = 1.1954 \end{aligned}$$

Sixth iteration:

$$\chi = \frac{1}{9} (9 + 1.6473 - 2 \times 1.1954) = .0.9174$$

$$y = \frac{1}{10} (15 - 0.9174 + 2 \times 1.1954) = 1.6473$$

$$Z = \frac{1}{13} (2 \times 0.9174 - 2 \times 1.6473 + 17) = 1.1954$$
The solution is .

$$\chi = 0.9174 + 9 = 1.6473, \quad \chi = 1.1954$$

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