



(An Autonomous Institution) Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Method of variation of parameters

IJ. Solve
$$\frac{d^2y}{dx^2} + y = esc x$$
 using method of variation of parameters.

Solon.

Given
$$(p^2+1)$$
 $y = CSC \times AE$
 $M = 0$
 $M^2 = -1$
 $M = \pm 1$
 $M = -1$
 M

 $= \int \cos x \times \frac{1}{\text{Sqn} x} \, dx = \int \cot x \, dx$

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$$= \int \frac{\cos^{9}x}{89n \times} dx$$

$$= \int \frac{1 - 89n^{2}x}{89n \times} dx$$

$$= \int [cscx - s9nx] dx$$

$$= \int cscx dx - \int s9nx dx$$

$$= -log [cscx + cotx] + cos x$$

$$\therefore PI = -89nx cos x + flog (cscx + cotx) + cos x flog$$
The general sdp. 9s,
$$3 = cF + PI$$

$$= c_{1} cos x + c_{2} s9nx - s9nx cos x + flog (cscx + cotx)$$

$$+ c9nx cos x$$

$$= c_{1} cos x + c_{2} s9nx + log (cscx + cotx) s9nx.$$

4]. Solve (p3+a3) y = Sec ax using method of variation of Parameters. Soln.

Gren
$$(D^2 + \alpha^2)y = Sec qx$$

$$m^2 + \alpha^2 = 0$$

$$m^2 = -\alpha^2$$

$$m = \pm \alpha i$$

$$Cf = C_1 \cos qx + C_2 \sin qx$$
Here $f_1 = \cos qx$

$$f_1 = -\alpha \sin qx$$

$$f_2 = \sin qx$$

$$\omega = f_1 f_2 - f_1 f_2$$

$$= \cos qx (\alpha \cos qx) + \alpha \sin qx$$

$$= \alpha \cos^2 qx + \alpha \sin^2 qx$$

$$= \alpha [\cos^2 qx + \sin^2 qx] = \alpha(1) = \alpha$$
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UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Method of variation of parameters

PI = Pf, +8f₂

$$P = -\int \frac{f_2 \times dx}{w} dx$$

$$= -\int \frac{S^2 n \, ax \, Sec \, ax}{a} dx = -\int \frac{1}{a} \tan ax \, dx$$

$$= -\int \frac{1}{a} \int \frac{S^2 n \, ax}{a} dx = -\int \frac{1}{a} \tan ax \, dx$$

$$= +\int \frac{1}{a} \log \frac{(Sec \, ax)}{a} \int \frac{1}{a} \tan ax + \frac{1}{a} \log \frac{(Sec \, ax)}{a}$$

$$P = -\int \frac{1}{a^2} \log \frac{(Sec \, ax)}{a} dx$$

$$= \int \frac{f_1 \times dx}{w} dx$$

$$= \int \frac{\cos ax \, Sec \, ax}{a} dx$$

$$= -\int \frac{1}{a^2} \int \frac{1}{a^2} \cos ax + \frac{1}{a} \int \frac{1}{a^2} \sin ax + \frac{1}{a} \int \frac{1}{a^2} \log \frac{(Sec \, ax)}{a} \cos ax + \frac{1}{a} \int \frac{1}{a^2} \log \frac{(Sec \, ax)}{a} \cos ax + \frac{1}{a} \int \frac{1}{a^2} \log \frac{(Sec \, ax)}{a} \cos ax + \frac{1}{a^2} \cos \cos a$$