

## SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)
Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Cauchy's Linear Differential Equation

Solve 
$$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + 4y = \log x$$
 Sin( $\log x$ )

Soln.

Given  $\left[x^2 D^2 + x D + 4\right] y = \log x$  Sin( $\log x$ )

Take  $x = e^x$ 

$$\log x = x$$

$$xD = D \quad ; \quad x^2 D^2 = D \cdot (D - 1)$$

$$= D \cdot \int_{-\infty}^{\infty} x^2 D^2 = D \cdot (D - 1)$$



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(1) 
$$\int_{\mathbb{D}} D^{2} - D^{1} + D^{1} + A \int_{\mathbb{C}} y = x \operatorname{Sin} x$$

$$\int_{\mathbb{D}} D^{2} + A \int_{\mathbb{C}} y = x \operatorname{Sin} x$$

$$\int_{\mathbb{C}} D^{2} + A \operatorname{Sin} x = x \operatorname{Sin} x$$

$$\int_{\mathbb{C}} D^{2} + A \operatorname{Sin} x = x \operatorname{Sin} x$$

$$\int_{\mathbb{D}} D^{2} + A \operatorname{Sin} x = x \operatorname{Sin} x$$

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$$\int_{\mathbb{C}} D^{2} + A \operatorname{Sin} x = x \operatorname{Sin} x =$$



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Cauchy's Linear Differential Equation

(1) 
$$\Rightarrow$$
 ( $D^{12} - D^{1} - D^{1} + 1$ )  $y = x$   
( $D^{2} - 2D^{1} + 1$ )  $y = x$   
AE  $m^{3} - am + 1 = 0$   
( $m + 1$ ) ( $m - 1$ )  $= 0$   
 $m = 1$ , 1  
 $\therefore$   $CF = (A + Bx) e^{x}$   
PI =  $\frac{1}{D^{12} - 2D^{1} + 1} = \frac{1}{D^{12} - 2D^{1}$