



# SNS COLLEGE OF TECHNOLOGY

Coimbatore-35  
An Autonomous Institution



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## DEPARTMENT OF AEROSPACE ENGINEERING

### 19ASB304 – COMPUTATIONAL FLUID DYNAMICS FOR AEROSPACE APPLICATIONS III YEAR VI SEM

#### UNIT-III FINITE ELEMENT TECHNIQUES TOPIC: Piecewise defined shape functions

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## Piecewise-Defined Functions

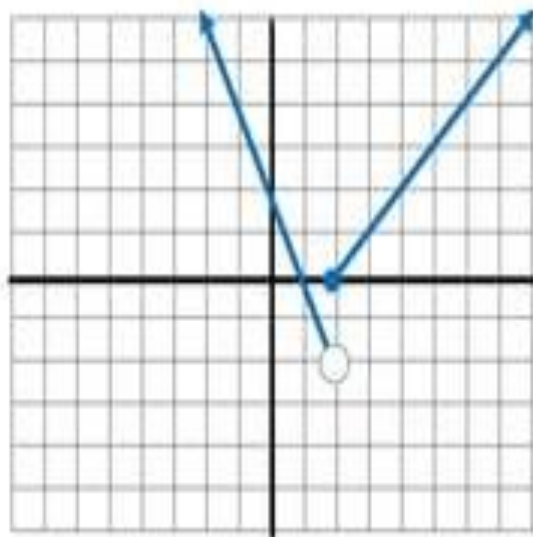
- Notice that this function is defined by different rules for different parts of its domain. Functions whose definitions involve more than one rule are called **piecewise-defined** functions.
- Graphing one of these functions involves graphing each rule over the appropriate portion of the domain.

# Example of a Piecewise-Defined Function



Graph the function

$$f(x) = \begin{cases} 2 - 2x & \text{if } x < 2 \\ x - 2 & \text{if } x \geq 2 \end{cases}$$



Notice that the point  $(2, 0)$  is included but the point  $(2, -2)$  is not.



- Up to now, we've been looking at functions represented by a single equation.
- In real life, however, functions are represented by a combination of equations, each corresponding to a part of the domain.
- These are called **piecewise functions**

# Piecewise Functions

many real-life problems, however, functions are represented by a combination of equations, each corresponding to a part of the domain. Such functions are called **piecewise functions**. For example, the piecewise function given by

$$f(x) = \begin{cases} 2x - 1, & \text{if } x \leq 1 \\ 3x + 1, & \text{if } x > 1 \end{cases}$$

is defined by two equations. One equation gives the values of  $f(x)$  when  $x$  is less than or equal to 1, and the other equation gives the values of  $f(x)$  when  $x$  is greater than 1.

$$f(x) = \begin{cases} 2x - 1, & \text{if } x \leq 1 \\ 3x + 1, & \text{if } x > 1 \end{cases}$$



- One equation gives the value of  $f(x)$  when  $x \leq 1$
- And the other when  $x > 1$



Evaluate  $f(x)$  when  $x=0$ ,  $x=2$ ,  $x=4$

$$f(x) = \begin{cases} x+2, & \text{if } x < 2 \\ \frac{2x+1}{1}, & \text{if } x \geq 2 \end{cases}$$

- First you have to figure out which equation to use
- You **NEVER** use both

$x=0$

This one fits into the top equation

So:

$$0+2=2$$

$x=2$

This one fits here

So:

$$2(2) + 1 = 5$$

$x=4$

This one fits here

So:

$$2(4) + 1 = 9$$



**Graph:**

$$f(x) = \begin{cases} \frac{1}{2}x + \frac{3}{2}, & \text{if } x < 1 \\ -x + 3, & \text{if } x \geq 1 \end{cases}$$

- For all  $x$ 's  $< 1$ , use the top graph (to the left of 1)
- For all  $x$ 's  $\geq 1$ , use the bottom graph (to the right of 1)



# Graphing a Piecewise Function

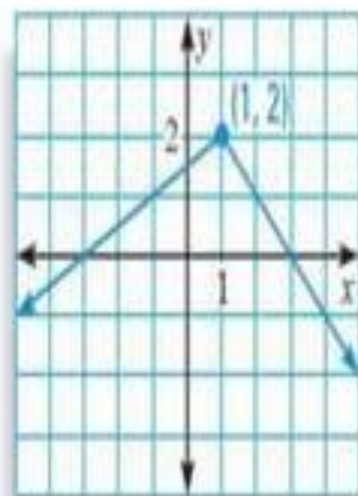
Graph this function:  $f(x) = \begin{cases} \frac{1}{2}x + \frac{3}{2}, & \text{if } x < 1 \\ -x + 3, & \text{if } x \geq 1 \end{cases}$

## SOLUTION

To the left of  $x = 1$ , the graph is given by  $y = \frac{1}{2}x + \frac{3}{2}$ .

To the right of and including  $x = 1$ , the graph is given by  $y = -x + 3$ .

The graph is composed of two rays with common initial point  $(1, 2)$ .



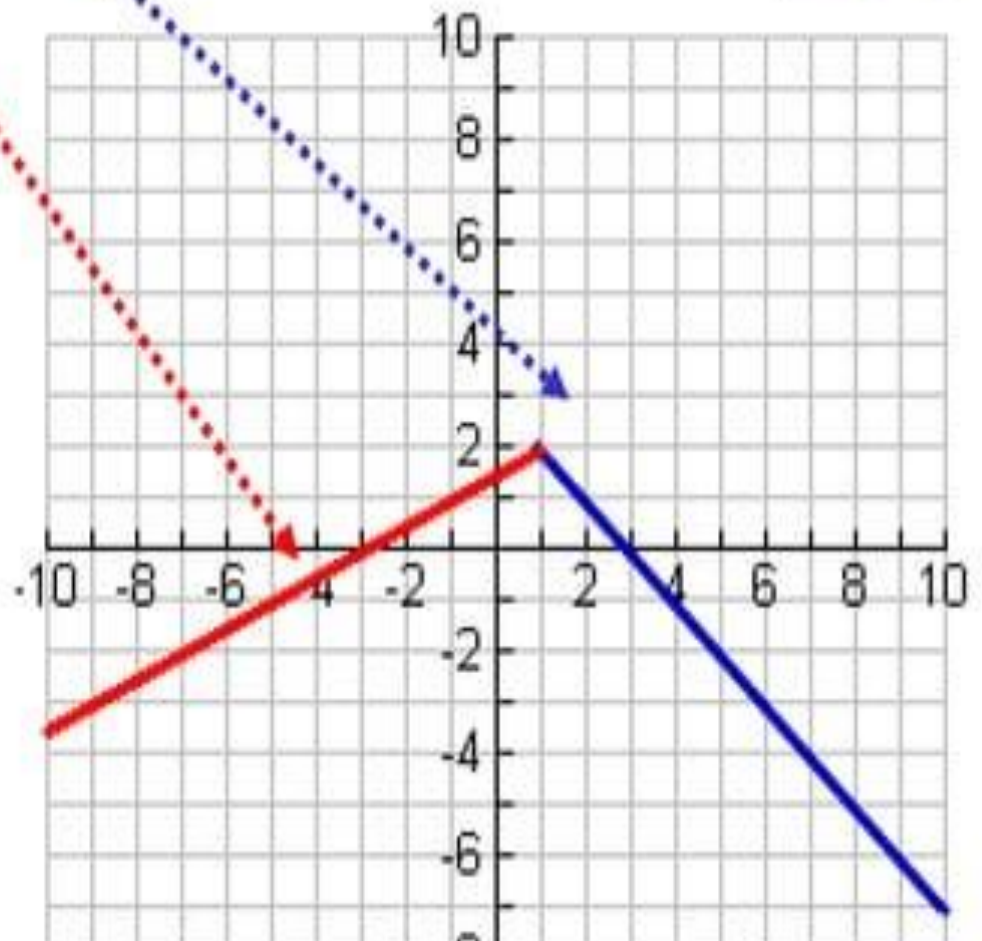
$$f(x) = \begin{cases} \frac{1}{2}x + \frac{3}{2}, & \text{if } x < 1 \\ -x + 3, & \text{if } x \geq 1 \end{cases}$$



$x=1$  is the breaking point of the graph.

To the left is the top equation.

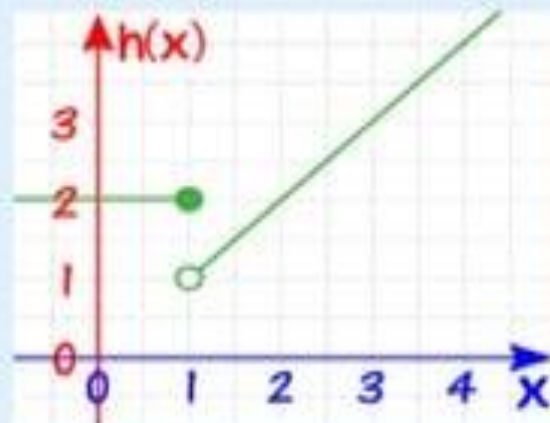
To the right is the bottom equation.



# Graph the function

$$h(x) = \begin{cases} 2, & \text{if } x \leq 1 \\ x, & \text{if } x > 1 \end{cases}$$

which looks like:



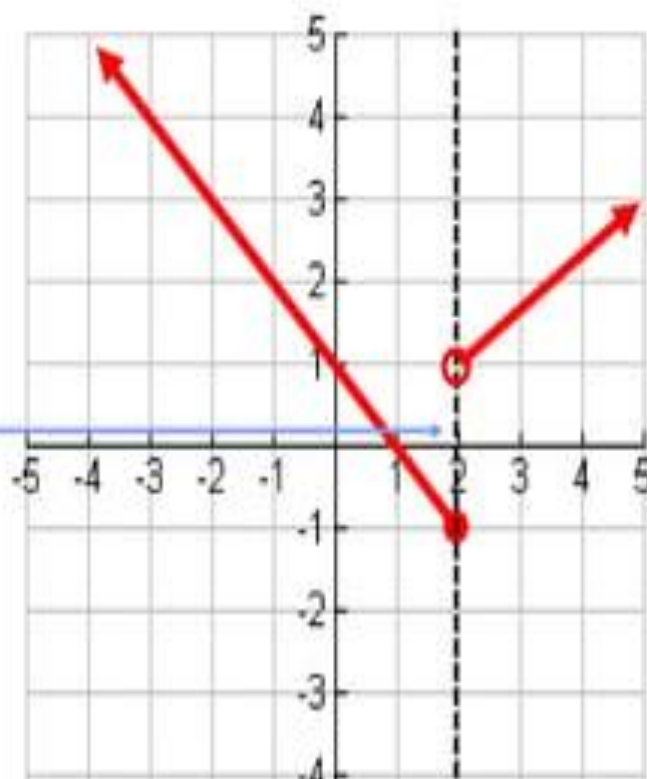
What is  $h(-1)$ ?  $x$  is  $\leq 1$ , so we use  $h(x) = 2$ , so  $h(-1) = 2$

# Graph:



$$f(x) = \begin{cases} x-1, & \text{if } x > 2 \\ -x+1, & \text{if } x \leq 2 \end{cases}$$

Point of Discontinuity



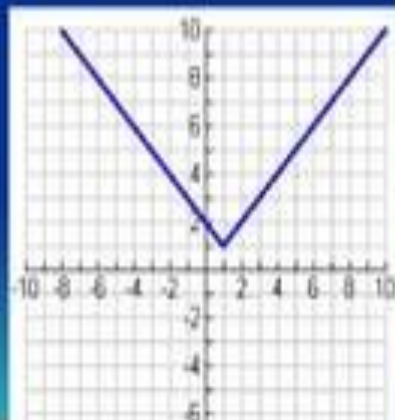
# Maxima and Minima

(aka extrema)

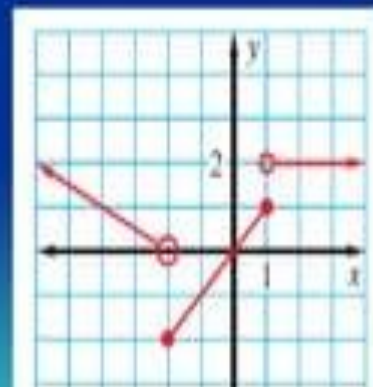
Highest point on the graph

Lowest point on the graph

In this function, the minimum is at  $y = 1$

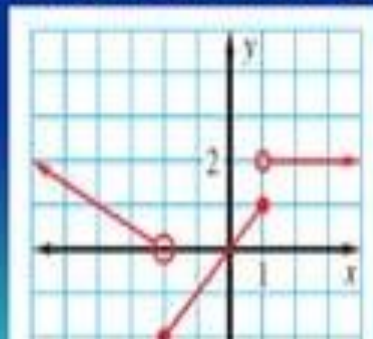


In this function, the minimum is at  $y = -2$



# Intervals of Increase and Decrease

- By looking at the graph of a piecewise function, we can also see where its slope is **increasing** (uphill), where its slope is **decreasing** (downhill) and where it is **constant** (straight line). We use the domain to define the 'interval'.



This function is decreasing on the interval  $x < -2$ , is increasing on the interval  $-2 \leq x \leq 1$ , and constant over  $x > 1$