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UNIT- 1 VECTOR CALCULUS

GAUSS DIVERGENCE THEOREM

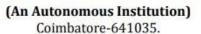
Gauss Divirgence theorem:

The furface integral of normal component of vector function F over a closed swiface & enclosing Volume V is equal to the volume integral of divergence of F taking through cut the volume V

i.e  $\iint \vec{F} \cdot \hat{n} \, ds = \iiint \vec{\nabla} \cdot \vec{F} \, dv$ 

Verify the gauss divergence theorem ( $\forall T D T$ ) for  $\vec{F} = H X \vec{T} - y^2 \vec{J} + y \vec{X} \vec{K}$ out the tube bounded by x = 0, x = 1 y = 0, y = 1, x = 0, x = 1Scanned with Eamscanner







**UNIT-1 VECTOR CALCULUS** GAUSS DIVERGENCE THEOREM SF. A de = SSS V. Folv F = HYII - Y'J' + YIR  $\overline{\nabla} \cdot \overline{F} = \left( \overrightarrow{i} \frac{\partial}{\partial x} + \overrightarrow{j} \frac{\partial}{\partial y} + \overrightarrow{i} \frac{\partial}{\partial z} \right) + \left( \frac{\partial}{\partial x} - \frac{\partial}{\partial z} \right) + \left( \frac{\partial}{\partial x} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} \right) + \left( \frac{\partial}{\partial x} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} \right) + \left( \frac{\partial}{\partial x} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} \right) + \left( \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} \right) + \left( \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} \right) + \left( \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} \right) + \left( \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} \right) + \left( \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} - \frac{\partial}{\partial z} \right) + \left( \frac{\partial}{\partial z} - \frac{\partial}{\partial z$  $= \frac{\partial}{\partial x} (H \times T) + \frac{\partial}{\partial y} (-y^2) + \frac{\partial}{\partial T} (yT)$  = HT - 2y + y = HT - y.  $\nabla \cdot \vec{F} = HT - y.$ RHI IST v. Folv = JSS(HZ-y) dudydz.  $= \iint_{x=0}^{\infty} (\mu \tau - y) dy dz$ =  $\iint_{x=0}^{\infty} (\mu \tau - y) dy dz.$  $= \int_{Q} (HTy - y_{12}^{2}) \int_{y=0}^{1} dt.$ =  $\int (HT - 1/2) dt.$  $= \left[ \frac{4t^2}{2} - \frac{1}{8} \right]_{a=0}^{a=0}$  $= \frac{4}{2} - \frac{1}{2}.$   $\iint \nabla \cdot \vec{F} \, dv = \frac{3}{2} - \frac{1}{2}.$ A

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### UNIT-1 VECTOR CALCULUS

GAUSS DIVERGENCE THEOREM

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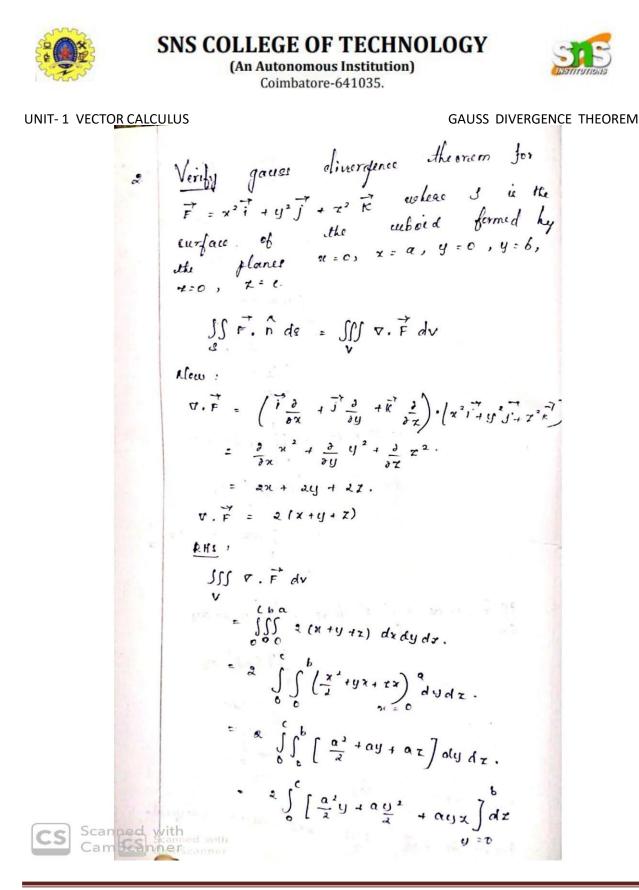
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UNIT-1 VECTOR CALCULUS

GAUSS DIVERGENCE THEOREM

$$F = \iint_{S_{1}} F \cdot \hat{n} ds = \iint_{S_{1}} F \cdot \hat{n} ds = \iint_{S_{2}} F \cdot \hat{n} ds = \iint_{S_{1}} Hz dy dz + \iint_{S_{1}} F \cdot \hat{n} ds = \iint_{S_{1}} Hz dy dz + 0 \cdot \\ = \iint_{S_{1}} F \cdot \hat{n} dz + \iint_{S_{1}} F \cdot \hat{n} ds = \iint_{S_{1}} Hz dy dz + 0 \cdot \\ = \iint_{A_{2}} Hz dz + \\ = H(\frac{z^{2}}{z})_{0}^{1} \cdot \\ = H_{A_{2}} \cdot \\ = \frac{z^{2}}{z} \cdot \\ = \int_{S_{1}} dz + \int_{S_{1}} F \cdot \hat{n} ds = -\iint_{S_{1}} dz dz + 0 \cdot \\ = \int_{S_{1}} [zJ]' dz \cdot \\ = -\int_{S_{1}} dz + \int_{S_{2}} F \cdot \hat{n} ds - \int_{S_{1}} [zJ]' dz \cdot \\ = -\int_{S_{1}} dz - (z)_{0}^{1} \cdot \\ = -1 \quad$$

$$\iint_{S_{5}} F \cdot \hat{n} ds + \iint_{S_{5}} F \cdot \hat{n} ds - \int_{S_{1}} \int_{S_{1}} y dz dy \cdot \\ = -\int_{S_{1}} dy \cdot \\ = \int_{S_{1}} y dy \cdot \\ = \int_{S_{1}} \int_{S_{1}} \int_{S_{1}} dy \cdot \\ = \int_{S_{1}} \int_{S_{1}} dy \cdot \\ = \int_{S_{1}} \int_{S_{1}} \int_{S_{1$$







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UNIT- 1 VECTOR CALCULUS					GAUSS DIVERGENCE THEOREM		
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UNIT-1 VECTOR CALCULUS

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GAUSS DIVERGENCE THEOREM

$$= \sigma^{2}bc$$

$$\iint \vec{F} \cdot \vec{n} \, ds + \iint \vec{f} \cdot \vec{n} \, dr = \iint \vec{b} \cdot \vec{b} \, dz \, dz + o.$$

$$= b^{2} \int m \, dt$$

$$= b^{2} a \int dz.$$

$$= b^{2} a \int dy.$$

$$= c^{2} \int a \, dy.$$

$$= c^{2} a \int dy.$$

$$= b^{2} \int dy.$$

$$=$$