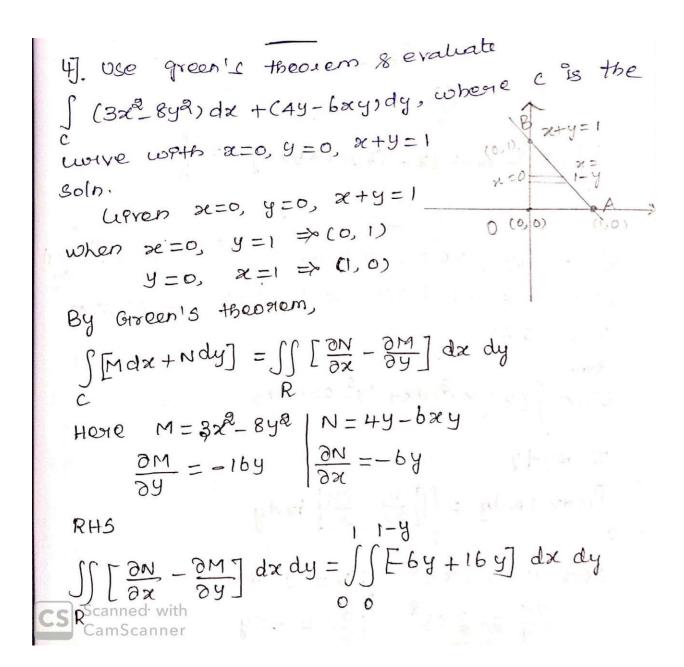




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UNIT-1 VECTOR CALCULUS

GREEN'S THEOREM







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UNIT-1 VECTOR CALCULUS

GREEN'S THEOREM

$$= \iint_{10}^{10} y \, dx \, dy$$

$$= 10 \iint_{10}^{10} y \, dx \, dy = 10 \iint_{10}^{10} y \left[x \right]_{10}^{10} dy$$

$$= 10 \iint_{10}^{10} y \left[1 - y - 0 \right] \, dy$$

$$= 10 \left[\frac{y^2}{2} - \frac{y^3}{3} \right]_{10}^{10} = 10 \left[\frac{1}{2} - \frac{1}{3} \right]_{10}^{10}$$

$$= 10 \left[\frac{3 - 2}{6} \right]_{10}^{10}$$

$$= \frac{10}{6}$$

$$= \frac$$





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UNIT-1 **VECTOR CALCULUS** **GREEN'S THEOREM**

RHS
$$\iint_{\Omega} \left[\frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right] dx dy = \iint_{\Omega} \left[-ay + 3xy^2 \right] dx dy$$

$$= \iint_{\Omega} \left[-ayx + 3\frac{x^2}{2}y^2 \right]^2 dy$$

$$= \iint_{\Omega} \left[-4y + \frac{3}{2}(4)y^2 \right] dy$$

$$= \iint_{\Omega} \left[-4y + \frac{3}{2}(4)y + \frac{3}{2}(4)y^2 \right] dy$$

$$= \iint_{\Omega} \left[-4y + \frac{3}{2}(4)y + \frac{3}{2}(4)y$$

evaluate S[Mdx+Ndy], we shall LHS

c In the different paths.

i). Along on
$$[y=0]$$
ii). Along AB $[x=2]$
iii). Along BC $[y=2]$
iv). Along CO $[x=0]$

Along OA
$$[y=0 \Rightarrow dy=0]$$

$$\int (x^2 - xy^3) dx + (y^2 - 2xy) dy$$

$$= \int [x^2 - 0] dx + [0 - 0](0)$$

canned with
$$x^2$$
 and x^3 $= \left[\frac{x^3}{3}\right]^{3}$





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Along AB
$$(x=2 \Rightarrow dx=0)$$

$$\int (x^{2}-xy^{3})dx + (y^{2}-2xy)dy$$

$$= \int (-4-2y^{3})(0) + (y^{2}-4y)dy$$

$$= \int \frac{y^{3}}{3} - \frac{4y^{3}}{2} \int_{0}^{2}$$

$$= \left(\frac{8}{3} - 2(4)\right) - 0 = \frac{8}{3} - 8$$

$$= \frac{8-24}{3}$$

$$= -\frac{16}{3}$$
Along Bc $(y=3 \Rightarrow dy=0)$

$$\int (x^{2}-xy^{3})dx + (y^{2}-2xy)dy$$

$$= \int (x^{2}-xy^{3})dx + (y^{2}-2xy)dy$$

$$= \int (x^{2}-xy^{3})dx + 0$$

$$= \int [x^{2}-8x]dx$$

$$= \int \frac{x^{3}}{3} - \frac{x^{3}}{2} \int_{0}^{2}$$

$$= 0 - \left(\frac{8}{3} - 4(4)\right) = -\left[\frac{8-48}{3}\right]$$

$$= \frac{40}{3}$$





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Along co
$$x=0 \Rightarrow dx=0$$

$$\int (x^{2}-xy^{3})dx + (y^{2}-2xy)dy$$

$$= \int [0+(y^{2}-0)dy]$$

$$= \int y^{3}dy$$

$$= \left[\frac{y^{3}}{3}\right]_{2}^{0}$$

$$= 0-8/3$$

$$= -8/3$$

$$= -8/3$$

$$= (x^{2}-xy^{3})dx + (y^{2}-2xy)dy = \frac{-8\cdot 16+40+8}{3}$$

$$= \frac{2^{2}+3}{3}$$

. LHO = RHS Hence veribred

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