

Boats & Streams

①

- 1) Still water - "boat speed"
- 2) running water - with flow of the river \rightarrow "Stream Speed".

4 Basic Concepts

① Downstream = along the river (water direction)

Speed ↑ → Time ↓

② Upstream = against the river (opposite direction of water)

Speed ↓ → Time ↑

Speed (\propto) Velocity of stream (ab) Velocity of the current.

$$\text{Down stream} = \text{Boat speed} + \text{Stream speed}$$

$$\text{Upstream} = \text{Boat speed} - \text{Stream speed}$$

② Always boat speed must be greater than stream.

$$\text{Boat speed of boat} = \frac{DS + US}{2}$$

$$\text{Speed of Stream} = \frac{DS - US}{2}$$

P
S/T

$$D = S \times T$$

$$DS = (B \cdot S + S \cdot S) \times T$$

$$US = (B \cdot S - S \cdot S) \times T$$

- (1) A man can row downstream at 11 km/hr and upstream at 7 km/hr . Find the speed of man at still water and stream?

$$\text{Speed of Boat} = \frac{D.S + U.S}{2} = \frac{11+7}{2} = \frac{18}{2} = 9 \text{ km/hr}$$

$$\text{Stream Speed} = \frac{D.S - U.S}{2} = \frac{11-7}{2} = \frac{4}{2} = 2 \text{ km/hr.}$$

- (2) A boat covers a distance of 40 kms downstream in 2 hrs while it takes 4 hrs to cover the same distance upstream. What is the speed of the boat in still water in km/hr.

$$D.S = \frac{40}{2} = 20 \text{ km/hr} \quad (\text{D.S. speed})$$

$$U.S = \frac{40}{4} = 10 \text{ km/hr} \quad (\text{U.S. speed})$$

$$\text{Speed of boat} = \frac{D.S + U.S}{2} = \frac{20+10}{2} = \frac{30}{2} = 15 \text{ km/hr}$$

- (3) The rate of stream is 12 km/hr and the ratio between the speeds of boat in downstream & the speed of the boat in upstream is $8:5$. What is the speed of the boat in still water?

(3)

$$\text{Ans: } D.S : U.S$$

$$8 : 5$$

$$8x : 5x$$

$$\text{boat Speed} = \frac{D.S + U.S}{2}$$

we know stream speed = 12 km/hr

$$S.S = \frac{D.S - U.S}{2} = \frac{8x - 5x}{2}$$

$$12 = \frac{3x}{2}$$

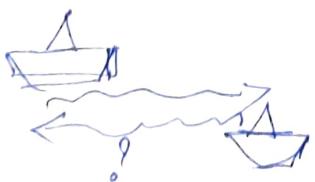
$$24 = 3x$$

$$x = 8$$

$$D.S = 64 \text{ km/hr}$$

$$\text{Speed of boat} = \frac{D.S + U.S}{2} = \frac{64 + 40}{2} = \frac{104}{2} = 54 \text{ km/hr}$$

(4) The speed of boat is 15 km/hr & speed of stream is 4 km/hr less than the speed of the boat. Find the time to travel 1045 km upstream and return back to starting point-



$$\text{Boat speed} = 15 \text{ km/hr}$$

$$\text{Stream speed} = 4 \text{ km/hr}$$

$$S/T \quad T = \frac{D}{S}$$

$$\text{Total time} = \frac{D}{S_{U.S}} + \frac{D}{S_{D.S}}$$

$$= \frac{1045}{B+S.S} + \frac{1045}{B-S.S} = \frac{1045}{15-4} + \frac{1045}{15+4}$$

$$= \frac{1045}{11} + \frac{1045}{19} = 95 + 55 = 150 \text{ hrs.}$$

(4)