



COIMBATORE-35

UNIT -3 / SOLUTION OF EQUATION AND EIGEN VALUE PROBLEMS
DEPARTMENT OF MATHEMATICS

value of $x = 2.4255$, $y = 3.5730$ and $z = 1.9260$.

(Use Gauss Seidel method)

GAUSS SEIDAL METHOD ∴

If in each equation of the system, the absolute value of the largest co-efficient is greater than the sum of the absolute value of the remaining co-efficient, co-efficient Matrix should be diagonally dominant...

① Solve the system of equation by Gauss Seidal Method...

$$\begin{aligned} 27x + 6y - z &= 85 \\ x + y + 54z &= 110 \\ 6x + 15y + 2z &= 72 \end{aligned}$$

By diagonally dominant rule, ...

$$\begin{aligned} 27x + 6y - z &= 85 \rightarrow \textcircled{1} \\ 6x + 15y + 2z &= 72 \rightarrow \textcircled{2} \\ x + y + 54z &= 110 \rightarrow \textcircled{3} \end{aligned}$$

The system of equation can be written as the equation 1, 2, & 3.

Now, ...

$$\begin{aligned} x &= \frac{85 - 6y + z}{27} \rightarrow \textcircled{4} \\ y &= \frac{72 - 6x - 2z}{15} \rightarrow \textcircled{5} \\ z &= \frac{110 - x - y}{54} \rightarrow \textcircled{6} \end{aligned}$$

$$\begin{aligned} A &= \frac{85 - 6B + C}{27} \\ B &= \frac{72 - 6A - 2C}{15} \\ C &= \frac{110 - A - B}{54} \end{aligned}$$

Iteration... let $x_0 = y_0 = z_0 = 0$. let $x = y = z = 0$



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3.1481	3.5400	1.9132
2.4323	3.5720	1.9258
2.4257	3.5729	1.9260
2.4255	3.5730	1.9260
<u>2.4255</u>	<u>3.5730</u>	<u>1.9260</u>

∴ value of $x = 2.4255$, $y = 3.5730$
 $z = 1.9260$.

②. Solve the system of equation by Gauss Seidal method:

$$\begin{aligned} 6x + 3y + 12z &= 35 \\ 8x - 3y + 2z &= 20 \\ 4x + 11y - z &= 33 \end{aligned}$$

$$\begin{aligned} \textcircled{8}x - 3y + 2z &= 20 \rightarrow \textcircled{1} \\ 4x + \textcircled{11}y - z &= 33 \rightarrow \textcircled{2} \\ 6x + 3y + \textcircled{12}z &= 35 \rightarrow \textcircled{3} \end{aligned}$$

∴ This implies the equation is diagonally dominant.



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From (1), $x = \frac{20 + 3y - 2z}{8} \rightarrow (4)$

By ... $y = \frac{33 - 4x + z}{11} \rightarrow (5)$

$z = \frac{35 - 6x - 3y}{12} \rightarrow (6)$

Iteration ...

Let ... $y = z = 0$

$x = \frac{1}{8}(20 + 3y - 2z)$

$y = \frac{1}{11}(33 - 4x + z)$

$z = \frac{1}{12}(35 - 6x - 3y)$

1.	2.5000	2.0909	1.1439
2.	2.9981	2.0138	0.9142
3.	3.0266	1.9929	0.9051
4.	3.0211	1.9837	0.9102
5.	3.0163	1.9859	0.9120
6.	3.0167	1.9859	0.9118
7.	3.0168	1.9859	0.9118
8...	<u>3.0168</u>	<u>1.9859</u>	<u>0.9118</u>

Value of $x = 3.0168$, $y = 1.9859$ and $z = 0.9118$

③. Solve the system of equation by Gauss Seidal Method.

$28x + 4y - z = 32$

$x + 3y + 10z = 24$

$2x + 17y + 4z = 35$

The given equation can be written as:

$28x + 4y - z = 32 \rightarrow (1)$

$2x + 17y + 4z = 35 \rightarrow (2)$

$x + 3y + 10z = 24 \rightarrow (3)$



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$$x = \frac{32 - 4y + z}{28} \rightarrow (4)$$

$$y = \frac{35 - 2x - 4z}{17} \rightarrow (5)$$

$$z = \frac{24 - 3y - x}{10} \rightarrow (6)$$

Iteration ∴ Let $(y=z=0)$.

$x = \frac{32 - 4y + z}{28}$	$y = \frac{35 - 2x - 4z}{17}$	$z = \frac{24 - 3y - x}{10}$
1.1429	1.9244	1.7084
0.9290	1.5476	1.8428
0.9876	1.5090	1.8485
0.9933	1.5070	1.8486
0.9936	1.5070	1.8485
<u>0.9936</u>	<u>1.5070</u>	<u>1.8485</u>

∴ $x = 0.9936$, $y = 1.5070$, $z = 1.8485$