



SNS COLLEGE OF TECHNOLOGY

Coimbatore-20
An Autonomous Institution



Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A++' Grade
Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

19ECT212 – CONTROL SYSTEMS

II YEAR/ IV SEMESTER

UNIT I – CONTROL SYSTEM MODELING

TOPIC 5- MODELING OF ELECTRIC SYSTEMS



OUTLINE



- REVIEW ABOUT PREVIOUS CLASS
- TYPES OF SYSTEMS
- DYNAMIC SYSTEMS
- WAYS TO STUDY A SYSTEM
- MODEL & ITS NEEDS,TYPES
- ACTIVITY
- MODELING OF ELECTRICAL SYSTEMS(R,L,C)
- V-I AND I-V RELATIONS
- EXAMPLES
- SUMMARY



TYPES OF SYSTEMS



- **Static System:** If a system does not change with time, it is called a static system.
- **Dynamic System:** If a system changes with time, it is called a dynamic system.



DYNAMIC SYSTEMS



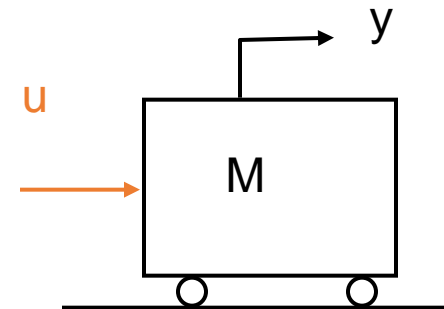
- A system is said to be dynamic if its current output may depend on the past history as well as the present values of the input variables.
- Mathematically,

$$y(t) = \varphi[u(\tau), 0 \leq \tau \leq t]$$

u : Input, t : Time

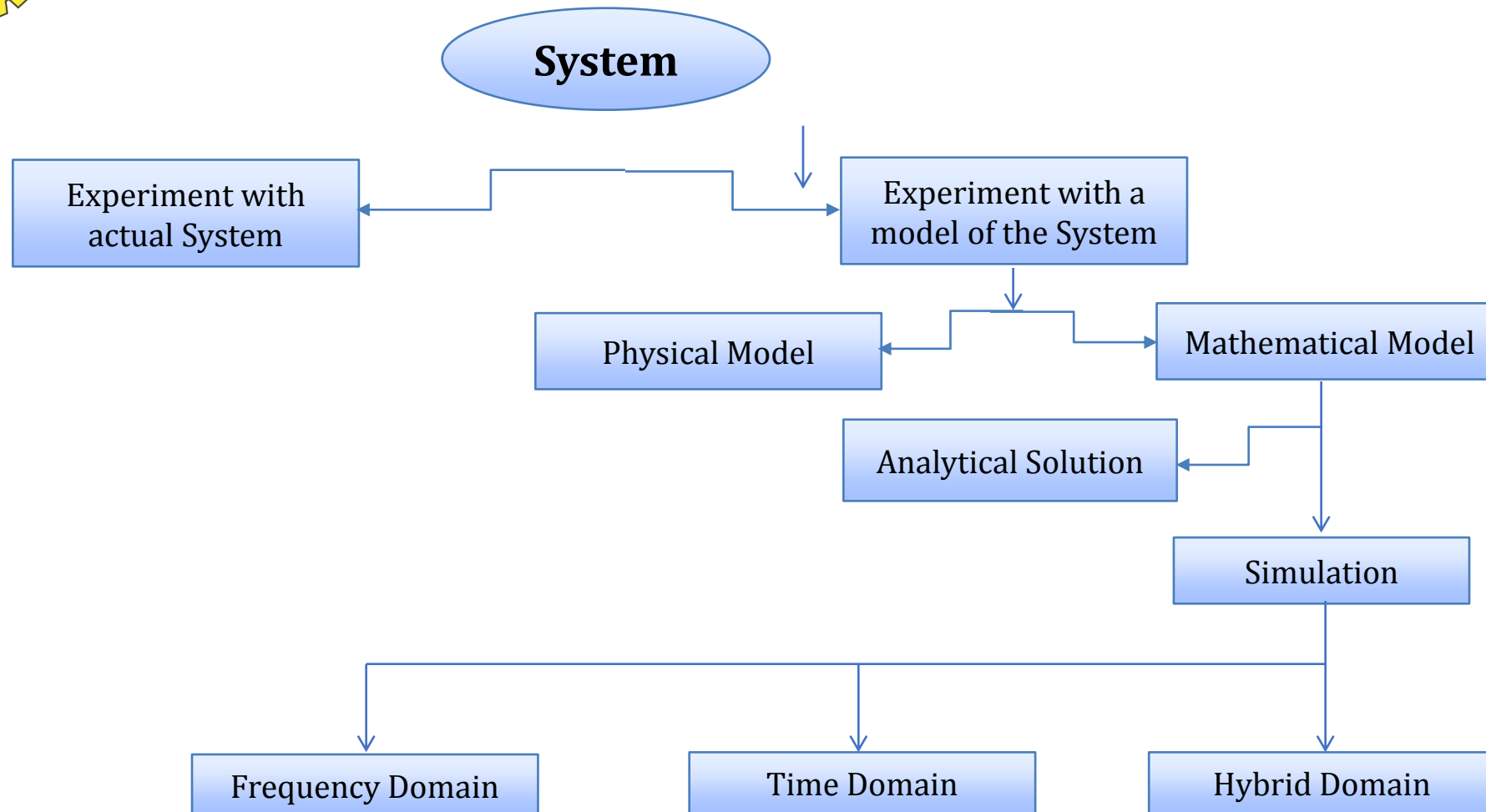
Example: A moving mass

Model: Force=Mass x Acceleration





WAYS TO STUDY A SYSTEM





MODEL

- A *model* is a simplified representation or abstraction of reality.
- Reality is generally too complex to model exactly.

A set of mathematical equations (e.g., differential eqs.) that describes the input-output behavior of a system.

What is a model used for?

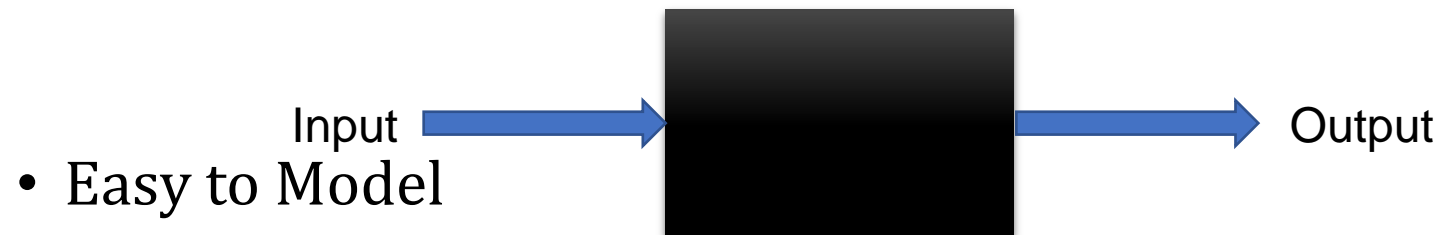
- Simulation
- Prediction/Forecasting
- Prognostics/Diagnostics
- Design/Performance Evaluation
- Control System Design



BLACK BOX MODEL



- When only input and output are known.
- Internal dynamics are either too complex or unknown.

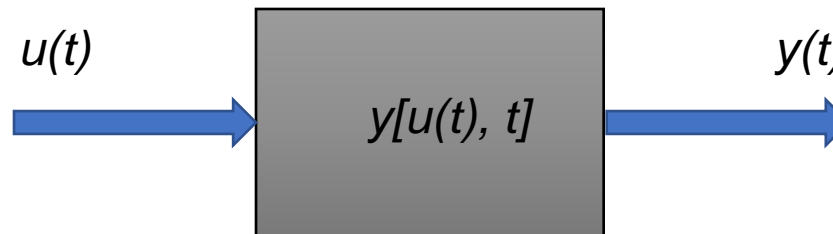




GREY BOX MODEL



- When input and output and some information about the internal dynamics of the system is known.



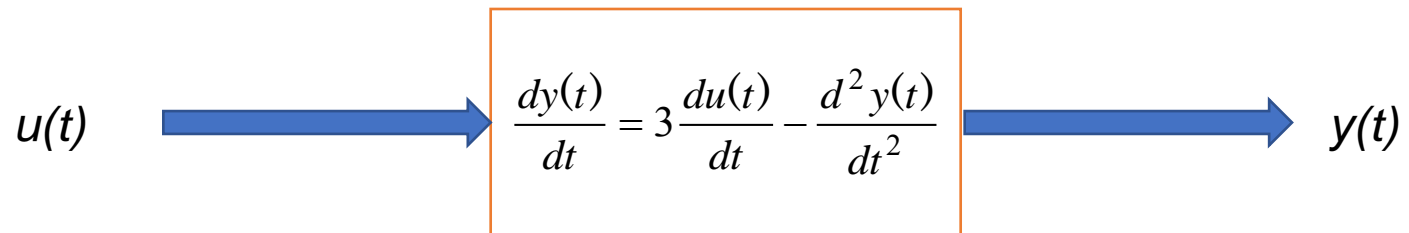
- Easier than white box Modelling.



WHITE BOX MODEL



- When input and output and internal dynamics of the system is known.



- One should know complete knowledge of the system to derive a white box model.



ACTIVITY



Fill the empty circle

① ② ③
④ ⑤ ④ ⑥ ⑦
② ① ⑩ ④ ⑥ ③
⑥ ⑦ ○ ⑧ ⑨
② ⑥ ⑧



BASIC ELEMENTS OF ELECTRICAL SYSTEMS



Symbol →



- The time domain expression relating voltage and current for the resistor is given by Ohm's law

$$v_R(t) = i_R(t)R$$

- The Laplace transform of the above equation is

$$V_R(s) = I_R(s)R$$



BASIC ELEMENTS OF ELECTRICAL SYSTEMS



- The time domain expression relating voltage and current for the Capacitor is given as:

$$v_c(t) = \frac{1}{C} \int i_c(t) dt$$

- The Laplace transform of the above equation (assuming there is no charge stored in the capacitor) is

$$V_c(s) = \frac{1}{Cs} I_c(s)$$



BASIC ELEMENTS OF ELECTRICAL SYSTEMS



- The time domain expression relating voltage and current for the inductor is given as:

$$v_L(t) = L \frac{di_L(t)}{dt}$$




- The Laplace transform of the above equation (assuming there is no energy stored in inductor) is

$$V_L(s) = LsI_L(s)$$



V-I AND I-V RELATIONS

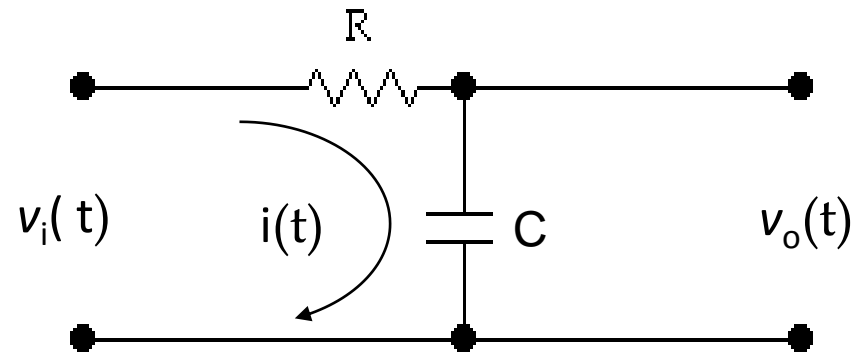


Component	Symbol	V-I Relation	I-V Relation
Resistor		$v_R(t) = i_R(t)R$	$i_R(t) = \frac{v_R(t)}{R}$
Capacitor		$v_c(t) = \frac{1}{C} \int i_c(t) dt$	$i_c(t) = C \frac{dv_c(t)}{dt}$
Inductor		$v_L(t) = L \frac{di_L(t)}{dt}$	$i_L(t) = \frac{1}{L} \int v_L(t) dt$



EXAMPLE 1

- The two-port network shown in the following figure has $v_i(t)$ as the input voltage and $v_o(t)$ as the output voltage. Find the transfer function $V_o(s)/V_i(s)$ of the network.



$$v_i(t) = i(t)R + \frac{1}{C} \int i(t) dt \qquad v_o(t) = \frac{1}{C} \int i(t) dt$$



EXAMPLE 1



$$v_i(t) = i(t)R + \frac{1}{C} \int i(t)dt \qquad v_o(t) = \frac{1}{C} \int i(t)dt$$

- Taking Laplace transform of both equations, considering initial conditions to zero.

$$V_i(s) = I(s)R + \frac{1}{Cs} I(s) \qquad V_o(s) = \frac{1}{Cs} I(s)$$

- Re-arrange both equations as:

$$V_i(s) = I(s)\left(R + \frac{1}{Cs}\right) \qquad CsV_o(s) = I(s)$$



EXAMPLE 1



$$V_i(s) = I(s)\left(R + \frac{1}{Cs}\right)$$

$$CsV_o(s) = I(s)$$

- Substitute $I(s)$ in equation on left

$$V_i(s) = CsV_o(s)\left(R + \frac{1}{Cs}\right)$$

$$\frac{V_o(s)}{V_i(s)} = \frac{1}{Cs\left(R + \frac{1}{Cs}\right)}$$

$$\frac{V_o(s)}{V_i(s)} = \frac{1}{1 + RCs}$$



EXAMPLE 1



$$\frac{V_o(s)}{V_i(s)} = \frac{1}{1 + RCs}$$

- The system has one pole at

$$1 + RCs = 0 \quad \Rightarrow \quad s = -\frac{1}{RC}$$



EXAMPLE 2

- Design an Electrical system that would place a pole at -3 if added to the other system.

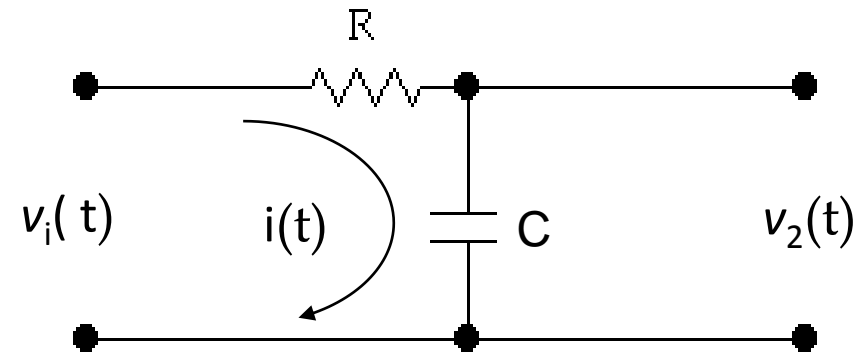
$$\frac{V_o(s)}{V_i(s)} = \frac{1}{1 + RCs}$$

- System has one pole at

$$s = -\frac{1}{RC}$$

- Therefore,

$$-\frac{1}{RC} = -3 \quad \text{if} \quad R = 1 \text{ M}\Omega \quad \text{and} \quad C = 333 \text{ pF}$$





SUMMARY

