



SNS COLLEGE OF TECHNOLOGY

Coimbatore-35 An Autonomous Institution

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DEPARTMENT OF FOOD TECHNOLOGY

CONDUCTION

PROBLEMS & SOLUTIONS

Problem

The inner surface of furnace wall is at 200°C and outer surface at 50°C. Calculate the heat lost per m² area of the wall. If thermal conductivity of the brick is 0.5 W/m°C & the wall thickness is 200mm.



The wall of a boiler is made up of 250mm of the brick, $K_{FB} = 1.05 \text{ W/m K}$; 120 mm of insulation brick $K_{IB} = 0.15 \text{ W/m K}$, and 200 mm of red brick, $K_{RB} = 0.85 \text{ W/m K}$. The inner and outer surface temperatures of the wall are 850°C and 65°C respectively. Calculate the temperatures at the contact surfaces.



The rate of heat flow per square meter is

$$\frac{Q}{A} = q = \frac{(t_1 - t_4)}{\frac{x_1}{k_{FB}} + \frac{x_2}{k_{B}} + \frac{x_3}{k_{RB}}}$$

$$\frac{Q}{A} = \frac{1 \times (850 - 65)}{\frac{0.250}{1.05} + \frac{0.120}{0.15} + \frac{0.200}{0.85}}{\frac{0.65}{0.85}}$$

$$= 616.5 \text{ W/m}^2$$

$$\frac{Q}{A} = \frac{t_1 - t_2}{\frac{x_1}{k_{FB}}} = \frac{t_2 - t_3}{\frac{x_2}{k_{B}}} = \frac{t_3 - t_4}{\frac{x_3}{k_{RB}}}$$

$$\therefore \quad \frac{Q}{A} = \frac{t_1 - t_2}{\frac{x_1}{k_{FB}}} \Rightarrow 616.5 = \frac{850 - t_2}{0.250}$$

$$\Rightarrow \quad t_2 = 703^{0}\text{C}$$

Similarly t₃ can be determined from the relation

$$\frac{Q}{A} = \frac{t_2 - t_3}{\frac{x_2}{k_{IB}}} \Rightarrow 616.5 = \frac{703 - t_3}{0.120}$$
$$\therefore \Rightarrow t_3 = 209.8^{\circ}C$$

Scanned with CamScanner

The Boiler wall is made up of two layers, A & B. Thickness & Thermal conductivity of A are 240 mm and 0.2 W/m^oC respectively. For B, thickness & thermal conductivity are 525 mm and 0.3 W/m^oC respectively. Inner surface of A is maintained at 1000^oC and outer surface of B is maintained at 250^oC. If there is contact thermal resistance of 0.05^oC/W per unit area exists at the interface.

Cal. i. the heat lost per m² area

II. The temperature drop at the interface

Sol: Given, $T_1 = 1000^{\circ}C$, $T_4 = 250^{\circ}C$ $L_A = 240 \text{ mm} = 0.24 \text{ m}$ $L_B = 525 \text{ mm} = 0.525 \text{ m}$ $K_A = 0.2 \text{ W/m}^{\circ}C$ $K_B = 0.3 \text{ W/m}^{\circ}C$ $(R_{th})_{contact} = 0.05^{\circ}C/W$

 $\therefore \text{ Temperature drop at interface} = T_2 - T_3$ = 700 - 687.5 $= 12.5^{\circ}C$



Heat Lost per m² area.

$$\frac{Q}{A} = q = \frac{\Delta T}{\Sigma R_{th}} = \frac{\Delta T}{R_{th-A} + R_{th-contact} + R_{th-B}} \\
= \frac{T_1 - T_4}{\frac{L_A}{K_A} + R_{th-contact} + \frac{L_B}{K_B}} \\
= \frac{1000 - 250}{\frac{0.24}{0.2} + 0.05 + \frac{0.525}{0.3}} \\
= \frac{750}{3} = 250 W / m^2 \\
d \text{ also we can write.} \\
a = \frac{T_1 - T_2}{T_1 - T_2} = \frac{T_3 - T_4}{T_3 - T_4}$$

$$q = \frac{T_1 - T_2}{\frac{L_a}{K_A}} = \frac{T_3 - T_4}{\frac{L_8}{K_B}}$$

$$250 = \frac{1000 - T_2}{\frac{0.240}{0.2}} = \frac{T_3 - 250}{\frac{0.525}{0.3}}$$

$$1000 - T_2 = 250 \times \frac{0.24}{0.2}$$

$$1000 - T_2 = 300$$

$$\Rightarrow T_2 = 700^{\circ} C$$

$$T_3 - 250 = 250 \times \frac{0.525}{0.3}$$

$$T_3 = 687.5$$

A furnace wall 200 mm thick is made of a material having thermal conductivity of 1.45 W/m. K. The inner and outer surface are exposed to average temperatures of 350° C and 40° C respectively. If the gas and air film coefficients are 58 and 11.63 W/m² K respectively, find the rate of heat transfer through a wall of 2.5 square meters. Also, find the temperatures on the two sides of the wall.

Sol: Given, x = 200 mm = 0.2 m,
k = 1.45 W/mK, A = 2.5 m²
T_A = 350⁰C = 623 K, T_B = 40⁰C = 313 K,
h_A = 58 W/m² K, h_B = 11.63 W/m²K,
Rate of heat transfer, Q =
$$\frac{A(T_A - T_B)}{\frac{1}{h_A} + \frac{x}{k} + \frac{1}{h_B}}$$

= $\frac{2.5(623 - 313)}{\frac{1}{58} + \frac{0.2}{1.45} + \frac{1}{11.63}}$ = 3214 J/s
Let, T₁ = Temperature on the inner side of
the wall, and
T₂ = Temperature on the outside of the
wall.
Q = h_A.A(T_A - T₁)
3214 = 58 × 2.5(623 - T₁)
 \Rightarrow T₁ = 600.84 K = 327.84^oC
Similarly
Q = h_BA(T₂ - T_B)
3214 = 11.63×2.5(T₂ - 313)
T₂ = 423.5 K = 150.5^oC

A steam pipe of inner diameter 200 mm is covered with 50mm thick high insulated material of thermal conductivity $k = 0.01 \text{ W/m}^{\circ}\text{C}$. The inner and outer surface temperatures maintained at 500°C and 100°C respectively. Calculate the total heat loss per meter length of pipe?



A 25 cm steam main 225 meter long is covered with 5 cm of high temperature insulation (k=0.095 W/m K) and 4 cm of low temperature insulation (k=0.065 W/m K). The inner and outer surface temperatures as measured are 400°C and 50°C respectively. Neglect heat conduction through pipe material.

Determine

- i. The total heat loss per hour.
- ii. The total heat loss per sq. m of outer surface.
- iii. The heat loss per sq.m of pipe surface.
- iv. The temperature between the two layers of insulation.

Sol: Outside diameter of pipe, $d_1 = 25$ cm Outside diameter of first layer, $d_2 = 25 + 2 \times 5 = 35$ cm Outside diameter of second layer, $d_3 = 35 + 2 \times 4 = 43$ cm $k_1 = 0.095$ W/m K, $k_2 = 0.065$ W/m K

(i) Total heat loss,

$$Q_{total} = \frac{2\pi\ell (T_1 - T_3)}{\frac{\ln(d_2/d_1)}{k_1} + \frac{\ln(d_3/d_2)}{k_2}}$$

= $\frac{2\pi \times 225(400 - 50)}{\frac{\ln(35/25)}{0.095} + \frac{\ln(43/35)}{0.065}}$
= $73754 \text{ W} = \frac{73754 \times 3600}{1000} \text{ kJ/H}$
= 265515 kJ/h
(ii) Total heat lost per sq. m of outer surface
= $\frac{Q_{total}}{\pi d_3 \ell} = \frac{265515}{\pi \times 0.43 \times 225}$
= 873.5 kJ/h



(iv) For temperature between two layers $\frac{Q}{\ell} = \frac{2\pi k(t_1 - t_2)}{ln(d_2/d_1)}$ $\frac{73754}{225} = \frac{2\pi \times 0.095(400 - t_2)}{ln(35/25)}$ $\therefore \quad t_2 = 215^{\circ} \text{C}$ Water is pumped through an iron pipe (k=67.2 W/m² K), 2 meters long as the rate of 1000kg/min. The inner and outer diameters of the tube are 50mm and 60mm respectively. Calculate the rise in temperature of water when the outside of the tube is heated to a temperature of 600° C. The initial temperature of the water is 30° C.

Sol: Given, k = 67.2 W/mK, L = 2m, m = 1000 kg/min $r_1 = 25 \text{ mm} = 0.025 \text{ m},$ $r_2 = 30 \text{ mm} = 0.03 \text{ m},$ $T_1 = 600^0 C = 873 K$. $T_{wl} = 30^{\circ}C = 303 \text{ K}$ Let T_{w2} = Final temperature of water in K. Heat transferred through the tube per second, $Q = Mass \times Sp.$ Heat \times Rise in temperature. $=\frac{1000 \times 4.2(T_{w2} - 303)}{60}$ $= 70(T_{w2} - 303)kJ/s -----(i)$ We also know that $Q = \frac{2\pi\ell k (T_1 - T_2)}{\ln\left(\frac{r_2}{2}\right)}$

$$= \frac{2\pi \times 2 \times 67.2 \left[873 - \frac{(303 + T_{w2})}{2} \right]}{ln \left(\frac{0.03}{0.025} \right)}$$
$$= 4632 \left[873 - \frac{(303 + T_{w2})}{2} \right]$$
$$= 4632 \left(721.5 - \frac{T_{w2}}{2} \right)$$
$$= 4.632 \left(721.5 - \frac{T_{w2}}{2} \right) kJ/s - \dots (ii)$$

Equating equations (i) and (ii) $70(T_{w2} - 303) = 4.632 \left(721.5 - \frac{T_{w2}}{2}\right) kJ/s$

$$T_{w2} = 339.5 \text{ K} = 66.5^{\circ} \text{ C}$$

:. Rise in temperature = $T_{w2} - T_{w1} = 66.5 - 30 = 36.5^{\circ}C$ A spherical shaped vessel of 1.2 m diameter is 100 mm thick. Find the rate of heat leakage, if the temperature difference between the inner and outer surface is 200°C. Thermal conductivity of the material of sphere is 0.3kJ/m-h°C.

Sol: Given, Outside diameter of sphere $d_2 = 1.2 \text{ m}$ $r_2 = 0.6 m$ Inside diameter of sphere $= 1.2 - 2 \times 0.100 = 1 \text{ m}$ $r_1 = 0.5 m$ $t_1 - t_2 = 200^{\circ}C$, $k = 0.3 \text{ kJ/m}^{\circ}C$ Heat transfer in hollow sphere is given by, $Q = \frac{4\pi kr_{1}r_{2}(t_{1}-t_{2})}{(r_{2}-r_{1})}$ $4\pi \times 0.3 \times 0.5 \times 0.6 \times 200 = 2262 \text{ kJ/h}$ 0.100

A cylinder having its diameter 30 cm and length 60 cm, has hemispherical ends, giving an overall length of 90 cm. The cylinder which is maintained at a steady temperature of 60°C is covered to a depth of 5 cm with lagging which has a coefficient of conductivity of 0.14 W/mK. Calculate the rate of heat loss if the outer surface of lagging is at 30°C. Sol: Rate of heat loss from cylindrical portion $Q = \frac{2\pi\ell k(t_1 - t_2)}{\ln(r_2 / r_1)}$ $=\frac{2 \times \pi \times 0.6 \times 0.14(60 - 30)}{55} = 55 \text{ W}$ $\ln(20/15)$ Rate of heat loss from spherical portion $Q = \frac{4\pi k r_1 r_2 (t_1 - t_2)}{(r_2 - r_1)}$ $4\pi \times 0.14 \times 0.15 \times 0.20(60 - 30)$ 0.20 - 0.15= 31.667 WHence total heat loss = 55 + 31.66 = 86.667W

The temperature on the two surfaces of a 1000 mm thick steel plate, (k=50 W/m°C) having a uniform volumetric heat generation of 20x 10³ W/m³, are 300°C and 200°C. Determine the following: i) the temperature distribution across the plate

ii) the value and position of the maximum temperature, and

iii) the flow of heat from each surface of the plate



= 300 + (200(1 - x) - 100) x $t = 300 + 100x - 200 x^{2}$ (ii) In order to determine the position of maximum temperature, differentiating the above expression and equating it to zero, we obtain

$$\frac{dt}{dx} = 100 - 400 x = 0$$
$$x = \frac{100}{400} = 0.25 \text{ m or } 25 \text{ mm}$$

2.

The maximum temperature is $t_{max} = 300 + 100 \times 0.25 - 200 \times 0.25^2$ $= 312.5^{\circ}C$

(iii) The flow of heat from each surface of the plate, q1, q2:

The heat flow at the left face (x = 0) $q_{1} = -k A \left(\frac{dt}{dx}\right)_{x=0}$ $= -50 \times 1 \times (100 - 400 \text{ x})_{x=0}$ $= -5000 \text{ W/m}^{2}$

The negative sign signifies that the heat flo at the left face is in a direction opposite to th of measurement of the distance,

$$q_2 = 50 \times 1 \times (100 - 400 \text{ x})_{x=1}$$

= 50 × 1 × (100 - 400 × 1)
= -15000 W/m²

A 3 mm diameter wire (k=20 W/m°C, resistivity, ρ = 10x10⁻⁸ Ω m) 100 m long has a voltage of 100 V impressed on it. The outer surface of the wire is maintained at 100°C. Calculate the centre temperature of the wire. If the heated wire is submerged in a fluid maintained at 50°C, find the heat transfer coefficient on the surface of the wire. Sol: Given, Radius of wire, R = 1.5 mm = 0.0015 mLength of the wire, L = 100 mVoltage impressed = 100 VThermal conductivity, k = 20 W/m °CResistivity, $\rho = 10 \times 10^{-8} \Omega \text{m}$ The temperature of the wire, $t_w = 100 \text{ °C}$ Fluid temperature, $t_a = 50 \text{ °C}$

Resistance of the wire,
$$R = \frac{\rho L}{A}$$

= $\frac{10 \times 10^{-8} \times 100}{\pi \times 0.0015^2} = 1.415 \Omega$

Rate of heat generation,

$$Q_g = VI = \frac{V^2}{R} = \frac{100^2}{1.415} = 7067 W$$

∴ Rate of heat generation per unit volume $q_g = \frac{Q_g}{AL}$ $= \frac{7067}{\pi \times 0.0015^2 \times 100} = 9.998 \times 10^6 \text{ W/m}^3$

Centre temperature is given by

$$t_{max} = t_w + \frac{q_g}{4k} R^2$$

= 100 + $\frac{9.998 \times 10^6}{4 \times 20} \times 0.0015^2 = 100.28^{\circ} C$

Heat transfer coefficient, h:

$$t_{w} = t_{a} + \frac{q_{g}}{2h}.R$$

$$100 = 50 + \frac{9.998 \times 10^{6}}{2h} \times 0.0015$$

$$h = \frac{7498.5}{50} = 149.97 \text{ W}/\text{m}^{2} \text{°C}$$

The meat rolls of 25 mm diameter having k=1 W/m°C are heated up with the help of microwave heating for roasting. Thecentre temperature of the rolls in maintained at 100°C when the surrounding temperature is 30°C. The heat transfer coefficient on the surface of the meat roll is 20 W/m°C. Find themicrowave heating capacity required in W/m³. ol: Given, R = 0.0125 m, $k = 1 \text{ W/m}^\circ \text{ C}$; $t_{\text{max}} = 100^\circ \text{C}$, $t_a = 30^\circ \text{C}$, $h = 20 \text{ W/m}^{2\circ} \text{C}$.

Microwave heating capacity, q_g : The maximum temperature occurs at the centre and is given by

$$t_{max} = t_{a} + \frac{q_{g}}{2h} \times R + \frac{q_{g}}{4k} \times R^{2}$$

$$100 = 30 + \frac{q_{g} \times 0.0125}{2 \times 20} + \frac{q_{g} \times 0.0125^{2}}{4 \times 1}$$

$$q_g = \frac{(100 - 30)}{(0.0003125 + 0.00003906)}$$
$$= 1.991 \times 10^5 \text{ W/m}^3$$