



**SNS COLLEGE OF TECHNOLOGY**

**Coimbatore – 35**

**An Autonomous Institution**



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Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

**DEPARTMENT OF ELECTRONICS AND COMMUNICATION ENGINEERING**

19ECT311 / Wireless Communication

IV ECE/ VII SEMESTER

Unit IV - **MULTIPATH MITIGATION TECHNIQUES**

**Topic 2** : Equalization-Linear and Non-Linear equalization



# Introduction



## Two general categories

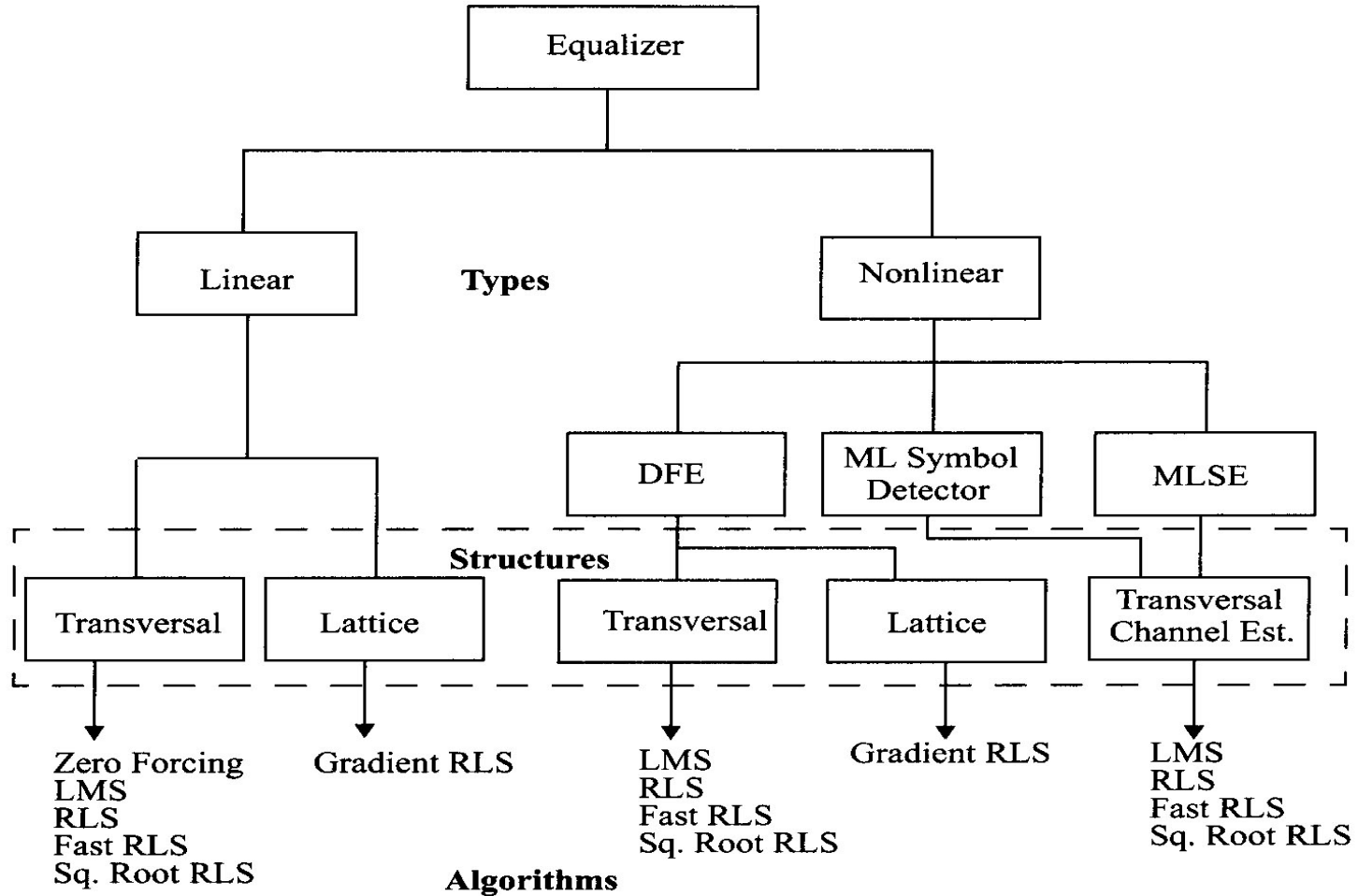
- Linear equalization
- Nonlinear equalization

## Based on

- How the output of an adaptive equalizer is used for subsequent control (feedback) of the equalizer



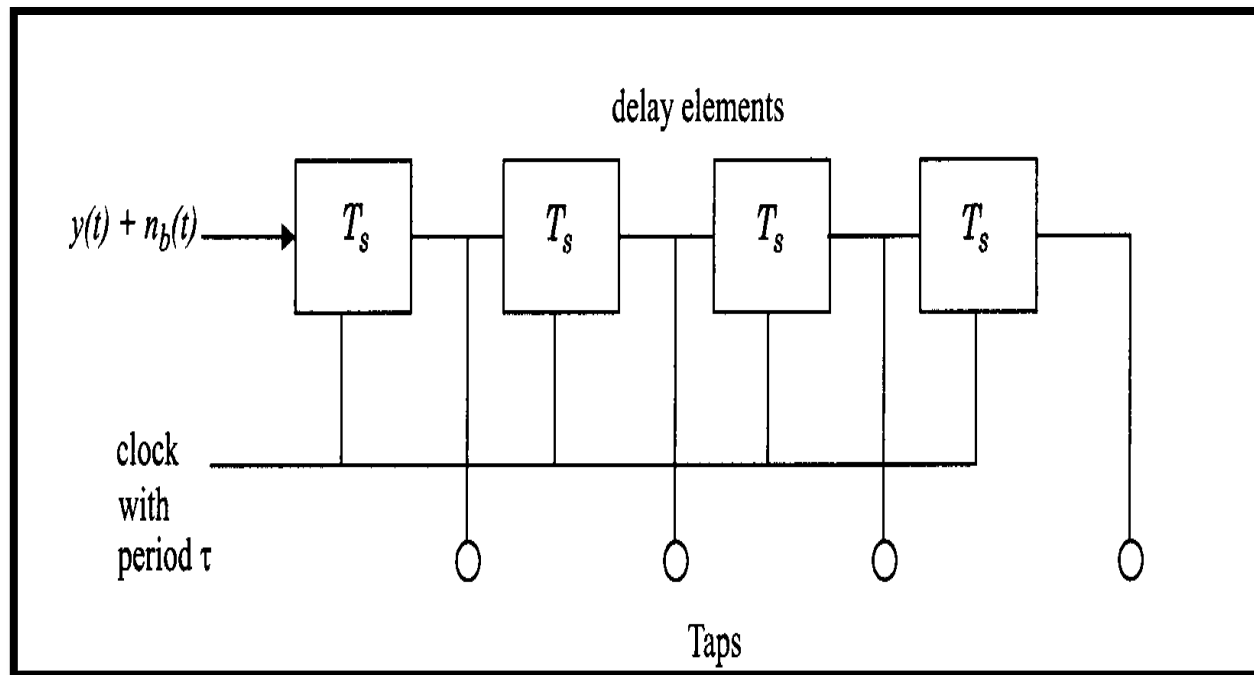
# Types





# Linear transversal equalizer

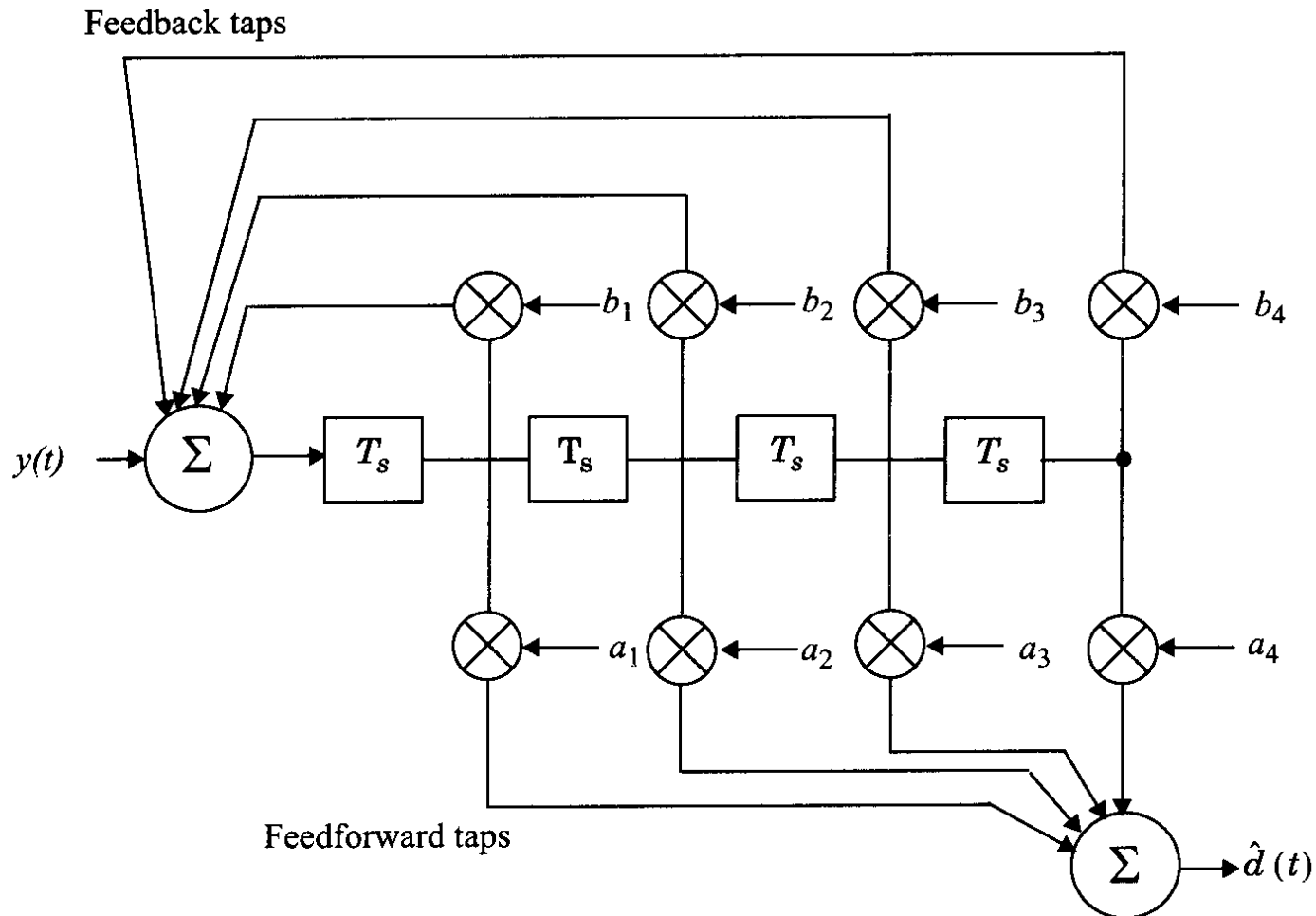
- Made up of tapped delay lines
- Tappings spaced a symbol period ( $T_s$ ) apart



Basic linear transversal equalizer structure



# Linear transversal equalizer



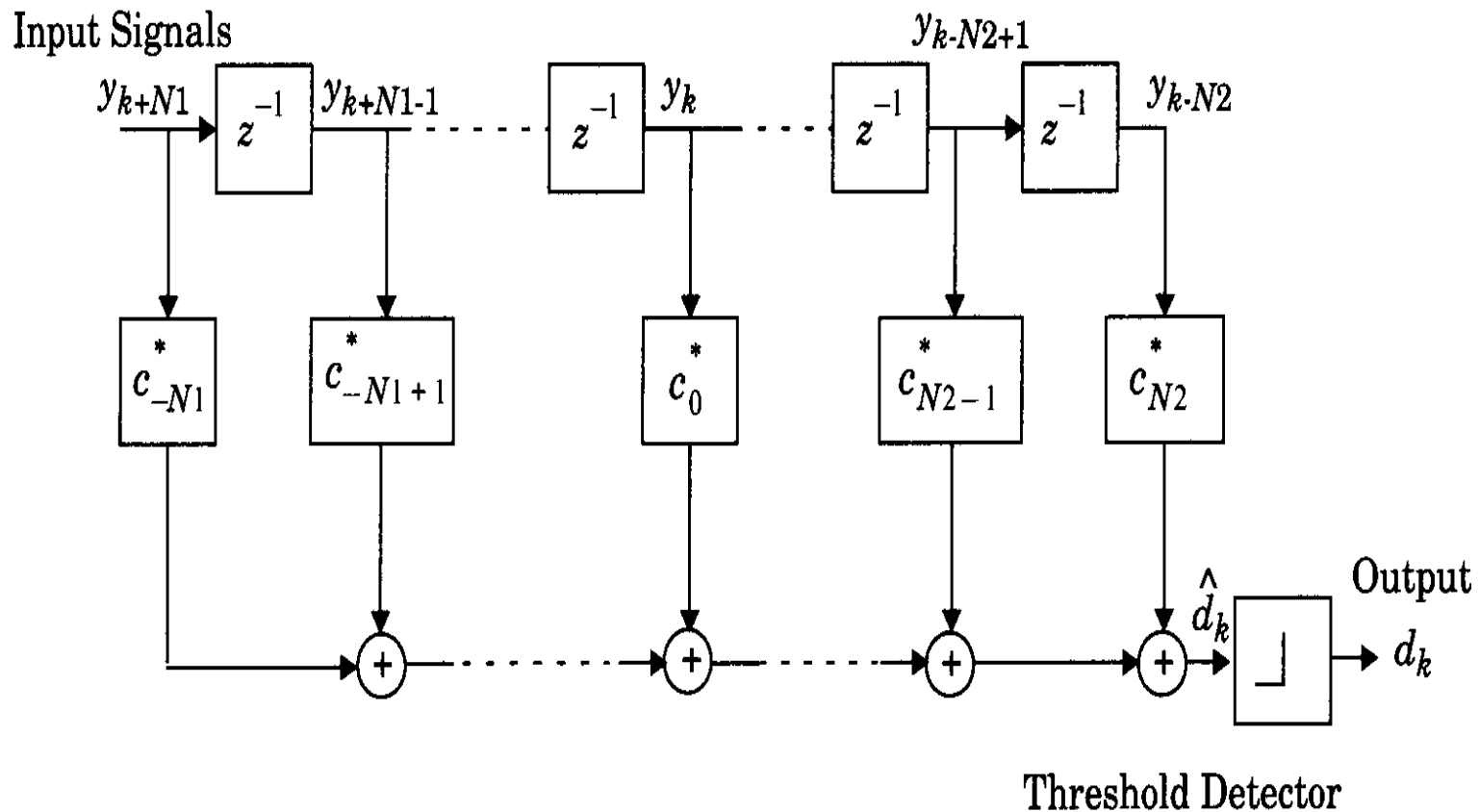
Tapped delay line filter with both feed forward and feedback taps



# Structure of Linear transversal equalizer



The current and past values of the received signal are linearly weighted by the filter coefficient and summed to produce the output





# Linear transversal equalizer



The minimum mean squared error  $E [e (n)]$  of a linear transversal equalizer can achieve is

$$\hat{\mathbf{d}}_k = \sum_{n=-N_1}^{N_2} \mathbf{C}_n^* \mathbf{y}_{k-n}$$

$$E[|e(n)|^2] = \frac{T}{2\pi} \int_{-\frac{\pi}{T}}^{\frac{\pi}{T}} \frac{N_o}{|F(e^{j\omega T})|^2 + N_o} d\omega$$

$F(e^{j\omega T})$  :Frequency response of the channel

$N_o$  :Noise spectral density



# Activity



- Imagine folding a paper in half once
- Then take the result and fold it in half again; and so on
- How many times can you do that?





# Nonlinear Equalization

- Used in applications where the channel distortion is too severe
- Three effective methods
  - Decision Feedback Equalization (DFE)
  - Maximum Likelihood Symbol Detection
  - Maximum Likelihood Sequence Estimator (MLSE)



# Decision Feedback Equalizer



- Basic idea : Once an information symbol has been detected and decided upon, the ISI that it induces on future symbols can be estimated and subtracted out before detection of subsequent symbols
- Realized in either the direct transversal form or as a lattice filter
- It consists of a feed forward filter (FFF) and a feedback filter (FBF)
- The FBF is driven by decisions on the output of the detector
- Its coefficients can be adjusted to cancel the ISI on the current symbol from past detected symbols



# DFE

The equalizer has

- $N_1 + N_2 + 1$  taps in the feed forward filter
- $N_3$  taps in the feedback filter

Its output

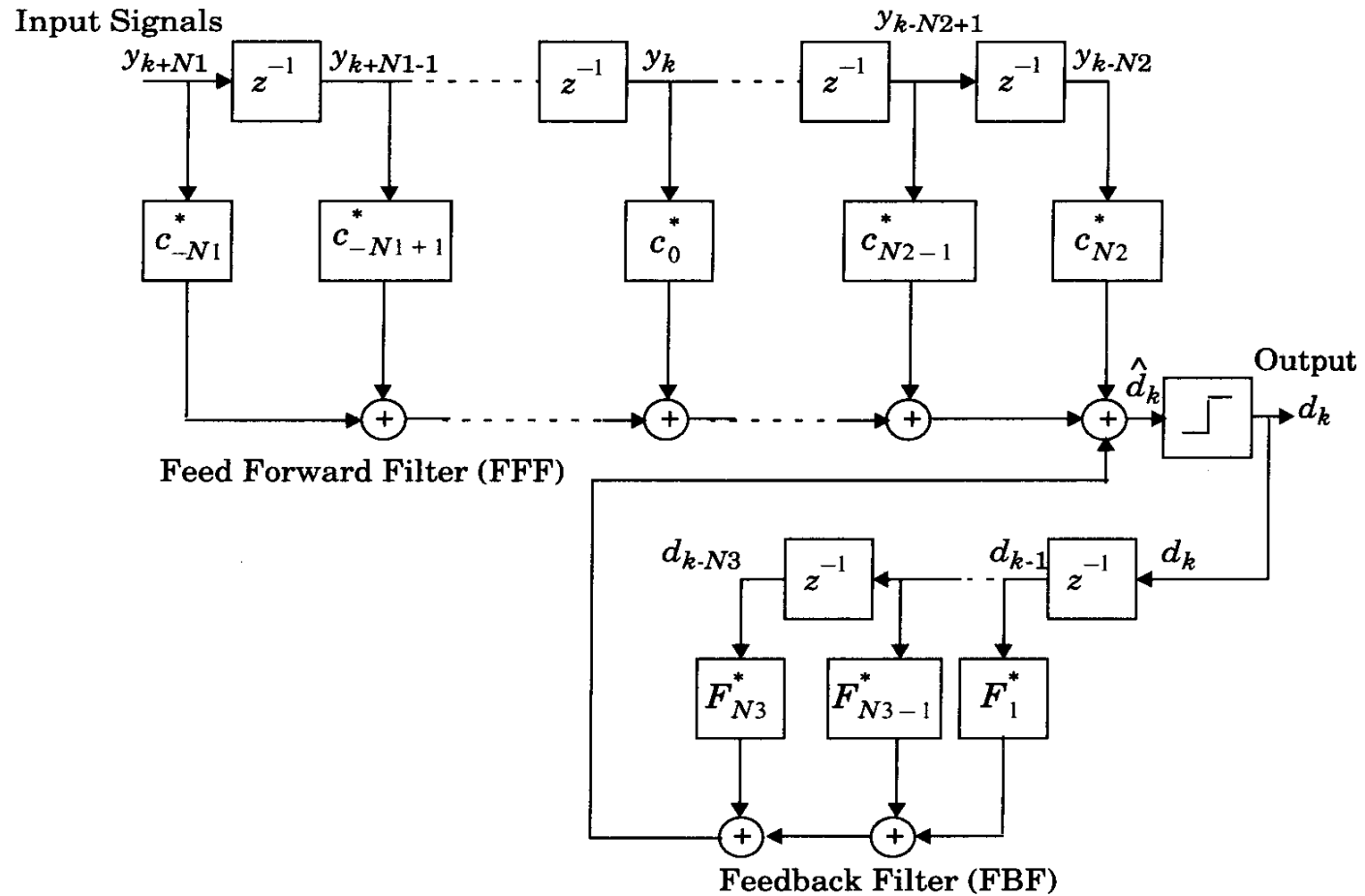
$$\hat{d}_k = \sum_{n=-N_1}^{N_2} C_n^* y_{k-n} + \sum_{i=1}^{N_3} F_i d_{k-i}$$

Minimum mean square error

$$E[|e(n)|^2]_{\min} = \exp \left\{ \frac{T}{2\pi} \int_{-\frac{\pi}{T}}^{\frac{\pi}{T}} \ln \left[ \frac{N_o}{|F(e^{j\omega T})|^2 + N_o} \right] d\omega \right\}$$



# DFE



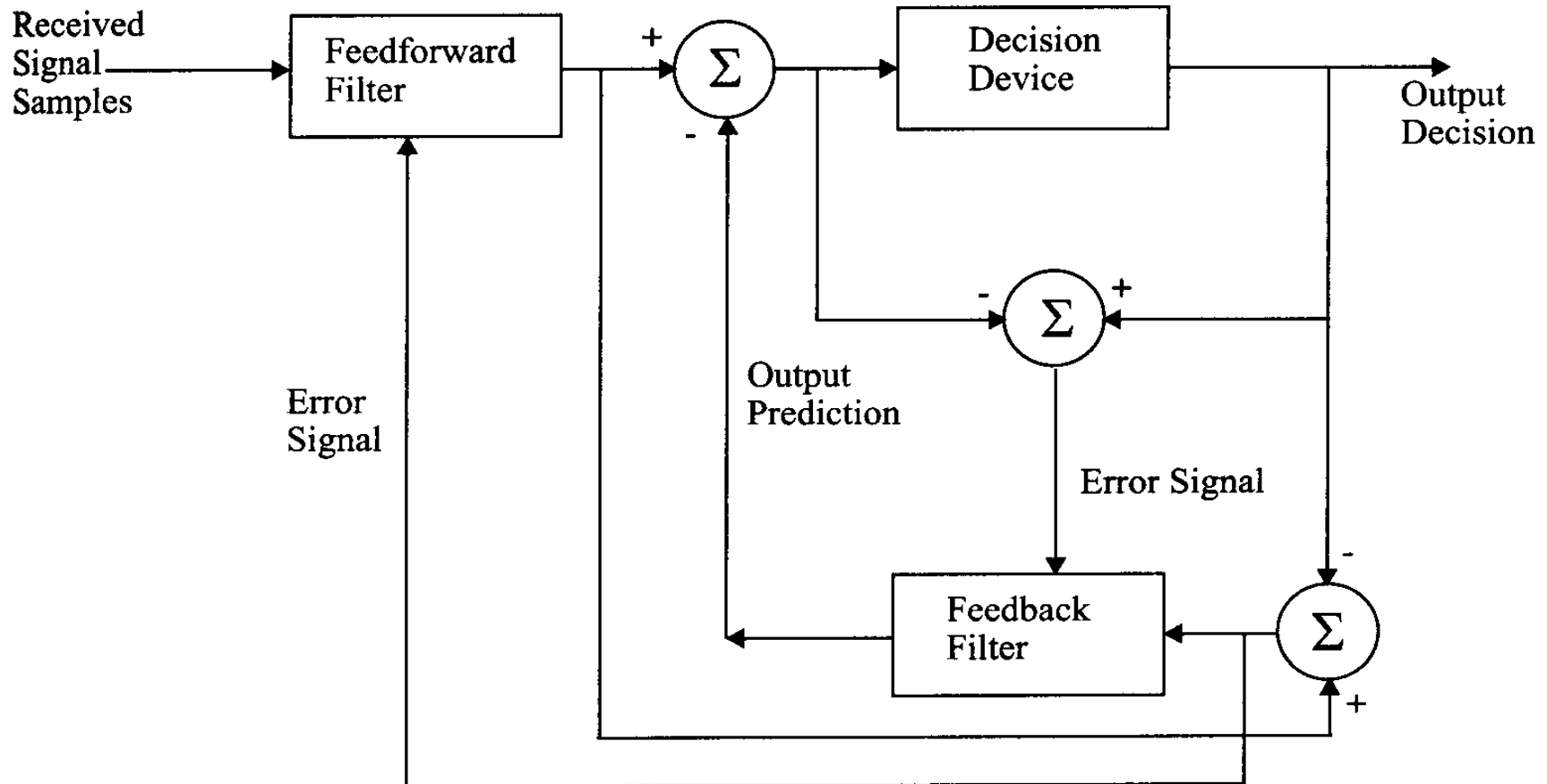


# DFE

- *Predictive DFE*
  - Consists of an FFF and an FBF, the latter is called a *noise predictor*
  - Predictive DFE performs as well as conventional DFE as the limit in the number of taps in FFF and the FBF approach infinity
  - The FBF in predictive DFE can also be realized as a lattice structure
- The RLS algorithm can be used to yield fast convergence



# Predictive decision feedback equalizer



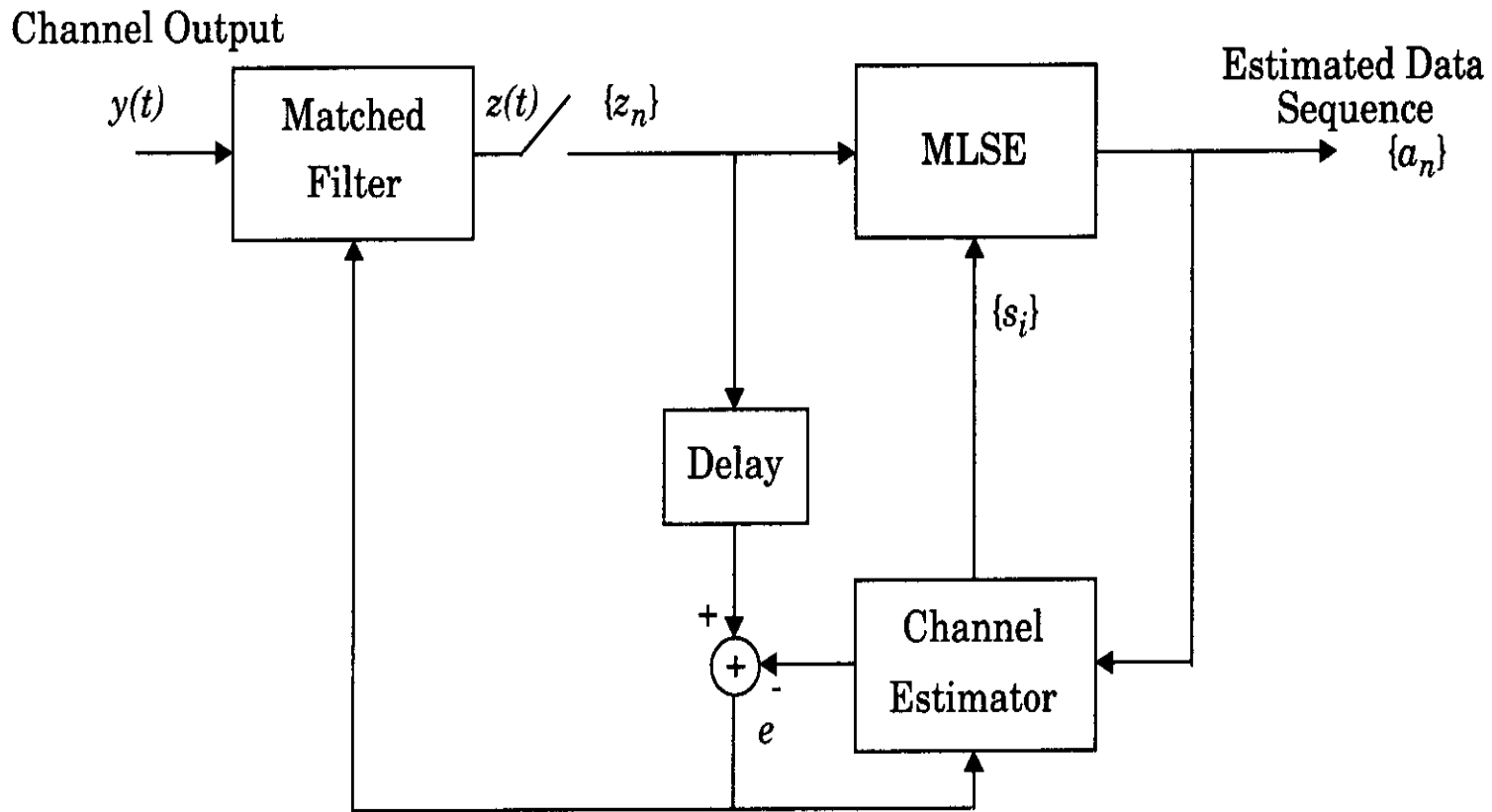


# Nonlinear Equalization--MLSE

- MLSE tests all possible data sequences
- Chooses the data sequence with the maximum probability as the output
- Usually has a large computational requirement
- The block diagram of MLSE receiver



# Nonlinear Equalization--MLSE



The structure of a maximum likelihood sequence equalizer(MLSE) with an adaptive matched filter





# Nonlinear Equalization--MLSE

- MLSE requires knowledge of the channel characteristics in order to compute the matrices for making decisions
- MLSE also requires knowledge of the statistical distribution of the noise corrupting the signal



# Assessment



➤ **The decision feedback equalizer has a linear traversal**

- a) **Feed forward section**
- b) Feedback section
- c) Both of the mentioned
- d) None of the mentioned



➤ **Choice of equalizer structure and its algorithm is not dependent on \_\_\_\_\_**

- a) Cost of computing platform
- b) Power budget
- c) Radio propagation characteristics
- d) **Statistical distribution of transmitted power**



# THANK YOU