

SNS COLLEGE OF TECHNOLOGY

Coimbatore-22 An Autonomous Institution



Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A++' Grade Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

19ECT212 – CONTROL SYSTEMS

II YEAR/ IV SEMESTER

UNIT I – CONTROL SYSTEM MODELING

TOPIC 8- SIGNAL FLOW GRAPH

19ECT212/Control Systems/Unit 1/Dr.S.Pradeep/AP/ECE







•REVIEW ABOUT PREVIOUS CLASS

• INTRODUCTION

•BASIC ELEMENTS OF SIGNAL FLOW GRAPH

•6 -EXAMPLE-SFG

•ACTIVITY

•CONVERSION OF BLOCK DIAGRAMS INTO SIGNAL FLOW GRAPHS

•EXAMPLE

•MASON'S GAIN FORMULA

•SUMMARY



INTRODUCTION



- Signal flow graph is a graphical representation of algebraic equations
- The block diagram reduction process takes more time for complicated system
- So, to overcome this drawback, use signal flow graphs (representation) is done where the calculation of transfer function is just by using a Mason's gain formula without doing any reduction process.

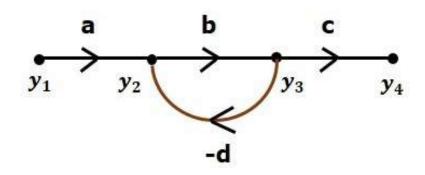


BASIC ELEMENTS OF SIGNAL FLOW GRAPH



Nodes and branches are the basic elements of signal flow graph. Node

Node is a point which represents either a variable or a signal. There are three types of nodes — input node, output node and mixed node.
Input Node – It is a node, which has only outgoing branches.
Output Node – It is a node, which has only incoming branches.
Mixed Node – It is a node, which has both incoming and outgoing branches.





BASIC ELEMENTS OF SIGNAL FLOW GRAPH...



- Forward path: It is a path from an input node to an output node that does not cross any node more than once.
- **Individual loop**: It is a closed path starting from one node and after passing through the graph arrives at the same node without crossing any node more than once.
- Non-touching loops: If a loop does not have a common node then they are said to be non-touching loops



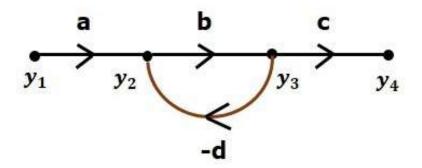
EXAMPLE



Let us consider the following signal flow graph to identify these nodes.

The nodes present in this signal flow graph are y₁, y₂, y₃ and y₄.
y₁ and y₄ are the input node and output node respectively.
y₂ and y₃ are mixed nodes.

Branch is a line segment which joins two nodes. It has both **gain** and **direction**. For example, there are four branches in the above signal flow graph. These branches have **gains** of **a**, **b**, **c** and -**d**.



EXAMPLE



Let us construct a signal flow graph by considering the following algebraic eqns. – $y_2 = a_{12}y_1 + a_{42}y_4$

 $y_3 = a_{23}y_2 + a_{53}y_5$

 $y_4 = a_{34} y_3$

 $y_5 = a_{45}y_4 + a_{35}y_3$

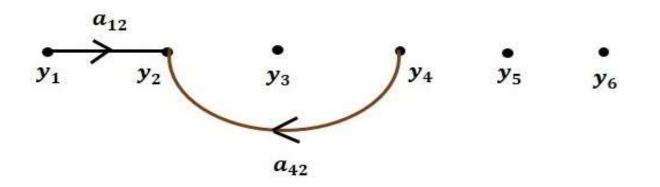
 $y_6 = a_{56}y_5$

There will be six **nodes** $(y_1, y_2, y_3, y_4, y_5 \text{ and } y_6)$ and eight **branches** in this signal flow graph. The gains of the branches are a_{12} , a_{23} , a_{34} , a_{45} , a_{56} , a_{42} , a_{53} and a_{35} .

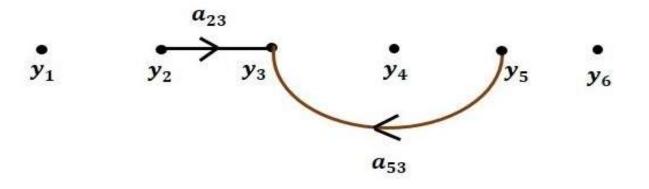
To get the overall signal flow graph, draw the signal flow graph for each equation, then combine all these signal flow graphs and then follow the steps given below –







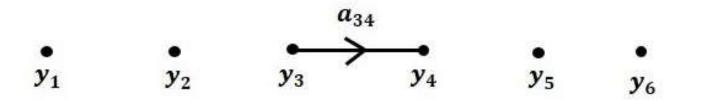
Step 2 – Signal flow graph for $y_3 = a_{23}y_2 + a_{53}y_5$ is shown in the following figure.



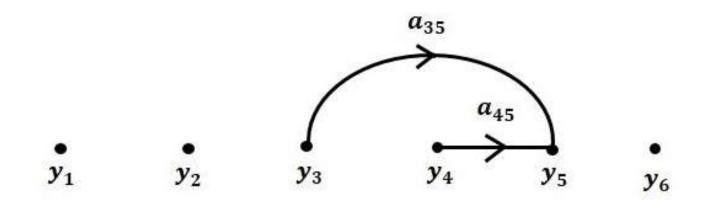




Step 3 – Signal flow graph for $y_4 = a_{34}y_3$ is shown in the following figure.



Step 4 – Signal flow graph for $y_5 = a_{45}y_4 + a_{35}y_3$ is shown in the following figure.



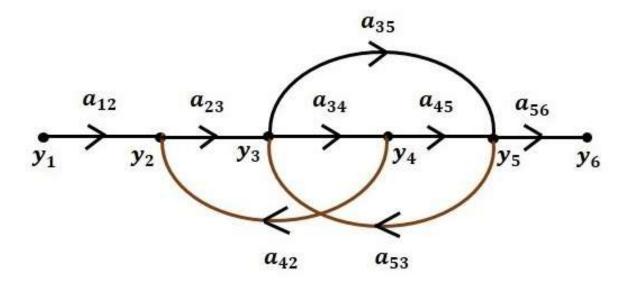




Step 5 – Signal flow graph for $y_6 = a_{56}y_5$ is shown in the following figure.



Step 6 - Signal flow graph of overall system is shown in the following figure.





ACTIVITY



ODD MAN OUT WITH REASON..?

108,120,132,144,156,164

Options :

- A 156
- B 164
- C 120
- D 108

Three of the following four are same in a certain way and hence form a group. Find out the one which does not belong to that group. **Options :**

- A Violet
- B Black
- C Green
- D Red



CONVERSION OF BLOCK DIAGRAMS INTO SIGNAL FLOW GRAPHS



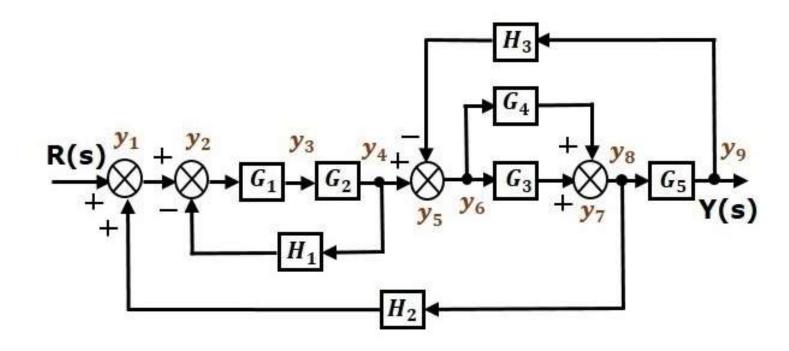
- Represent all the signals, variables, summing points and take-off points of block diagram as **nodes** in signal flow graph.
- Represent the blocks of block diagram as **branches** in signal flow graph.
- Represent the transfer functions inside the blocks of block diagram as **gains** of the branches in signal flow graph.
- Connect the nodes as per the block diagram.







Let us convert the following block diagram into its equivalent signal flow graph.





EXAMPLE ...



Represent the input signal R(s)R(s) and output signal C(s)C(s) of block diagram as input node R(s)R(s) and output node C(s)C(s) of signal flow graph.

Just for reference, the remaining nodes $(y_1 \text{ to } y_9)$ are labelled in the block diagram. There are nine nodes other than input and output nodes.

That is four nodes for four summing points, four nodes for four take-off points and one node for the variable between blocks G1G1 and G2G2. The following figure shows the equivalent signal flow graph.







 $\begin{array}{c} 1 & 1 & G_1 & G_2 & 1 \\ R(s) & y_1 & y_2 & y_3 \\ H_2 \end{array}$ $\begin{array}{c} I & 1 & G_1 & G_2 & 1 \\ R(s) & y_1 & y_2 & y_3 & y_4 & y_5 & y_6 & y_7 \\ H_1 & & & & \\ H_2 & & & \\ H_2 & & & & \\ H_2$

This is the advantage of signal flow graphs.

To simplify (reduce) the signal flow graphs for calculating the transfer function.



MASON'S GAIN FORMULA:-Mason's gain formula stalis that. Orecall gain, $T = \frac{1}{\Delta} \stackrel{>}{\underset{\scriptstyle}{k}} P_k \Delta_k$. where, T = T(3) = Transfer for of the system. Pk = Forward path gain of Kth forward path. Δ = 1 - (Sum of individual loop gains) + [Sum of gain products of all possible combination] of two non-touching loops - [Surs of gain products of all possible combinations of three non-touching loops] Δh = Δ for that part of the graph which is not buching kth forward path.





MASON'S GAIN FORMULA



Let us now discuss the Mason's Gain Formula. Suppose there are 'N' forward paths in a signal flow graph.

The gain between the input and the output nodes of a signal flow graph is nothing but the **transfer function** of the system. It can be calculated by using Mason's gain formula.



MASON'S GAIN FORMULA



- Represent all the signals, variables, summing points and take-off points of block diagram as **nodes** in signal flow graph.
- Represent the blocks of block diagram as **branches** in signal flow graph.
- Represent the transfer functions inside the blocks of block diagram as **gains** of the branches in signal flow graph.
- Connect the nodes as per the block diagram.



MASON'S GAIN FORMULA



 $T=rac{C(s)}{R(s)}=rac{\Sigma_{i=1}^NP_i\Delta_i}{\Delta}$

Where,

- C(s) is the output node
- R(s) is the input node

T is the transfer function or gain between R(s) and C(s)

P_i is the ith forward path gain

 $\Delta = 1 - (sum \ of \ all \ individual \ loop \ gains)$

+(sum of gain products of all possible two nontouching loops)

 $-(sum \ of \ gain \ products \ of \ all \ possible \ three \ nontouching \ loops)+\dots$

 Δ_i is obtained from Δ by removing the loops which are touching the *i*th forward path. Consider the following signal flow graph in order to understand the basic terminology involved here.







