

SNS COLLEGE OF TECHNOLOGY

Coimbatore – 35

An Autonomous Institution



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DEPARTMENT OF ELECTRONICS AND COMMUNICATION ENGINEERING

16EC401 / Wireless Communication

IV ECE/ VII SEMESTER

Unit IV - MULTIPATH MITIGATION TECHNIQUES

Topic 3: Zero forcing Algorithm, LMS Algorithms



Algorithms for Adaptive Equalization



Practical considerations for choice of an equalizer structure and its algorithm

The cost of the computing platform (affordable or not?)
Especially when used in user equipments
The power budget (power limited applications or else?)
In portable radio applications, battery drain at the subscriber unit is a paramount consideration
The radio propagation characteristics (fast fading & time

delay spread?)

•The speed of the mobile unit determines the channel fading rate and the Doppler spread, which is directly related to the coherence time of the channel

Three basic equalization methods *Linear equalization (LE):*



Performance is not very good when the frequency response of the frequency selective channel contains deep fades.

Zero-forcing algorithm aims to eliminate the intersymbol interference (ISI) at decision time instants (i.e. at the center of the bit/symbol interval).

Least-mean-square (LMS) algorithm

Recursive least-squares (RLS) algorithm offers faster convergence, but is computationally more complex than LMS (since matrix inversion is required).



zero-forcing algorithm



Criterion:

To force the samples of the combined channel and equalizer impulse response to zero at all but one of sample points in the tapped delay line filter. <u>Disadvantage:</u>

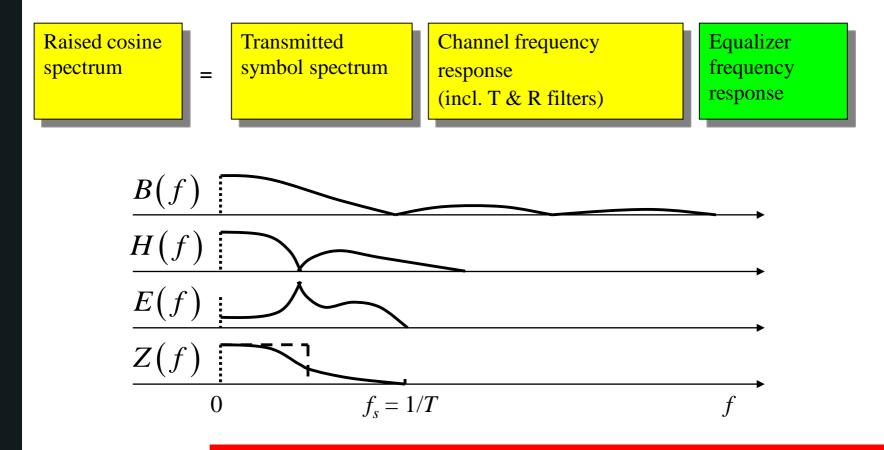
May excessively amplify noise at frequencies where the folded channel spectrum has high attenuation. <u>Suitability:</u> Wire line communications





Linear equalization, zero-forcing algorithm

Z(f) = B(f)H(f)E(f)Basic idea:

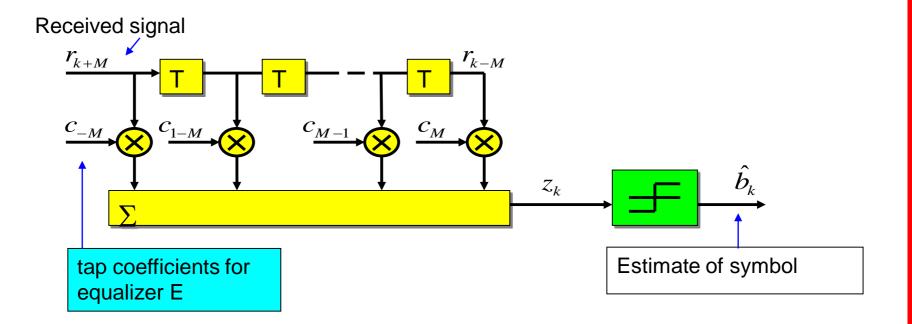




Zero-Forcing Equalization



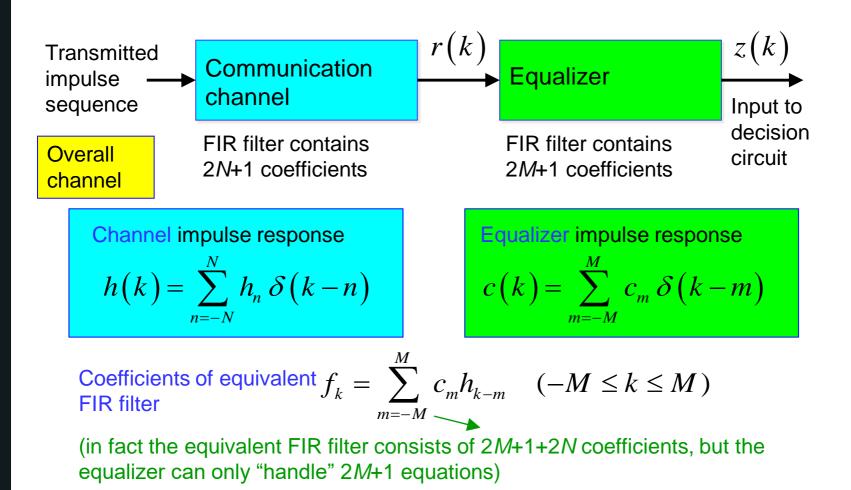
- Zero ISI at the receiver output
- B(f)H(f)E(f)=Z(f)
- Z(f): Nyquist spectrum e.g. raised cosine





Zero-forcing equalizer







Zero-forcing equalizer



Overall filter response to be non-zero at decision time k = 0 and zero at all other sampling times $k \neq 0$:

$$f_{k} = \sum_{m=-M}^{M} c_{m} h_{k-m} = \begin{cases} 1, \ k = 0\\ 0, \ k \neq 0 \end{cases}$$

This leads to a set of
$$2M+1$$
 equations:

$$\begin{split} h_0 c_{-M} + h_{-1} c_{-M+1} + \ldots + h_{-2M} c_M &= 0 \quad (k = -M) \\ h_1 c_{-M} + h_0 c_{-M+1} + \ldots + h_{-2M+1} c_M &= 0 \\ &\vdots \\ h_M c_{-M} + h_{M-1} c_{-M+1} + \ldots + h_{-M} c_M &= 1 \quad (k = 0) \\ &\vdots \\ h_{2M-1} c_{-M} + h_{2M-2} c_{-M+1} + \ldots + h_{-1} c_M &= 0 \\ h_{2M} c_{-M} + h_{2M-1} c_{-M+1} + \ldots + h_0 c_M &= 0 \quad (k = M) \end{split}$$



Activity



≻Imagine folding a paper in half once

≻Then take the result and fold it in half again; and so on

≻How many times can you do that?



Least-mean-square (LMS) algorithm Criterion:

- \succ To minimize the mean square error (MSE) between the desired $\xi = E[e_{k}^{\circ} \cdot e_{k}]$
- equalizer output and the actual equalizer output.
- \blacktriangleright Minimize must be solved iteratively
- > Simplest algorithm, requires only 2N + I operations per iteration.
- \succ The LMS equalizer maximizes the signal to distortion ratio
- at its output within the constraints of the equalizer filter length.
- \triangleright A step size α is used to control the convergence rate and the stability





Eeast-mean-square (LMS) algorithm

<u>Disadvantage:</u> Low convergence rate because of the only one parameter α .

Especially when the eigen values of the input covariance matrix R_{NN} have a very large spread, i.e. $\lambda_{max}/\lambda_{max} \gg 1$

To prevent the adaptation from becoming unstable, the value of a is chosen from $0 < \alpha < 2 / \sum_{i=1}^{N} \lambda_{i}$ Where λ_{i} is the ith eigenvalue of the covariance matrix R_{NN} . The step size a can be controlled by the total input power in

order to avoid instability in the equalizer

$$\sum \lambda_i = \boldsymbol{y}_N^T(n) \boldsymbol{y}_N(n)$$



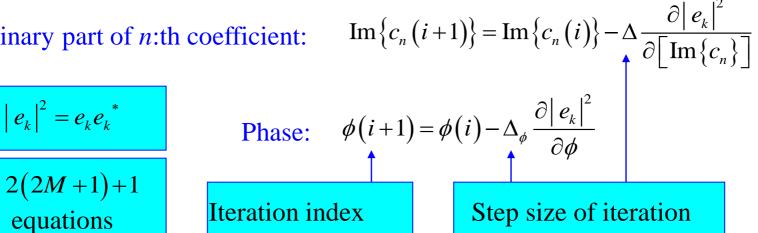
Least-mean-square (LMS) algorithm

For convergence towards minimum mean square error (MMSE)

Real part of *n*:th coefficient:

$$\operatorname{Re}\left\{c_{n}\left(i+1\right)\right\} = \operatorname{Re}\left\{c_{n}\left(i\right)\right\} - \Delta \frac{\partial \left|e_{k}\right|^{2}}{\partial \left[\operatorname{Re}\left\{c_{n}\right\}\right]}$$

Imaginary part of *n*:th coefficient:







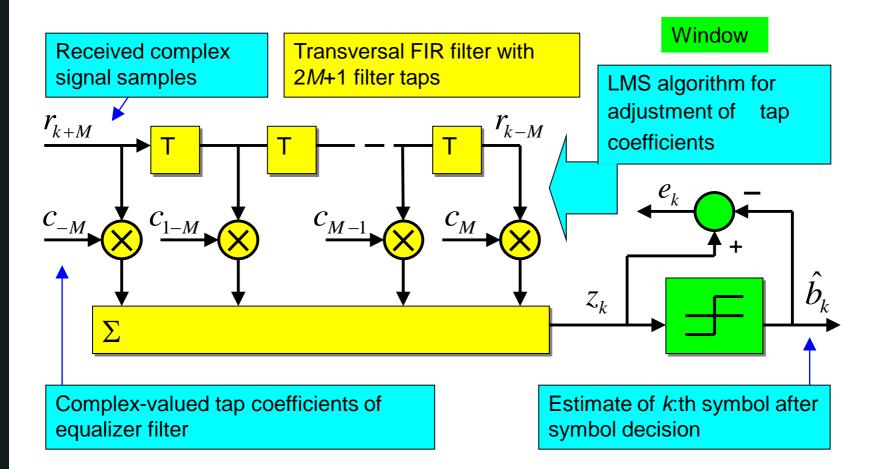
After some calculation, the recursion equations are obtained in the form

$$\operatorname{Re}\left\{c_{n}\left(i+1\right)\right\} = \operatorname{Re}\left\{c_{n}\left(i\right)\right\} - 2\Delta\operatorname{Re}\left\{\left(e^{j\phi}\sum_{m=-M}^{M}c_{m}r_{k-m}-\hat{b}_{k}\right)r_{k-n}^{*}e^{-j\phi}\right\}$$
$$\operatorname{Im}\left\{c_{n}\left(i+1\right)\right\} = \operatorname{Im}\left\{c_{n}\left(i\right)\right\} - 2\Delta\operatorname{Im}\left\{\left(e^{j\phi}\sum_{m=-M}^{M}c_{m}r_{k-m}-\hat{b}_{k}\right)r_{k-n}^{*}e^{-j\phi}\right\}$$
$$\phi(i+1) = \phi(i) - 2\Delta_{\phi}\operatorname{Im}\left\{\hat{b}_{k}^{*}e^{j\phi}\sum_{m=-M}^{M}c_{m}r_{k-m}\right\}$$



Conventional linear equalizer of LMS type

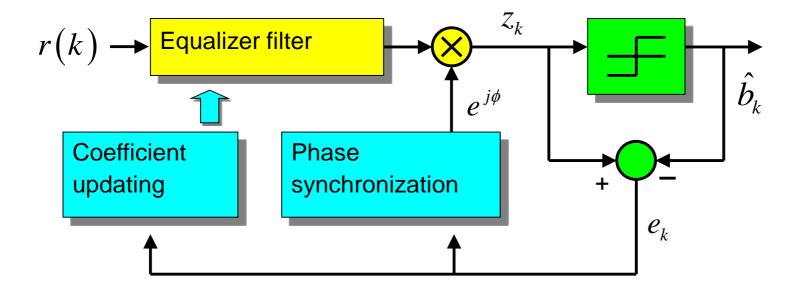






Joint optimization of coefficients and phase





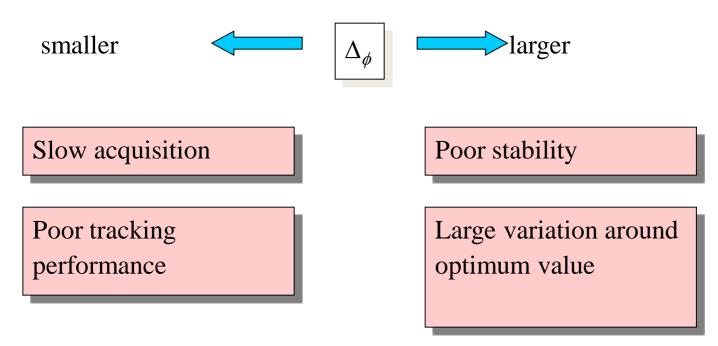
Minimize:

$$J = E \left| e_k \right|^2 \qquad e_k = z_k - \hat{b}_k = \left(\sum_{m=-M}^M c_m r_{k-m} \right) \exp(j\phi) - \hat{b}_k$$



Effect of iteration step size





Convergence condition

 $0 < \Delta < 2/\lambda_{max}$

 λ : eigenvalue of autocorrelation matrix of **r**



Assessment



- > The decision feedback equalizer has a linear traversal filter which is
 - a) Feed forward section
 - b) Feedback section
 - c) Both of the mentioned
 - d) None of the mentioned



- Choice of equalizer structure and its algorithm is not dependent on ____
 - a) Cost of computing platform
 - b) Power budget
 - c) Radio propagation characteristics
 - d) Statistical distribution of transmitted power





THANK YOU