

## Unit - IV

### Magnetic forces and Materials

To study the force a magnetic field exerts on charged particles, current elements and loops.

Its important to problems on ~~chang~~ electrical devices such as ammeters, voltmeters, galvanometers, cyclotrons, plasmas, metors and magnetohydrodynamic generators.

#### Lorentz Force equation :

#### \* Force on a charged particle:

Electric force  $F_e$  on a stationary or moving electric charge  $Q$  in an electric field is given by Coulomb's experimental law

$$\vec{F}_e = Q\vec{E}$$

$F$  &  $E$  → same direct +ve charge  
opposite " -ve charge

A magnetic field exert force only on a moving charge.

Magnetic force experienced by a charge  $Q$  moving with a velocity  $v$  in a magnetic field  $B$  is,

$$\vec{F}_m = Q\vec{v} \times \vec{B}$$

$F_m$  is perpendicular to both  $v$  &  $B$ .

For a moving charge  $Q$  in the presence of both electric and magnetic fields, the total force on the charge is given by

$$F = F_e + F_m$$

$$F = q(E + v \times B)$$

This is known as Lorentz Force equation.

\* Force on a differential current element

Consider a current element placed in a magnetic field,

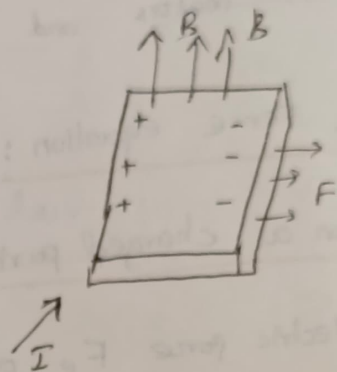
Force on a small differential element 'dl'

$$dF = dq(v \times B)$$

$$= dq \left( \frac{dl}{dt} \times B \right)$$

$$= \frac{dq}{dt} (dl \times B)$$

$$\vec{dF} = I (d\vec{l} \times \vec{B})$$



If  $I$  is along negative  $x$  direction and  $B$  is along  $+ve$   $z$  direction. So  $F$  will be along  $+ve$   $y$  direction.

$$\vec{F} = I (L(-\hat{x}) \times B(\hat{z})) \quad \hat{x} \hat{y} \hat{z}$$

$$= I L B \sin\theta \hat{y}$$

$$\vec{F} = B I L \sin\theta \hat{y} \quad \text{or} \quad F = I(L \times B)$$

The magnitude of force

$$F = B I L \sin\theta$$

