

Flux

$$\Psi = \int \vec{D} \cdot d\vec{s}$$

$$\Psi = \int \vec{B} \cdot d\vec{s}$$

$$\Psi = Q = CV$$

$$\Psi = LI$$

$$I = C \frac{dV}{dt}$$

$$V = L \frac{dI}{dt}$$

Energy density

$$W_E = \frac{1}{2} D \cdot E$$

$$W_m = \frac{1}{2} B \cdot H$$

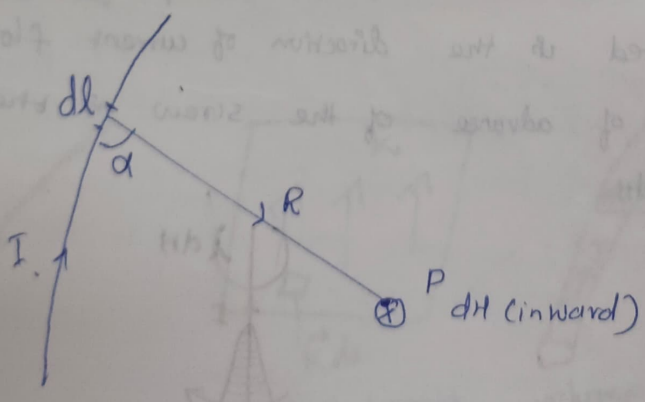
Poisson's equation

$$\nabla^2 V = -\frac{\rho_v}{\epsilon}$$

$$\nabla^2 A = -\mu J$$

Biot - Savart's law :-

Biot - Savart's law states that differential magnetic field intensity dH produced at a point P , by the differential current element $I dl$ is proportional to the product $I dl$ and the sine of the angle α between the element and the line joining P to the element and is inversely proportional to the square of the distance R .



Magnetic field at P due to current element $I dl$.

$$dH \propto \frac{Idl \sin \alpha}{R^2}$$

$$\text{or } dH = \frac{k Idl \sin \alpha}{R^2}$$

Constant of proportionality:

$$k = \frac{1}{4\pi}$$

$$\therefore dH = \frac{Idl \sin \alpha}{4\pi R^2}$$

In vector form

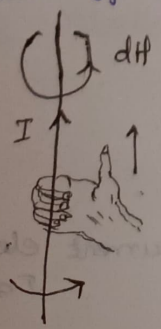
$$dH = \frac{Id\vec{l} \times \vec{R}}{4\pi R^3}$$

$$dH = \frac{I d\vec{l} \times \vec{R}}{4\pi R^3}$$

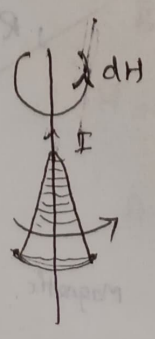
Direction of $d\vec{H}$

1) Right-hand rule: Right-hand thumb pointing in the direction of current and the right-hand fingers encircling the wire in the direction of dH .

2) Right-handed screw rule: The screw placed along the wire and pointed in the direction of current flow, the direction of advance of the screw is the direction of dH .



Right-hand rule



Right handed screw rule

○ H or I is out

⊗ H or I is in

Conventional representation of H
out of the page

• into the page

Different current distributions

line current,

surface current

volume current.

$k \rightarrow$ surface current density,
(Amperes per meter)

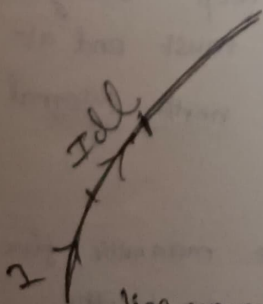
$J \rightarrow$ volume current density
(Amperes per meter squared)

Biot Savart's law

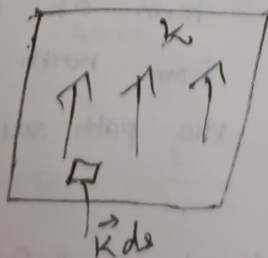
$$\vec{H} = \int_L \frac{I d\vec{l} \times \hat{a}_R}{4\pi R^2} \quad (\text{line current})$$

$$\vec{H} = \int_S \frac{\vec{k} ds \times \hat{a}_R}{4\pi R^2} \quad (\text{surface current})$$

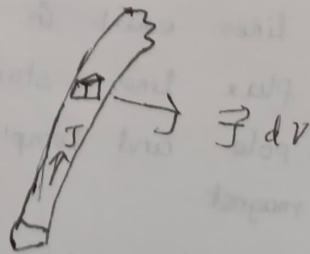
$$\vec{H} = \int_V \frac{\vec{J} dv \times \hat{a}_R}{4\pi R^2} \quad (\text{volume current})$$



line current



Surface current



volume current

\rightarrow Current distributions