

Introduction:-

- The controller (an analogue/digital circuit, and software), is trying to keep the controlled variable such as temperature, liquid level, motor velocity, robot joint angle, at a certain value called the set point (SP).
- Controllers improve steady state accuracy by decreasing the steady state errors.
- Maximum overshoot of the system can be controlled using these controllers

Some definitions :-

➤ **Peak time :-**

- The peak time is the time required for the response to reach the first peak of the overshoot.

➤ **Overshoot :-**

- Overshoot is when a signal or function exceeds its target.

➤ **Steady state error:-**

- The difference between the desired final output and the actual one" when the system reaches a steady state

Controllers:-

- A controller is one which compares controlled values with the desired values and has a function to correct the deviation produced.
- There are three basic types of controllers :
 - Proportional controller { P controller }
 - Derivative controller { D controller }
 - Integral controller { I controller }

P controller :-

- P controller stands for Proportional Control
- With proportional control, the actuator *applies a corrective force that is proportional to the amount of error:*

$$Output_p = K_p \times E$$

- $Output_p$ = system output due to proportional control
- K_p = proportional constant for the system called gain
- E = error, the difference between where the controlled variable should be and where it is. $E = SP - PV$.

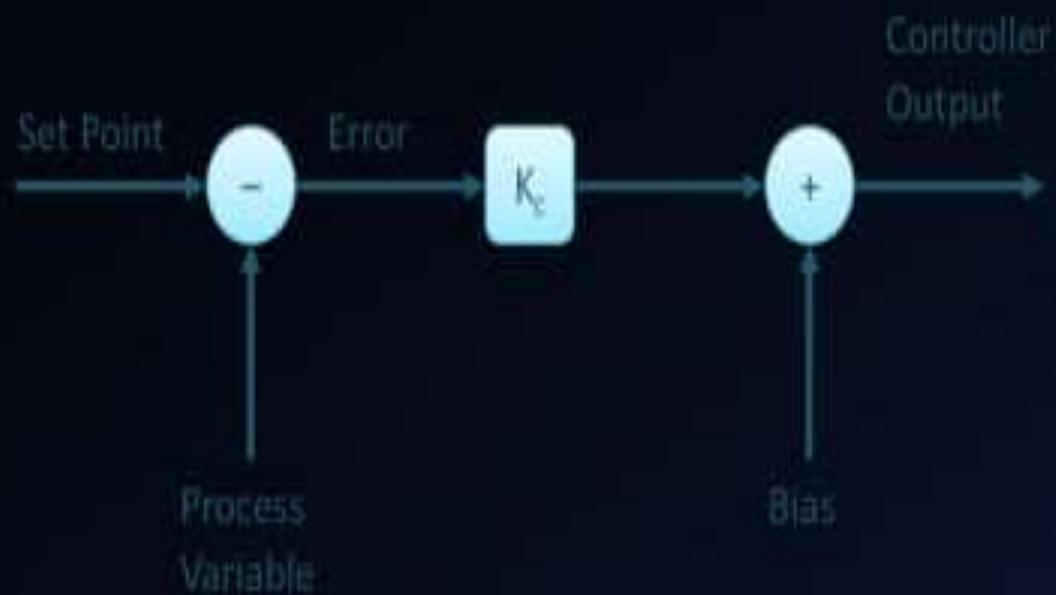
P controller :-

- In a proportional controller the output (also called the actuating signal) is directly proportional to the error signal.

$$A(t) = K_p \times e(t)$$

- Where, K_p is proportional constant also known as controller gain.
- K_p should be kept greater than unity. If the value of K_p is greater than unity, then it will amplify the error signal and thus the amplified error signal can be detected easily

P controller :-



P controller

PI controller :-

- PI controller stands for proportional integral controller.
- P-I controller is mainly used to eliminate the steady state error resulting from P controller.
- This controller is mostly used in areas where speed of the system is not an issue.
- it is a combination of proportional and an integral controller the output (also called the actuating signal) is equal to the summation of proportional and integral of the error signal.

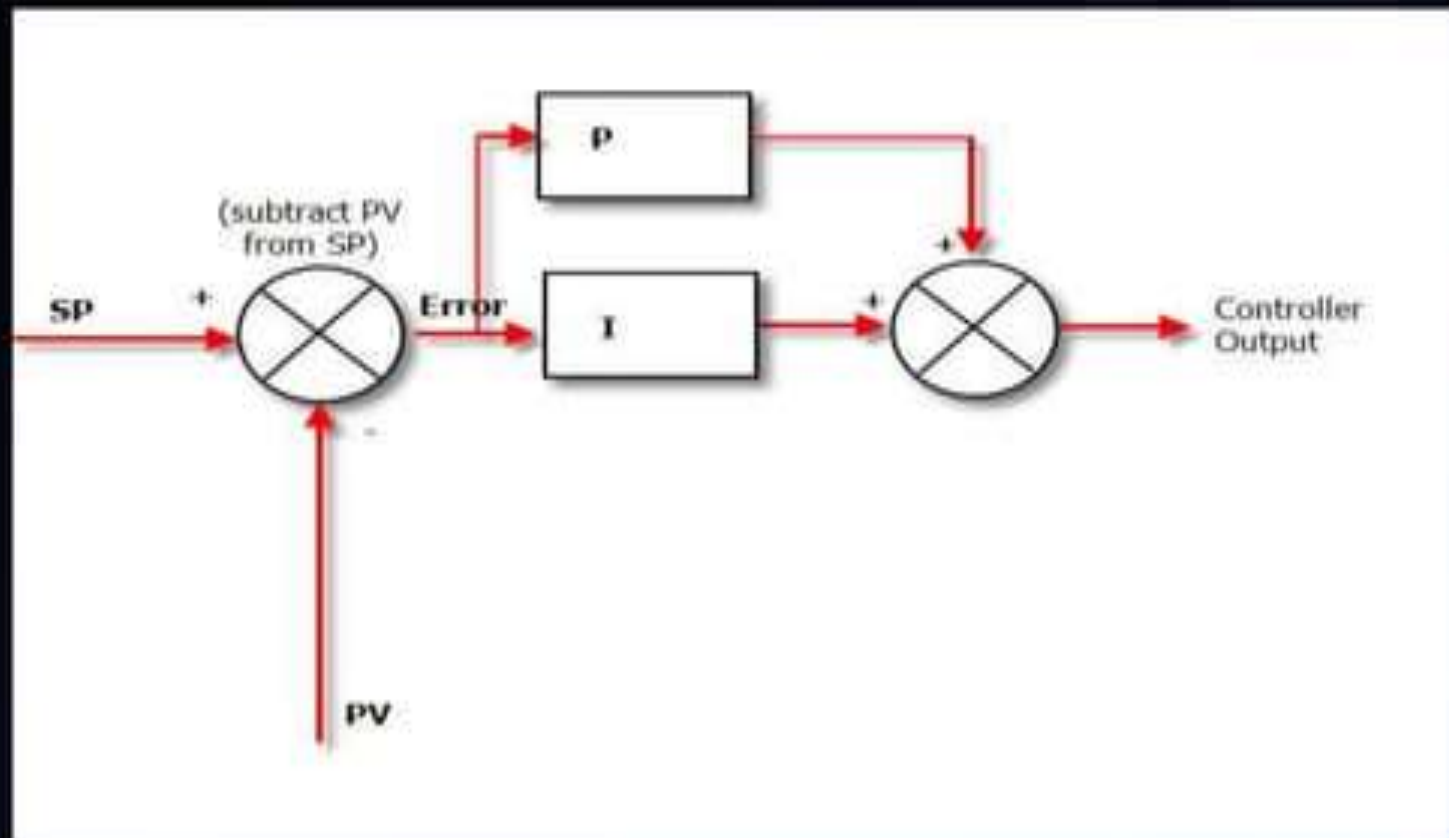
PI controller :-

- A proportional and integral controller output is directly proportional to the summation of proportional of error and integration of the error signal.

$$A(t) = K_i \int_0^t e(t) dt + K_p e(t)$$

- Where, K_i and k_p proportional constant and integral constant respectively.

PI controller :-



PID controller :-

- PID stands for proportional integrated derivative.
- A proportional–integral–derivative controller (PID controller) is a generic control loop feedback mechanism (controller) widely used in industrial control systems.
- A PID controller attempts to correct the error between a measured process variable and a desired setpoint by calculating and then outputting a corrective action that can adjust the process accordingly.

PID controller :-

- The foundation of the system is proportional control. Adding integral control provides a means to eliminate steady-state error, but increases overshoot.
- Derivative control increases stability by reducing the tendency to overshoot.
- It consists of three controllers :-
 - ❖ Integral control
 - ❖ Proportional control
 - ❖ Derivative control

PID controller :-

$$Output_{PID} = K_P \times E + K_I \times \sum (E \times \Delta t) + K_D \times \left(\frac{\Delta E}{\Delta t} \right)$$

$Output_{PID}$ = output from PID controller

K_P = proportional control gain

K_I = integral control gain

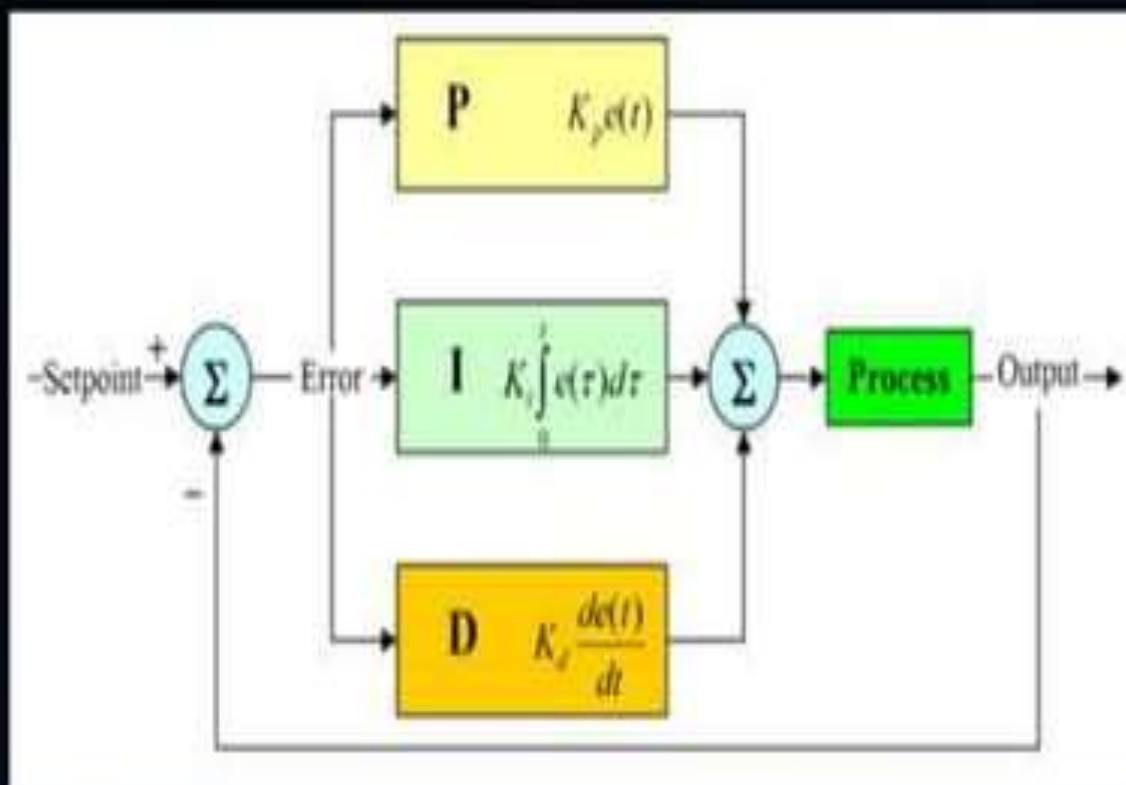
K_D = derivative control gain

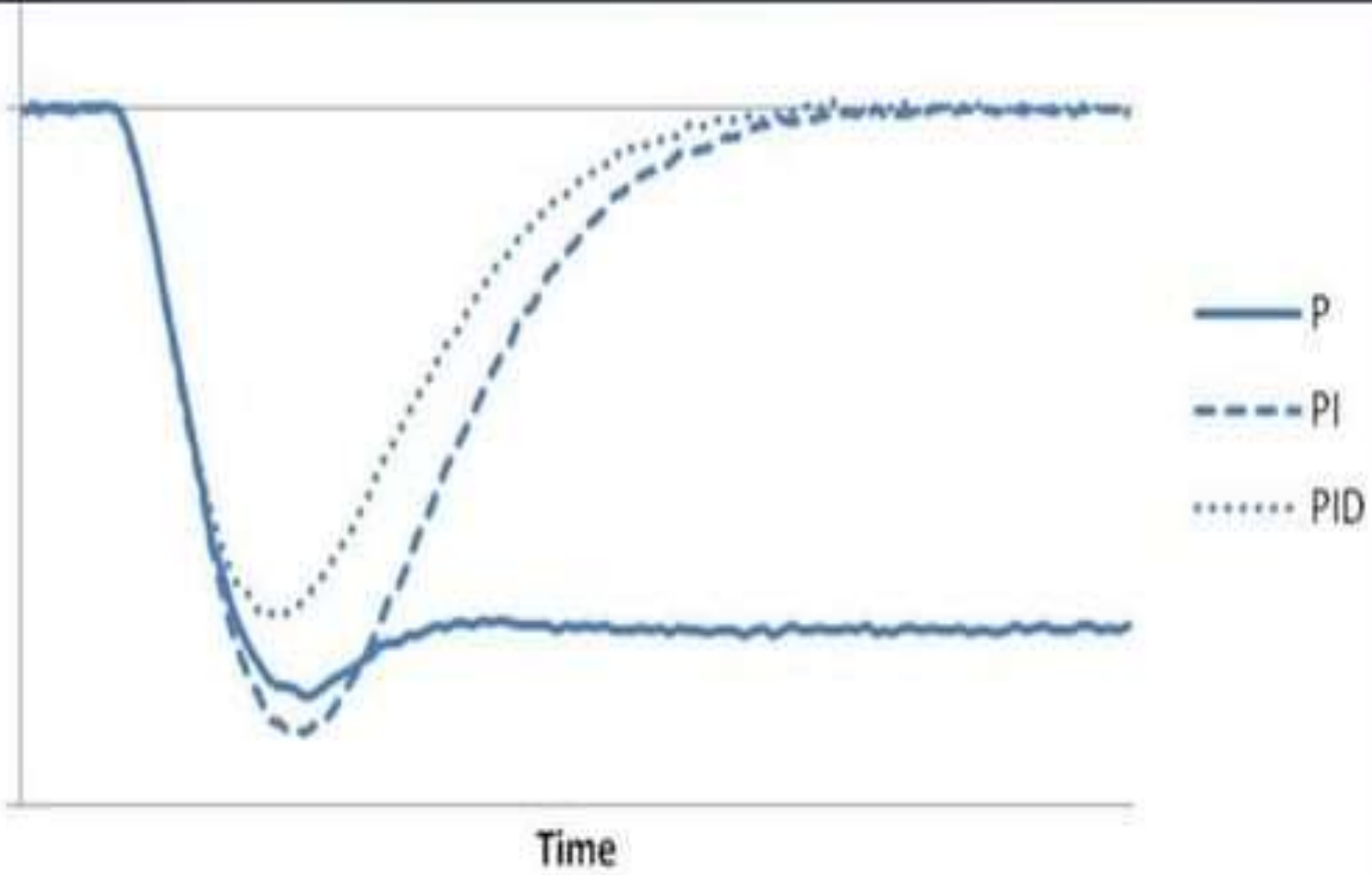
E = error (deviation from set point)

$\sum(E \times \Delta t)$ = sum of all past errors (area under the error/time curve)

$\Delta E / \Delta t$ = rate of change of error (slope of the error curve)

PID Controller :-







Thank you