



SNS COLLEGE OF TECHNOLOGY

An Autonomous Institution

Coimbatore-35



Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A++' Grade
Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

19ECB212 – DIGITAL SIGNAL PROCESSING

II YEAR/ IV SEMESTER

UNIT 1 – DISCRETE FOURIER TRANSFORM

TOPIC – Overlap Add Method



EMPATHY



Difficult to filter long data sequences

Real time filtering

Filtering of long data sequence is Slow



SECTIONED CONVOLUTION



- The response of an LTI system for any arbitrary input is given by linear convolution of the input and the impulse response of the system
- The input sequence or impulse response sequence is very much larger than the other, then it is very difficult to compute the linear convolution for the following reasons:
 - The entire sequence should be available before convolution can be carried out. This makes long delay in getting the output
 - Large amounts of memory is required to store the sequences



SECTIONED CONVOLUTION



- In this technique the larger sequence is sectioned (or splitted) into the size of smaller sequence
- Then the linear convolution of each section of longer sequence and the smaller sequence is performed
- The output sequences obtained from the convolutions of all the sections are combined to get the overall output sequence



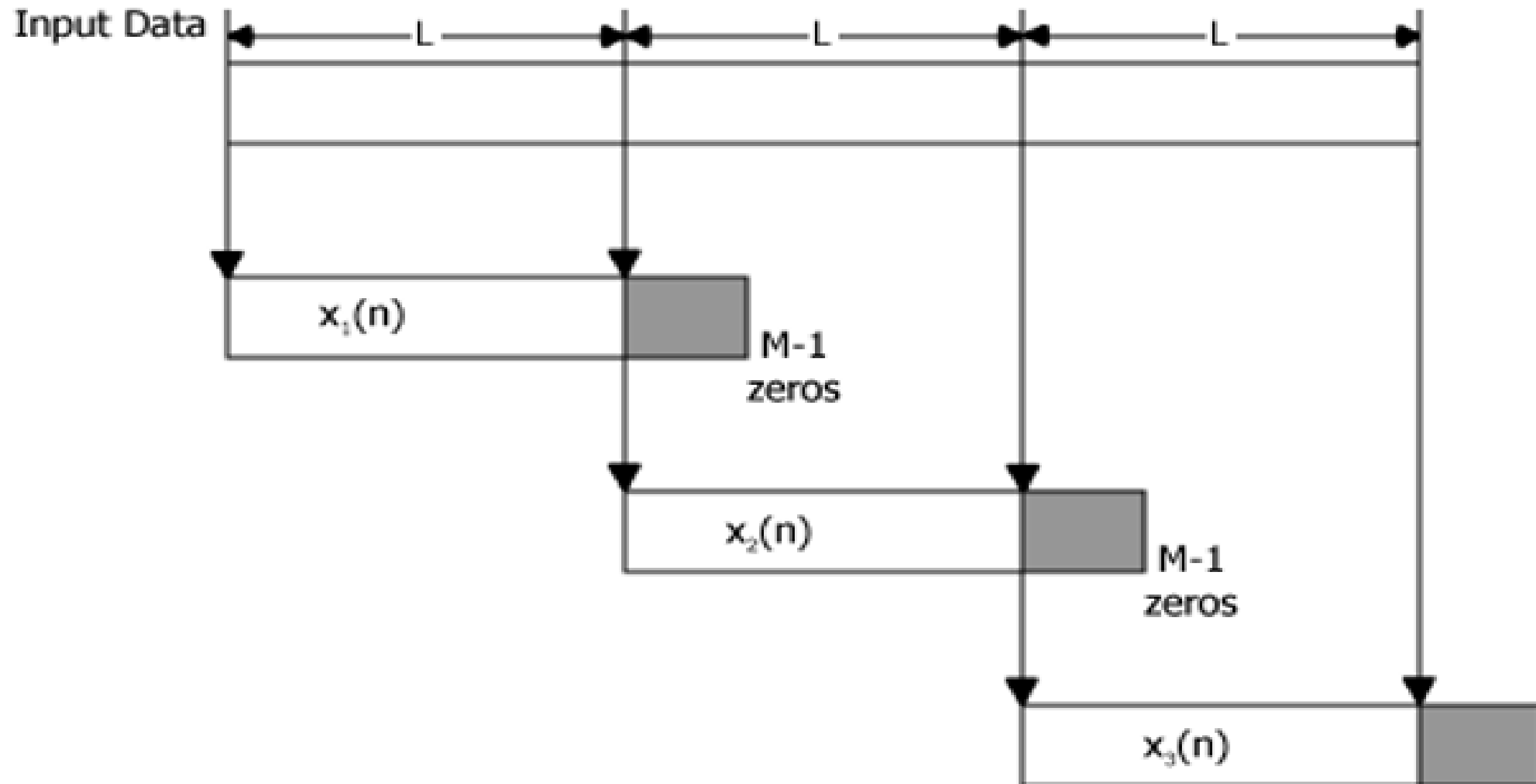
SECTIONED CONVOLUTION



- There are two methods of sectioned convolutions. They are
- **Overlap add method**
- **Overlap save method**



OVERLAP ADD METHOD

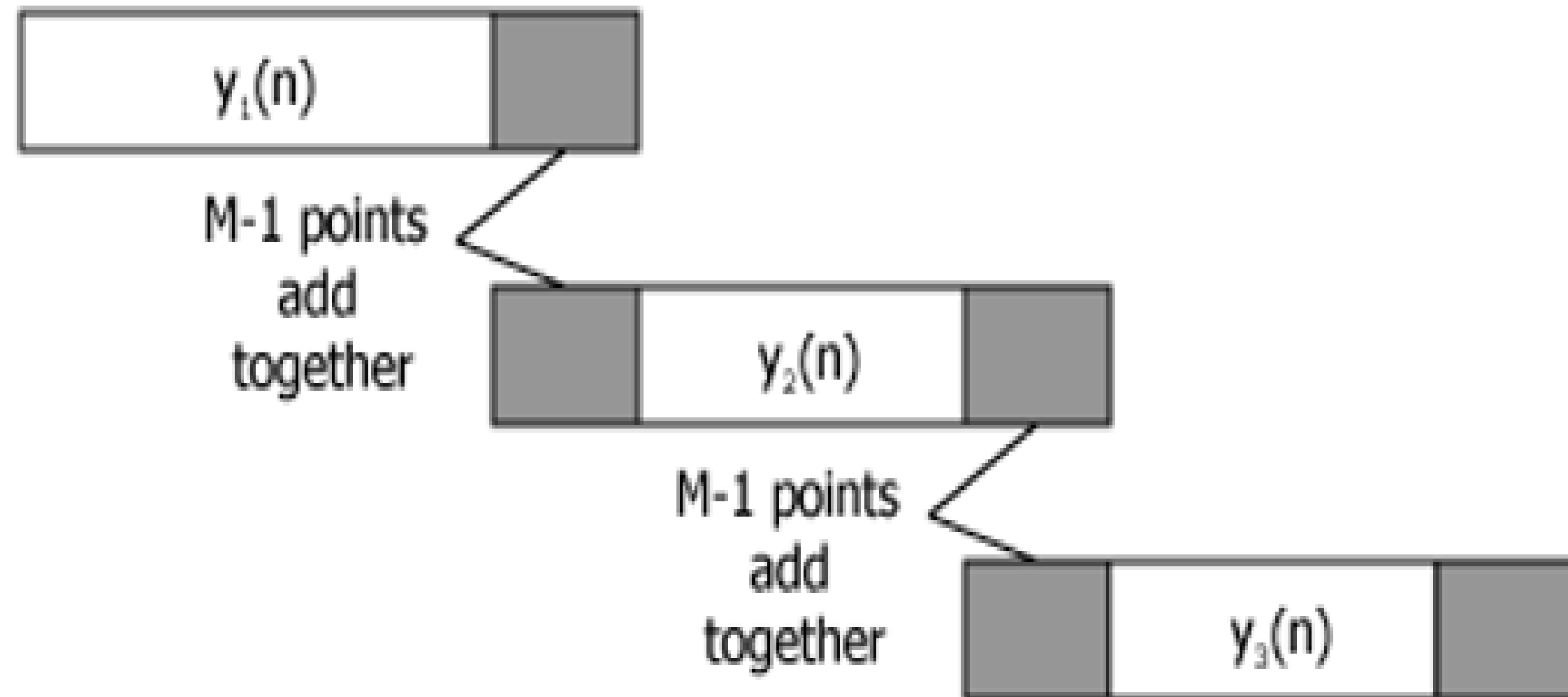




OVERLAP ADD METHOD



Output Data

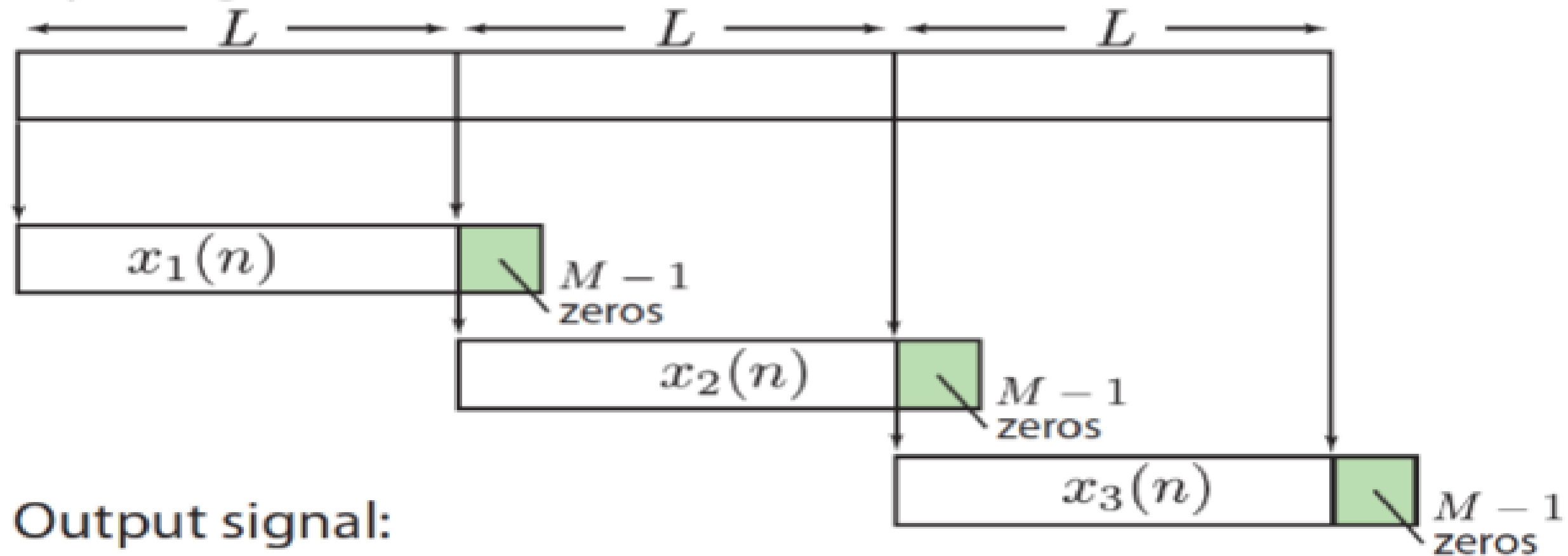




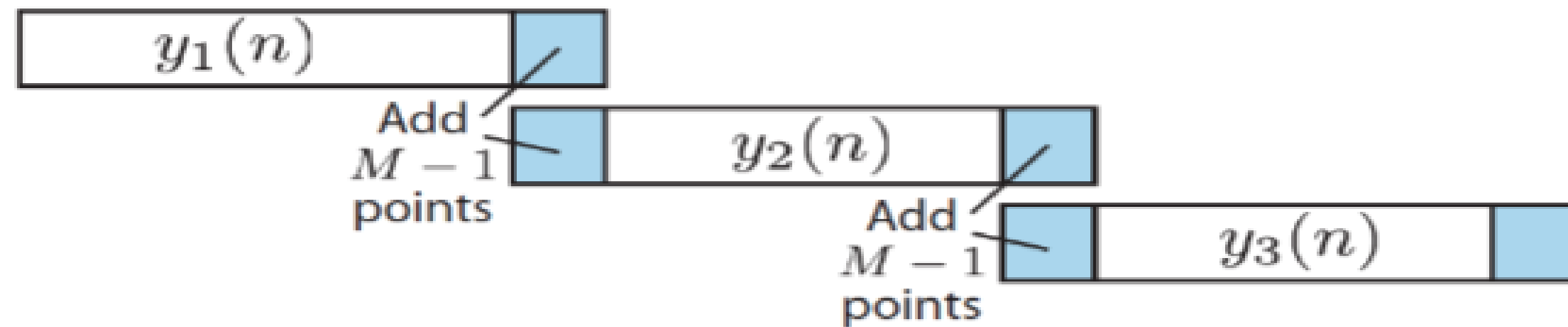
OVERLAP ADD METHOD



Input signal:



Output signal:





OVERLAP ADD METHOD



- Step 1: Divide the longer sequence into small sequences

$x(n)$ – Long sequence and $h(n)$ – Small Sequence

Then divide $x(n)$ into $x_1(n)$, $x_2(n)$, $x_3(n)$

- Length of $x_1(n)$ (or) Length of $x_2(n)$ (or) Length of $x_3(n)$ = Length of $h(n)$
- Step 2: Find $y_1(n)$ then $y_1(n) = x_1(n) * h(n)$
- Step 3: Find $y_2(n)$, $y_3(n)$
- Step 4: Combine all the outputs $y_1(n)$, $y_2(n)$, $y_3(n)$



OVERLAP ADD METHOD



- Find the linear convolution $x(n) = \{1,2,3,4,4,3,2,1\}$ and $h(n) = \{-1,1\}$ using Overlap Add Method:

- **Step 1:** Divide longer sequence into small subsequences

- $x(n)$ = Longer sequence and $h(n)$ = Small sequence

$x(n)$ is divided as below

- $x_1(n) = \{1,2\}$, $x_2(n) = \{3,4\}$, $x_3(n) = \{4,3\}$, $x_4(n) = \{2,1\}$
- Length of $x_1(n)$ or $x_2(n)$ or $x_3(n)$ or $x_4(n)$ = Length of $h(n)$

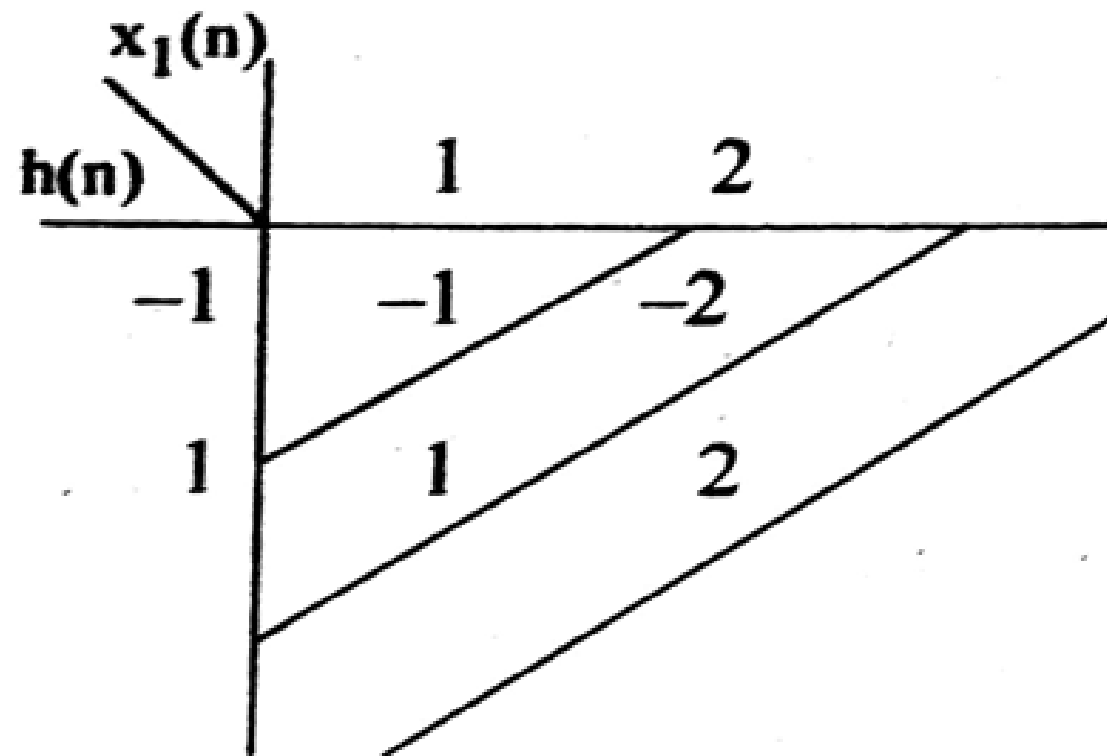


OVERLAP ADD METHOD



Step 2 : Find $y_1(n)$

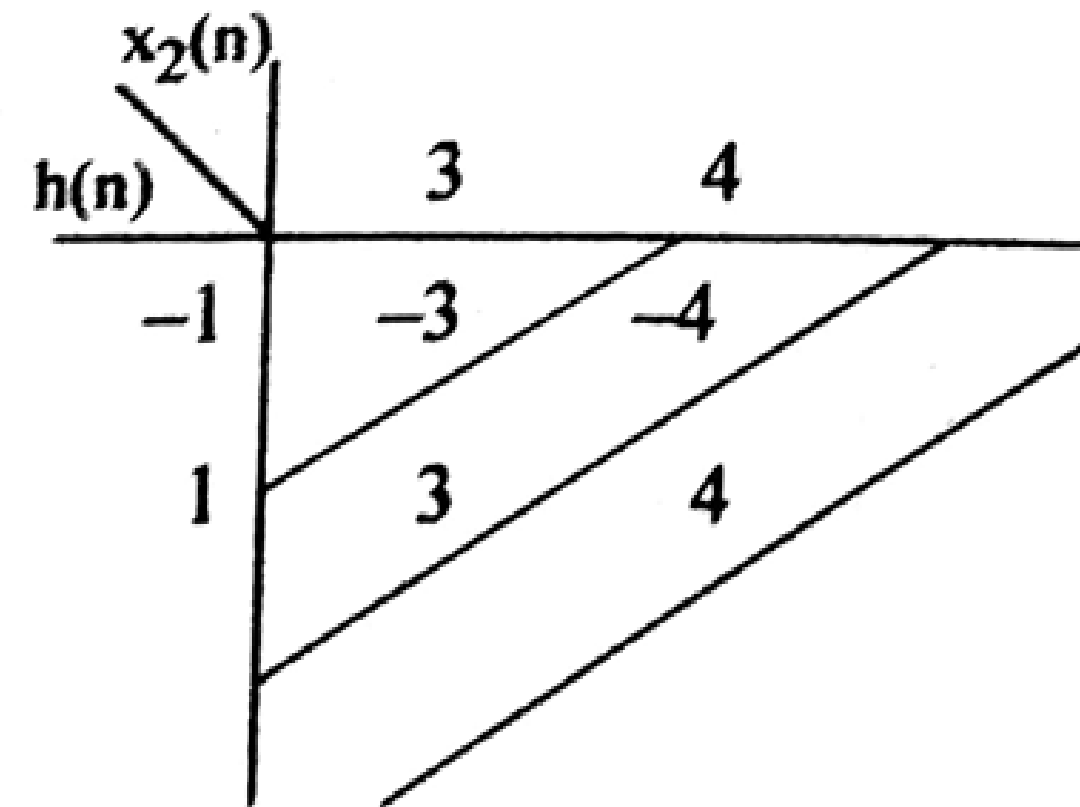
$$y_1(n) = x_1(n) * h(n)$$



$$y_1(n) = \{-1, -1, 2\}$$

Step 3 :

Find $y_2(n) = x_2(n) * h(n)$



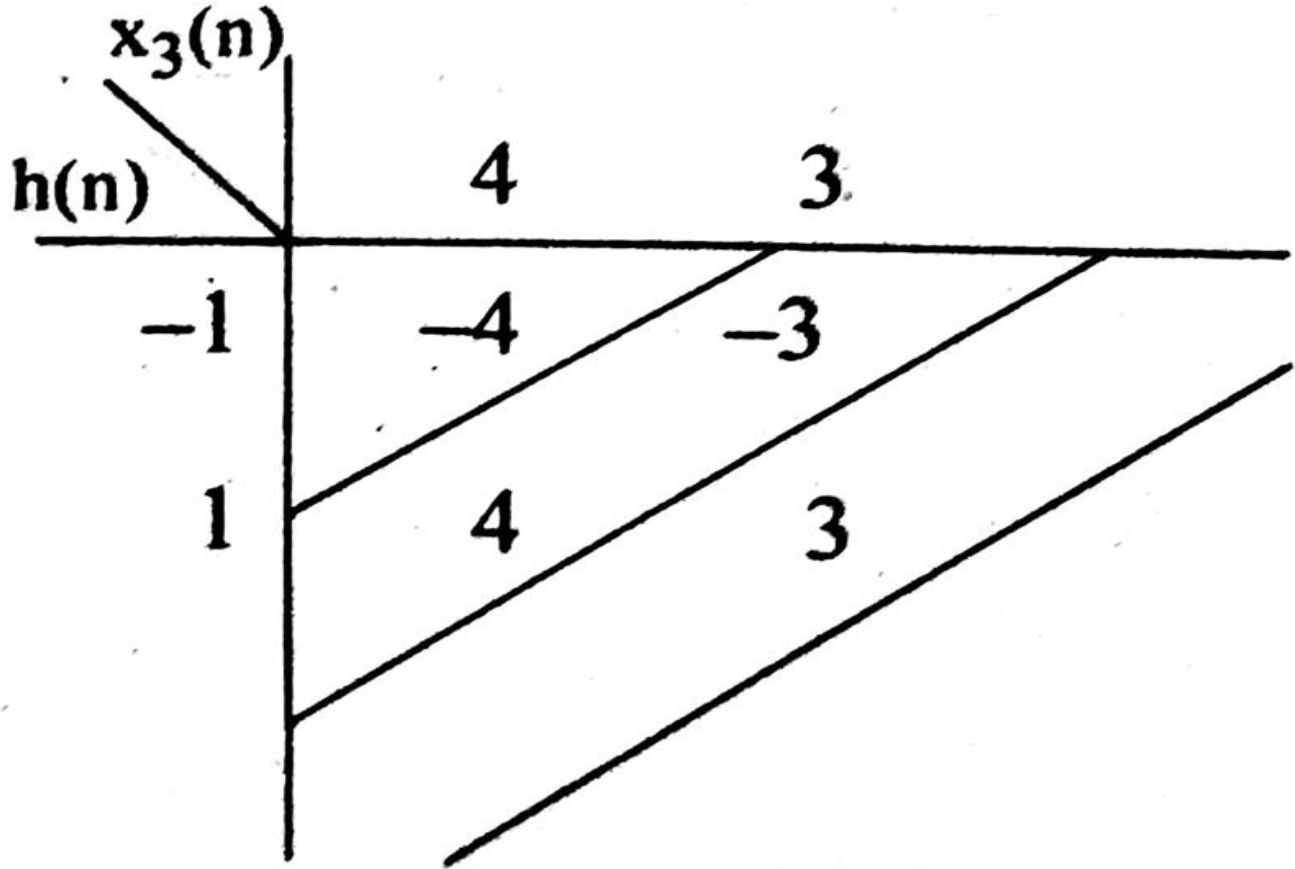
$$y_2(n) = \{-3, -1, 4\}$$



OVERLAP ADD METHOD

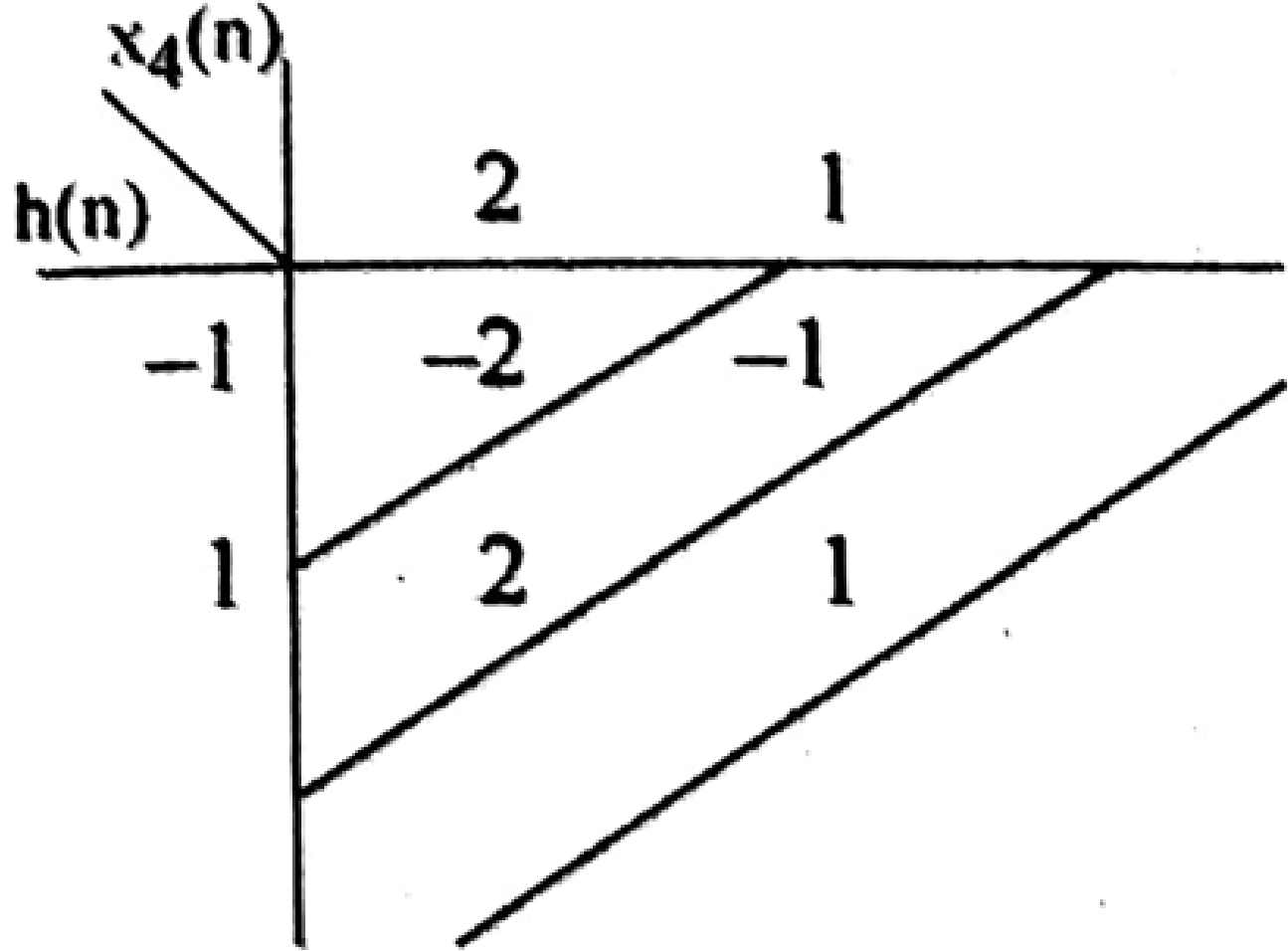


$$y_3(n) = x_3(n) * h(n)$$



$$y_3(n) = \{-4, 1, 3\}$$

$$y_4(n) = x_4(n) * h(n)$$



$$y_4(n) = \{-2, 1, 1\}$$



OVERLAP ADD METHOD



Step 4 : Combine all the outputs :

n	0	1	2	3	4	5	6	7	8
$y_1(n)$	-1	-1	2						
$y_2(n)$			-3	-1	4				
$y_3(n)$					-4	1	3		
$y_4(n)$							-2	1	1
	-1	-1	-1	-1	0	1	1	1	1

$$y(n) = \{-1, -1, -1, -1, 0, 1, 1, 1, 1\}$$



APPLICATIONS



Communication Signal Processing

- * To remove noise which are added during transmission can be removed using filter where the operation involved is convolution



ASSESSMENT



1. List the methods involved to compute sectioned convolution.
2. Mention some applications of sectioned Convolution.
3. What is meant by sectioned Convolution.
4. Determine linear convolution $x(n) = \{1,2,3,4,4,3,2,1\}$ and $h(n) = \{-1,1\}$ using Overlap Add Method
5. The output sequences obtained from the convolutions of all the sections are combined to get the overall ----- sequence



THANK YOU