

SNS COLLEGE OF TECHNOLOGY



An Autonomous Institution Coimbatore-35

Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A+' Grade Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

19ECB212 - DIGITAL SIGNAL PROCESSING

II YEAR/ IV SEMESTER

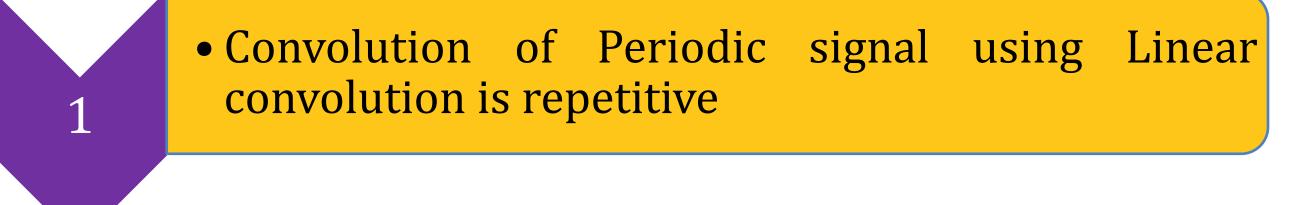
UNIT 1 – DISCRETE FOURIER TRANSFORM

TOPIC – Circular Convolution



EMPATHY





Convolution takes lot of time

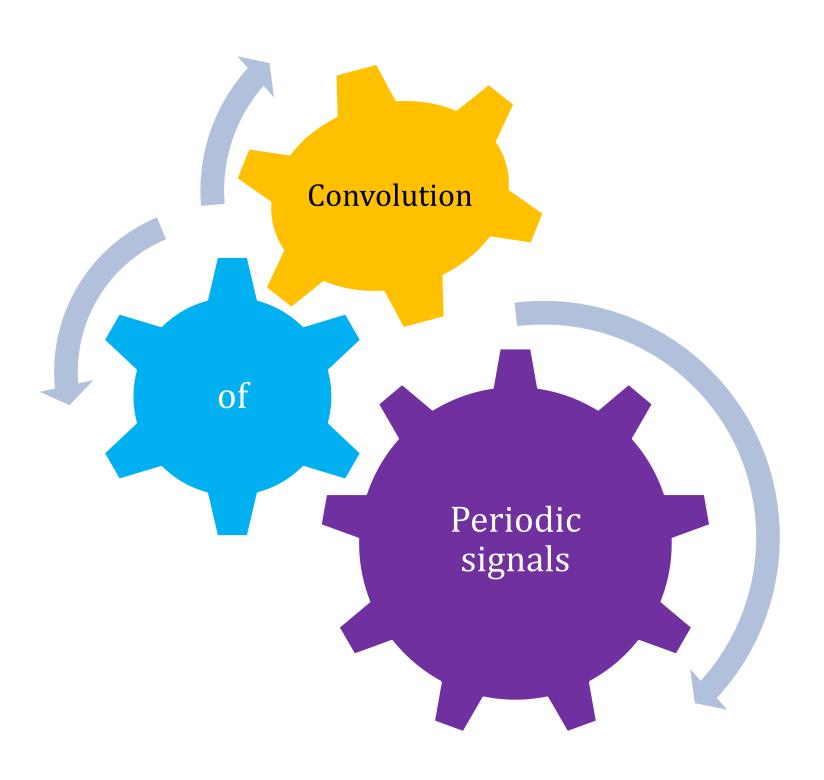
Utilization of DFT for Convolution

3



DEFINE

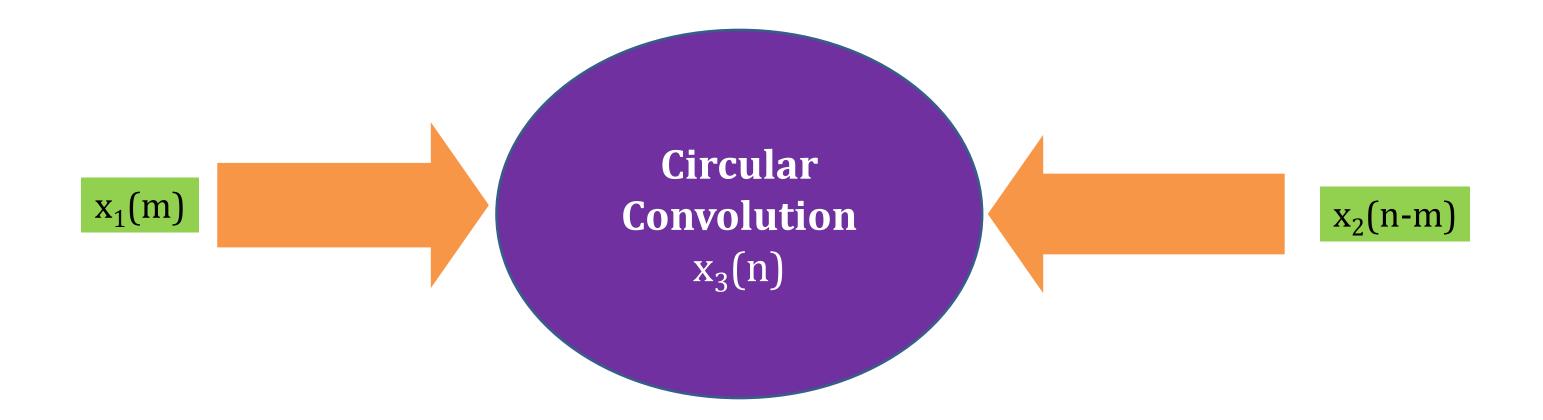






METHOD

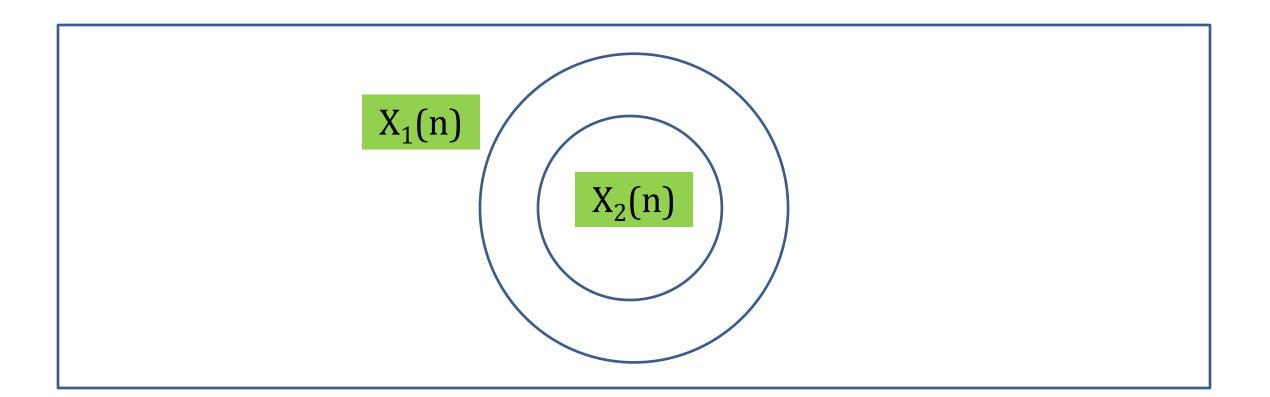






NEED FOR CONVOLUTION





- To find the output of a system with input and impulse response of the system linear convolution is used
- Circular Convolution can be applied for periodic signals and to obtain linear
 Convolution through Circular padding of zeros are done





• The circular convolution of two periodic discrete time sequences $X_1(n)$ and $X_2(n)$ with periodicity of N sample is defined as

$$y(n) = x(n) * h(n) = \sum_{k=0}^{N-1} x(k) . h(n-k)$$
 $x_3(n) = \sum_{m=0}^{N-1} x_1(m) x_2[((n-m))_N]$

• If x (n) and h(n) two finite duration signals with length M and P respectively then the length of y(n) = x(n) * h(n) is N=M+P-1 samples





- If x (n) and h(n) two periodic signals with period N then the length of
 - $y(n) = x(n) \circledast h(n)$ is also N
- The convolution of two periodic signal is also periodic and is circular convolution.

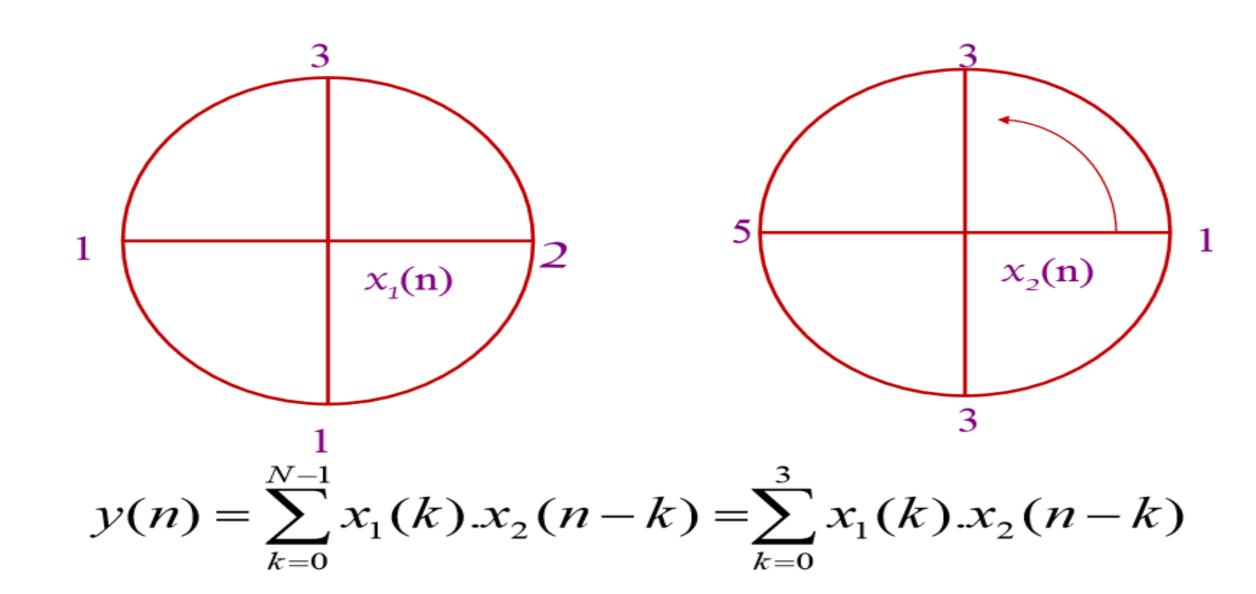
$$y(n) = x(n) \circledast h(n)$$

• Linear Convolution can be obtained by circular convolution by changing the length of both signals x(n) and h(n) to N by zero padding





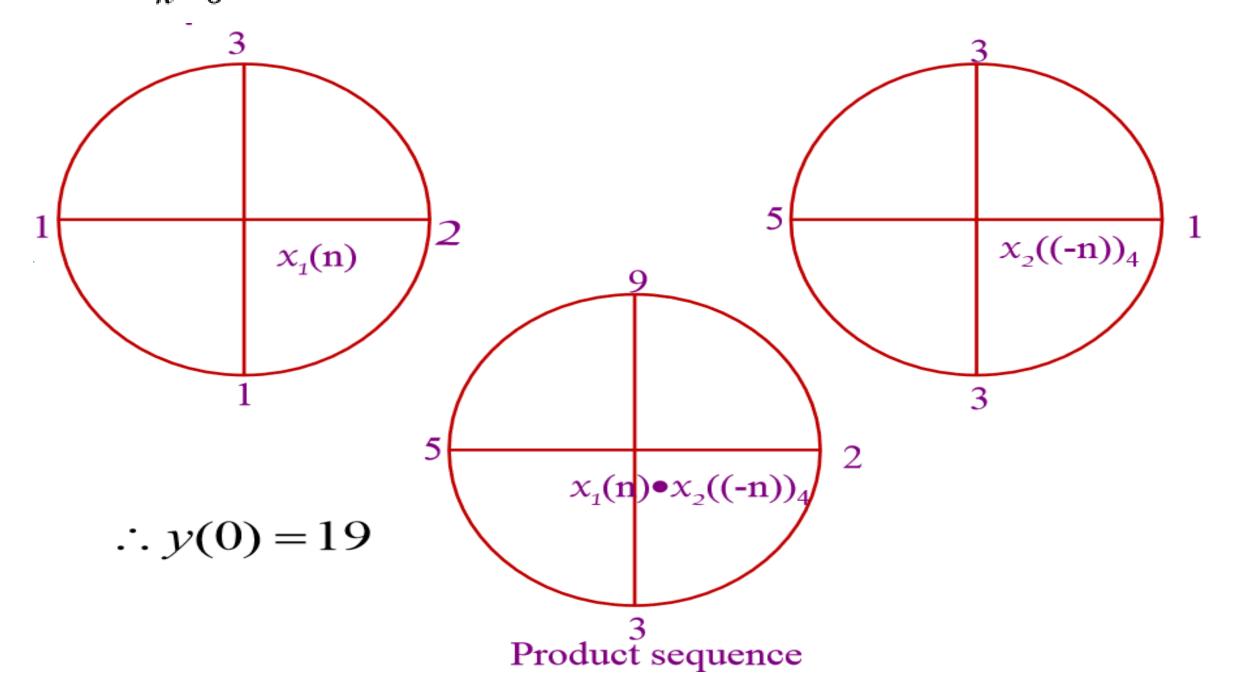
• Compute the circular convolution using time domain approach for the following sequence: $X_1(n) = \{2,3,1,1\}$ and $X_2(n) = \{1,3,5,3\}$





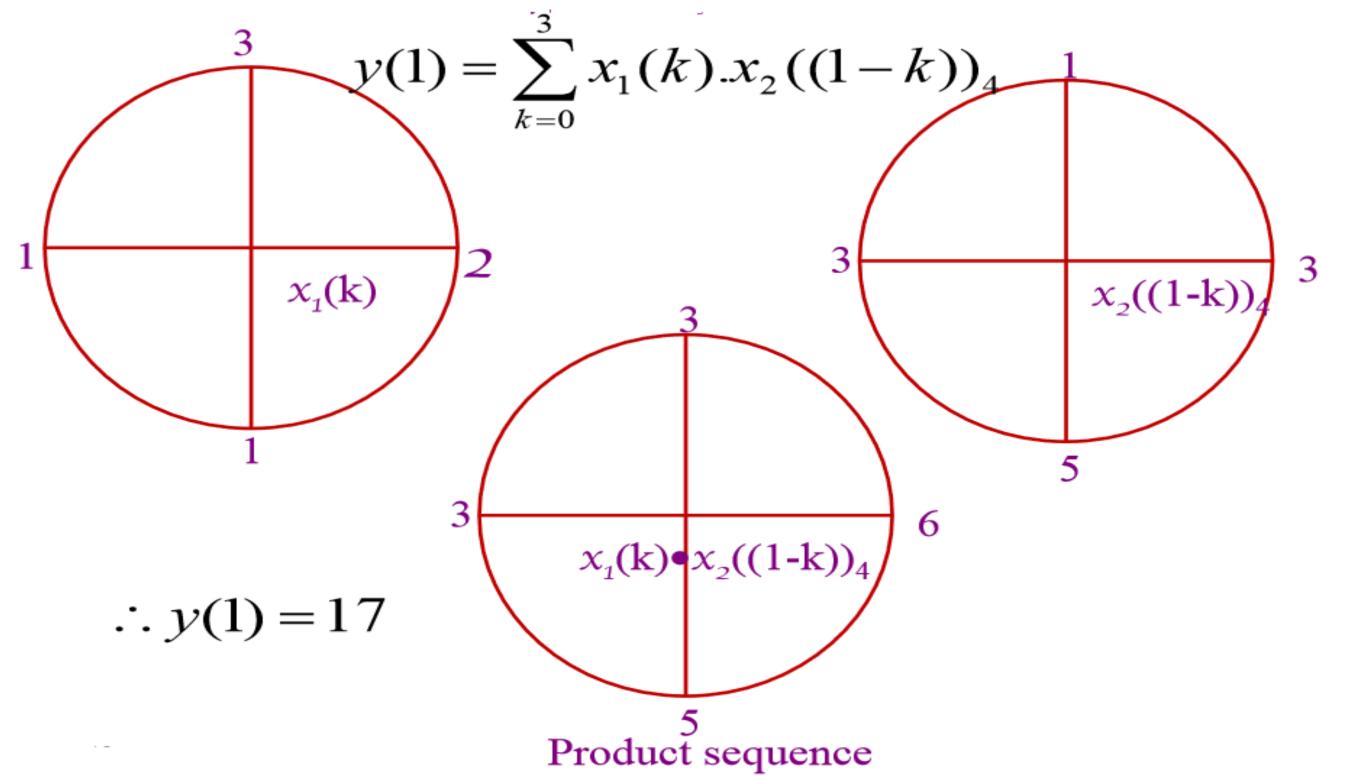


$$y(0) = \sum_{k=0}^{3} x_1(k).x_2(-k)$$



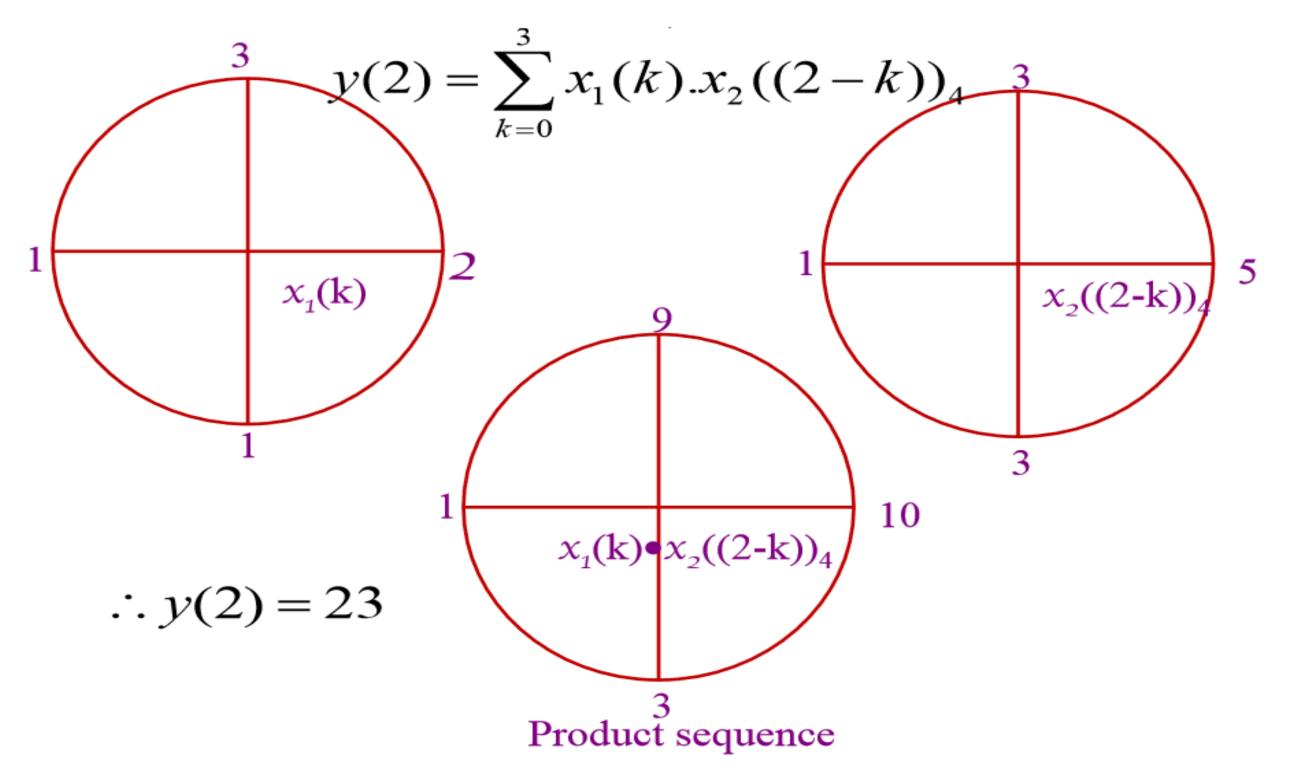






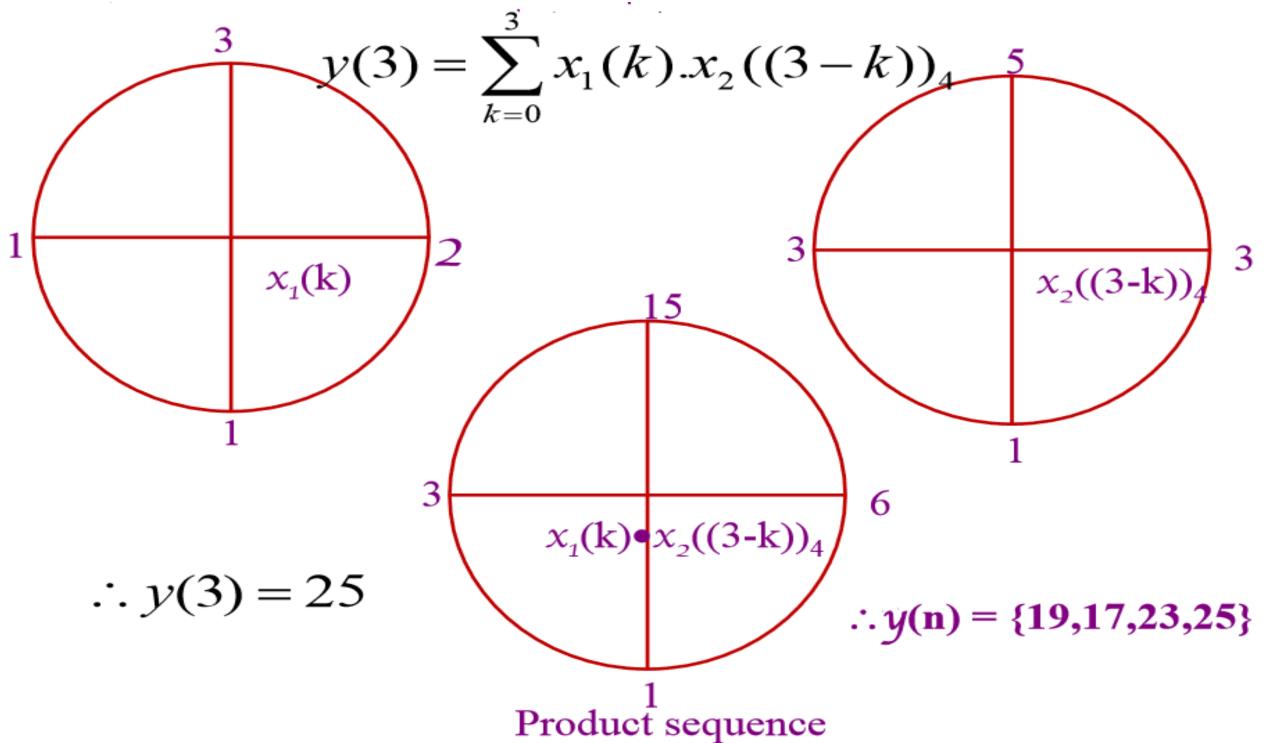














CIRCULAR CONVOLUTION – MATRIX APPROACH



$$y[n] = \begin{bmatrix} h(0) & h(N-1) & \dots & h(1) \\ h(1) & h(0) & \dots & h(2) \\ \vdots & \vdots & \dots & \vdots \\ h(N-1) & h(N-2) & \dots & h(0) \end{bmatrix} \begin{bmatrix} x(0) \\ x(1) \\ \vdots \\ x(N-1) \end{bmatrix}$$

$$e.g. \ h(n) = \{2,3,1,1\} \text{ and } x(n) = \{1,3,5,3\}$$

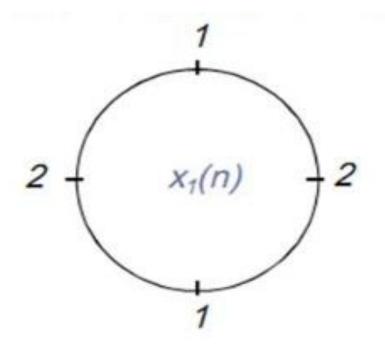
$$\therefore y[n] = \begin{bmatrix} 2 & 1 & 1 & 3 \\ 3 & 2 & 1 & 1 \\ 1 & 3 & 2 & 1 \\ 1 & 1 & 3 & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 3 \\ 5 \\ 3 \end{bmatrix}$$

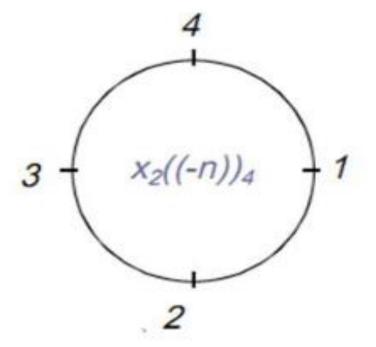
$$\therefore y[n] = \begin{bmatrix} 2+3+5+9 \\ 3+6+5+3 \\ 1+9+10+3 \\ 1+3+15+6 \end{bmatrix} = \begin{bmatrix} 19 \\ 17 \\ 23 \\ 25 \end{bmatrix}$$

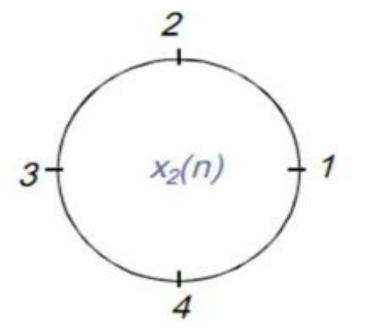


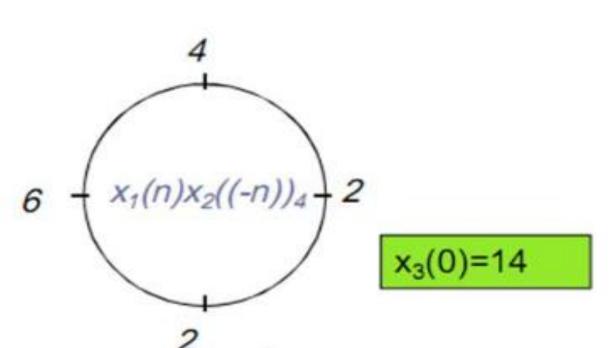


Perform circular convolution $X_1(n) = \{2,1,2,1\}$ and $X_2(n) = \{1,2,3,4\}$



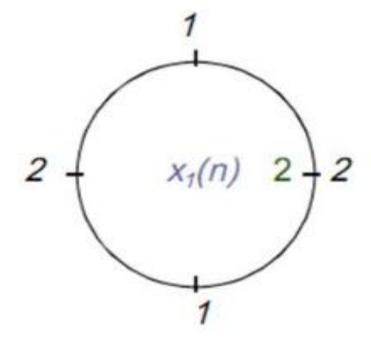


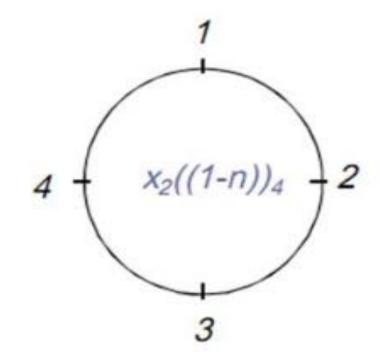


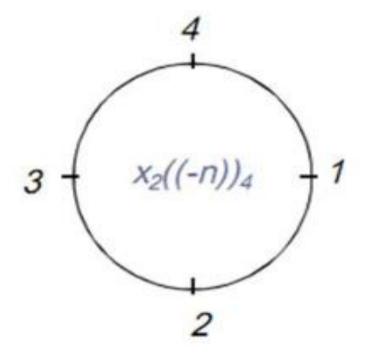


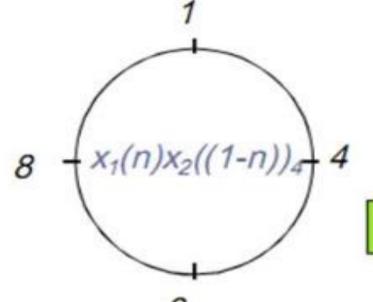








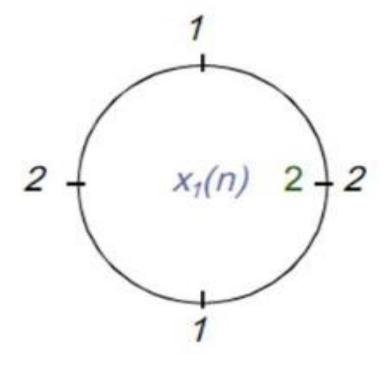


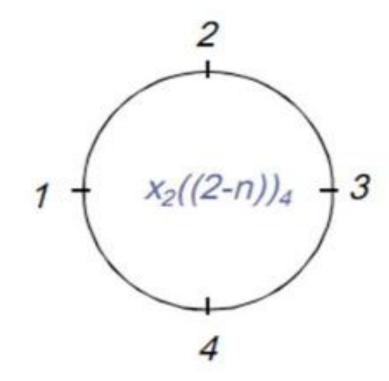


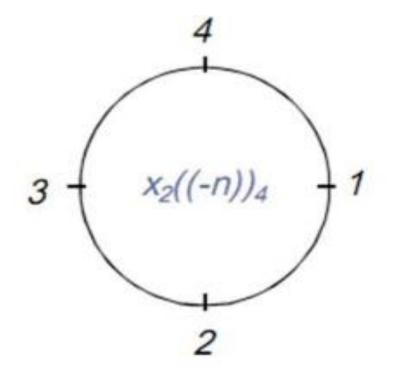
 $x_3(1)=16$

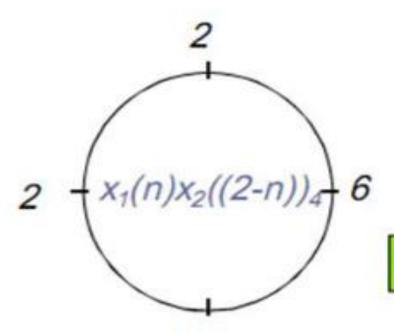








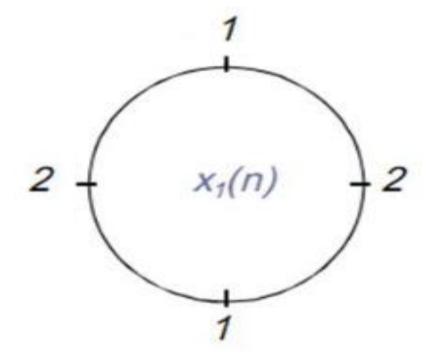


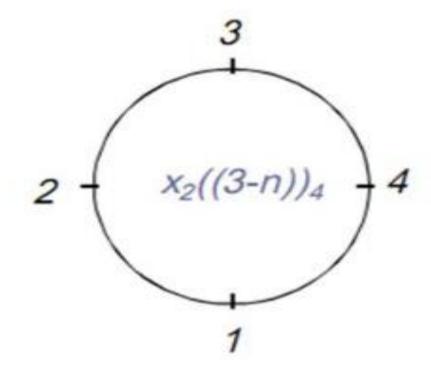


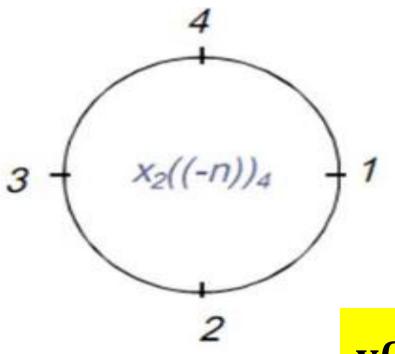
 $x_3(2)=14$

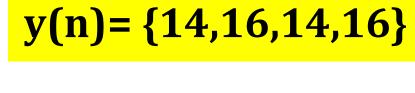


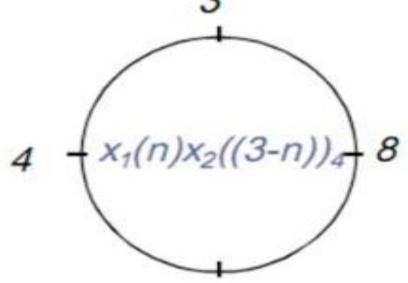












 $x_3(3)=16$



DIFFERENCE B/W LINEAR & CIRCULAR CONVOLUTION



S.No.	Linear Convolution	Circular Convolution
1	In case of convolution two signal sequences input signal x(n) and impulse response h(n) given by the same system, output y(n) is calculated	Multiplication of two DFT s is called as circular convolution.
2	Multiplication of two sequences in time domain is called as Linear convolution	Multiplication of two sequences in frequency domain is called as circular convolution.
3	Linear Convolution of two signals returns N-1 elements where N is sum of elements in both sequences.	Circular convolution returns same number of elements that of two signals.
4	$y(n) = \sum_{k=-\infty}^{\infty} x(k) h(n-k)$	$x_3(n) = \sum_{m=0}^{N-1} x_1(m) x_2 [((n-m))_N]$



ASSESSMENT



- 1. Define Circular Convolution.
- 2. If x (n) and h(n) two finite duration signals with length M and P respectively then the length of y(n) = x(n) * h(n) is ------ samples
- 3. Mention some applications of Circular Convolution.
- 4. Determine circular convolution of $X_1(n) = \{2,1,2,1\}$ and $X_2(n) = \{1,2,3,4\}$
- 5. What is the difference between linear convolution and circular convolution.





THANK YOU