

### **SNS COLLEGE OF TECHNOLOGY An Autonomous Institution Coimbatore-35**

Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A++' Grade Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

## **DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING 19ECB212 – DIGITAL SIGNAL PROCESSING**

II YEAR/ IV SEMESTER

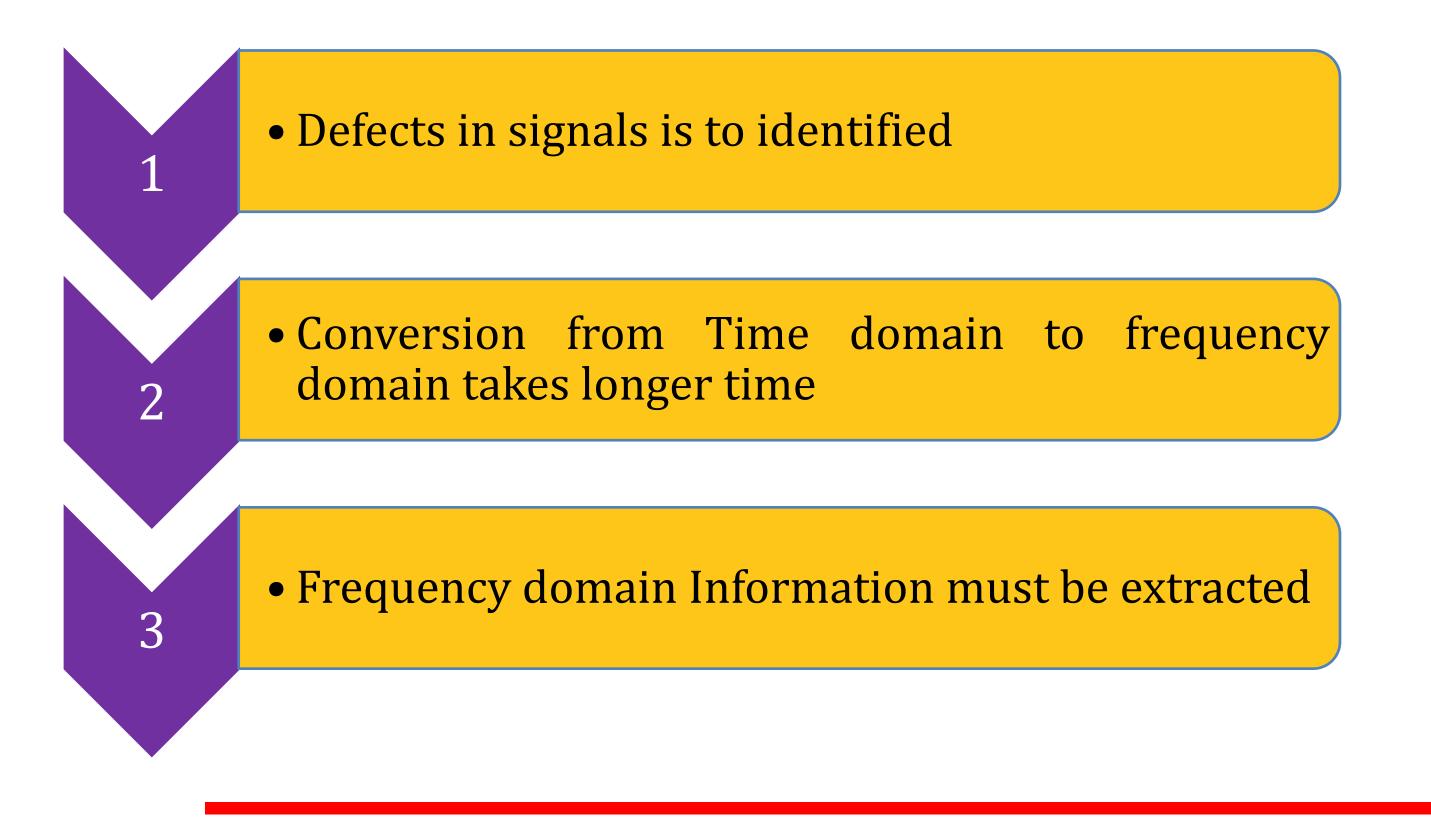
### **UNIT 1 – DISCRETE FOURIER TRANSFORM**

**TOPIC** – Introduction to DFT















# 3 Time to frequency domain conversion and process faster

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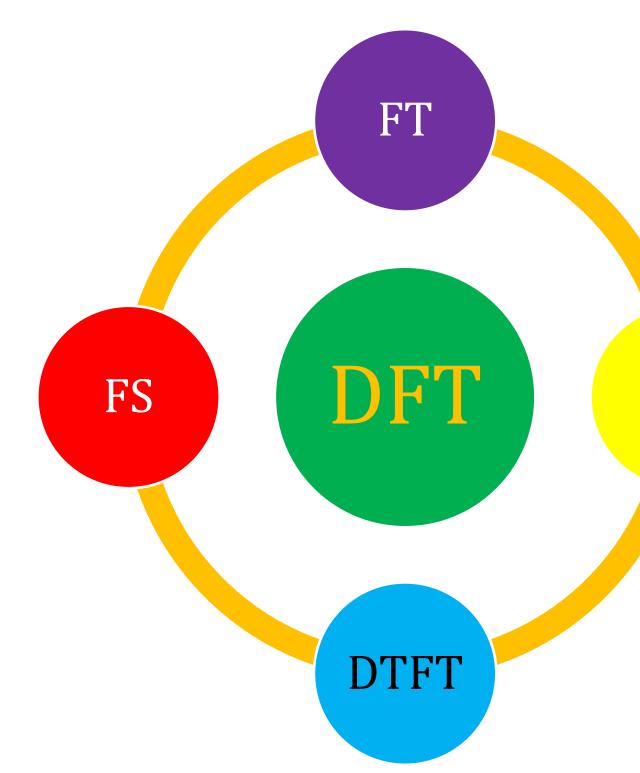




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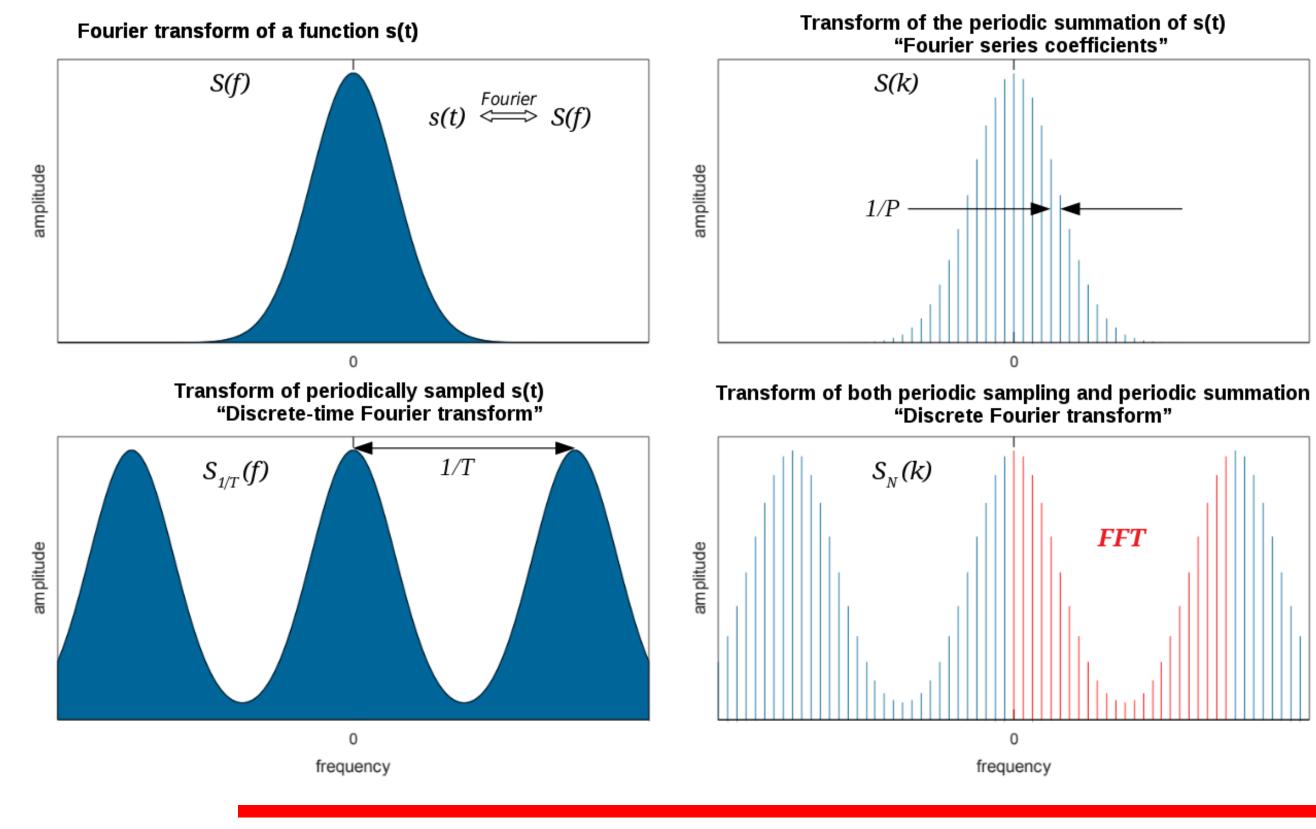
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### DFS



#### FOURIER COEFFICIENTS REPRESENTATION



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For a discrete time sequence we define two classes of Fourier **Transforms:** 

• The DTFT (Discrete Time FT) for sequences having infinite duration,

• The DFT (Discrete FT) for sequences having **finite** duration.

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DTFT AND INVERSE DTFT

DTFT

 $X(\omega) = DTFT\{x(n)\} = \sum x(n)e^{-j\omega n}$ 

**Inverse DFT** 

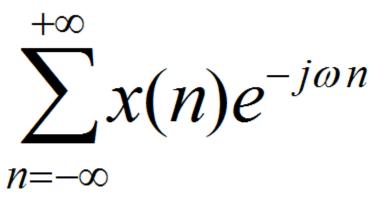
 $x(n) = IDTFT\left\{X(\omega)\right\} = \frac{1}{2\pi} \int_{-\infty}^{+\infty} X(\omega)e^{j\omega n}d\omega$ 

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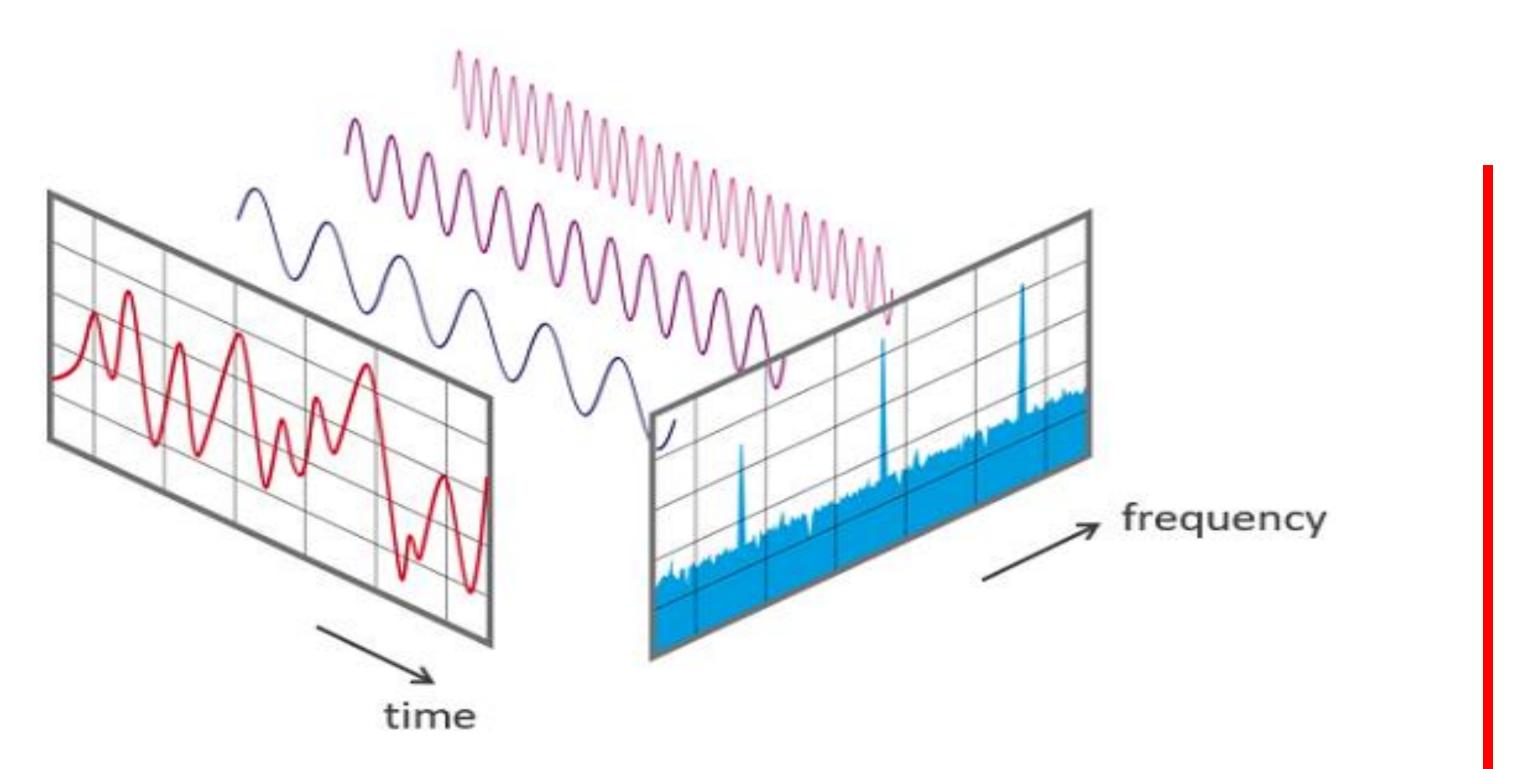
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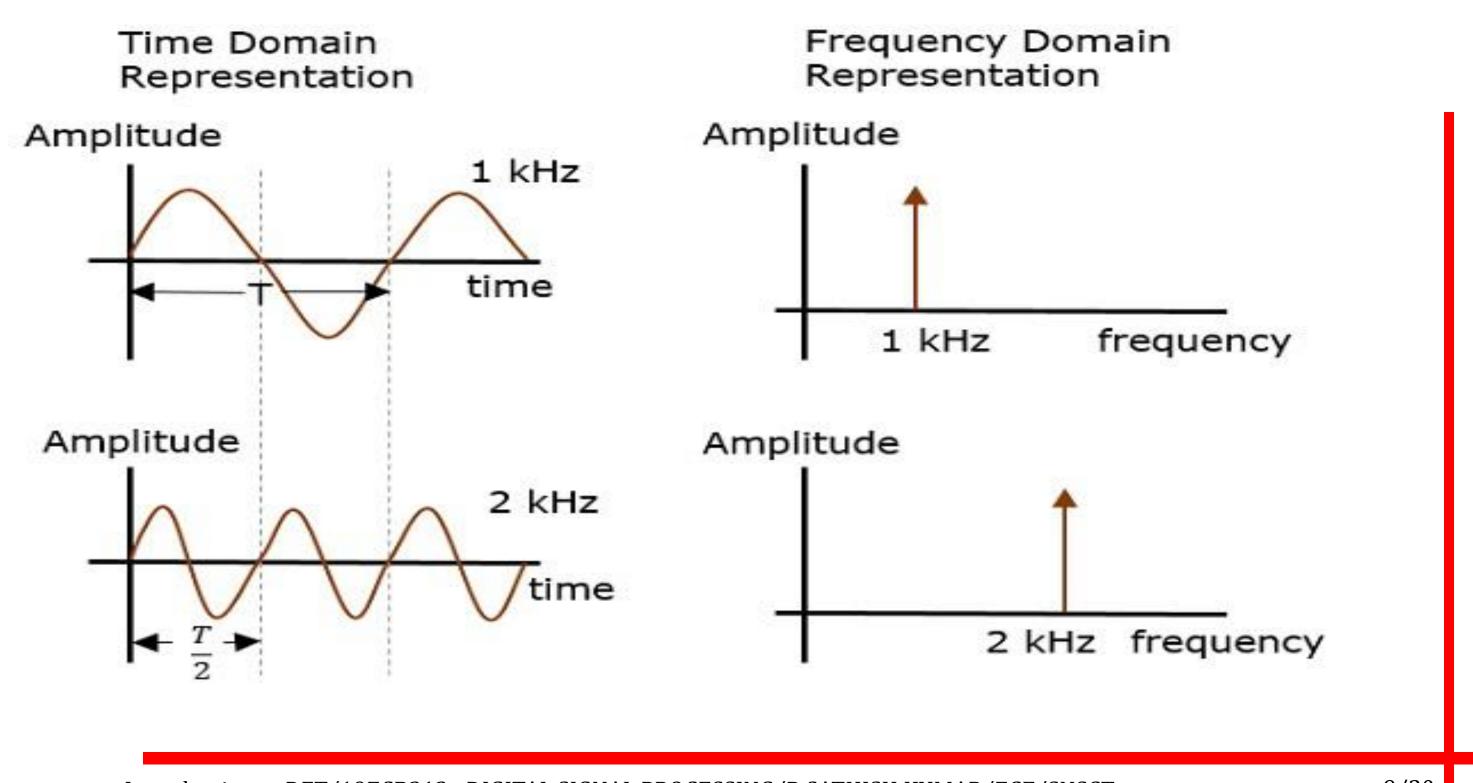
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#### **REPRESENTATION OF SIGNALS**



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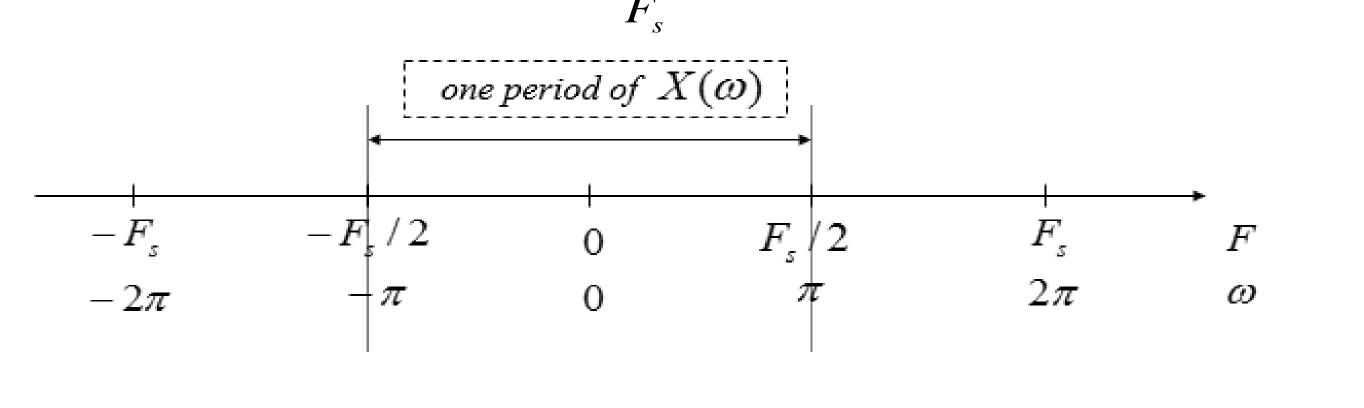




- The DTFT **X(\omega)** is periodic with period  $2\pi$
- The frequency  $\boldsymbol{\omega}$  is the digital frequency and therefore it is limited to the interval

 $-\pi < \omega < +\pi$ 

• The digital frequency  $\boldsymbol{\omega}$  is a normalized frequency relative to the sampling  $\omega = 2\pi \frac{F}{F_{\rm s}}$ frequency, defined as

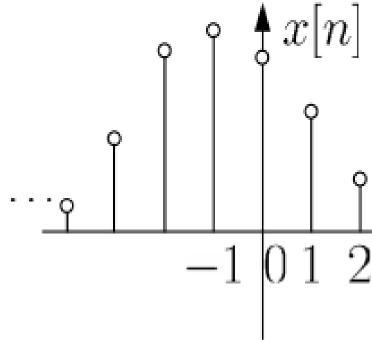






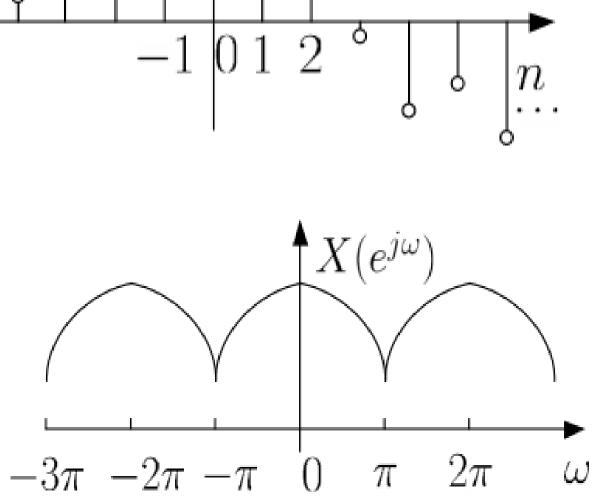


#### **DFT REPRESENTATION**



### **Freq Domain**

**Time Domain** 



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In Discrete Fourier Transform, Given a finite sequence

$$x = [x(0), x(1), ..., x(N-1)]$$

its Discrete Fourier Transform (DFT) is a finite sequence

$$X = DFT(x) = [X(0), X(1), \dots, X(N-1)]$$

Where 
$$X(k) = \sum_{n=0}^{N-1} x(n) w_N^{kn}, \quad w_N =$$

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1)]

 $=e^{-j2\pi/N}$ 





INVERSE DISCRETE FOURIER TRANSFORM

*In Inverse Discrete Fourier Transform, Given a sequence* 

$$X = [X(0), X(1), ..., X(N-1)]$$

its Inverse Discrete Fourier Transform (IDFT) is a finite sequence

 $x = IDFT(X) = [x(0), x(1), \dots, x(N-1)]$ 

Where

$$x(n) = \frac{1}{N} \sum_{k=0}^{N-1} X(k) w_N^{-kn}, \quad w_N$$

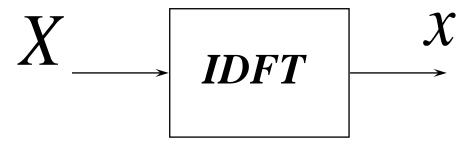
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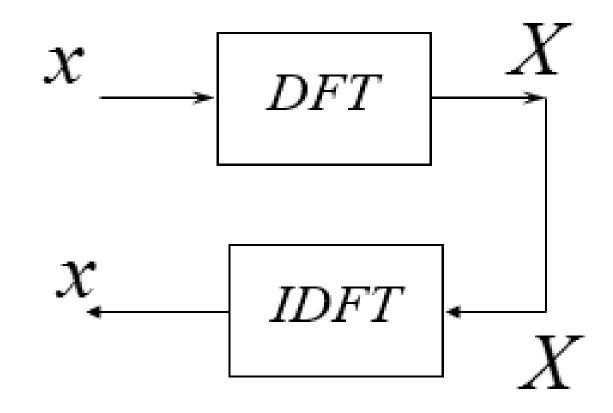
L)|



 $v = e^{-j2\pi/N}$ 



#### The DFT and the IDFT form a transform pair.



The DFT is a numerical algorithm, and it can be computed by a digital computer.

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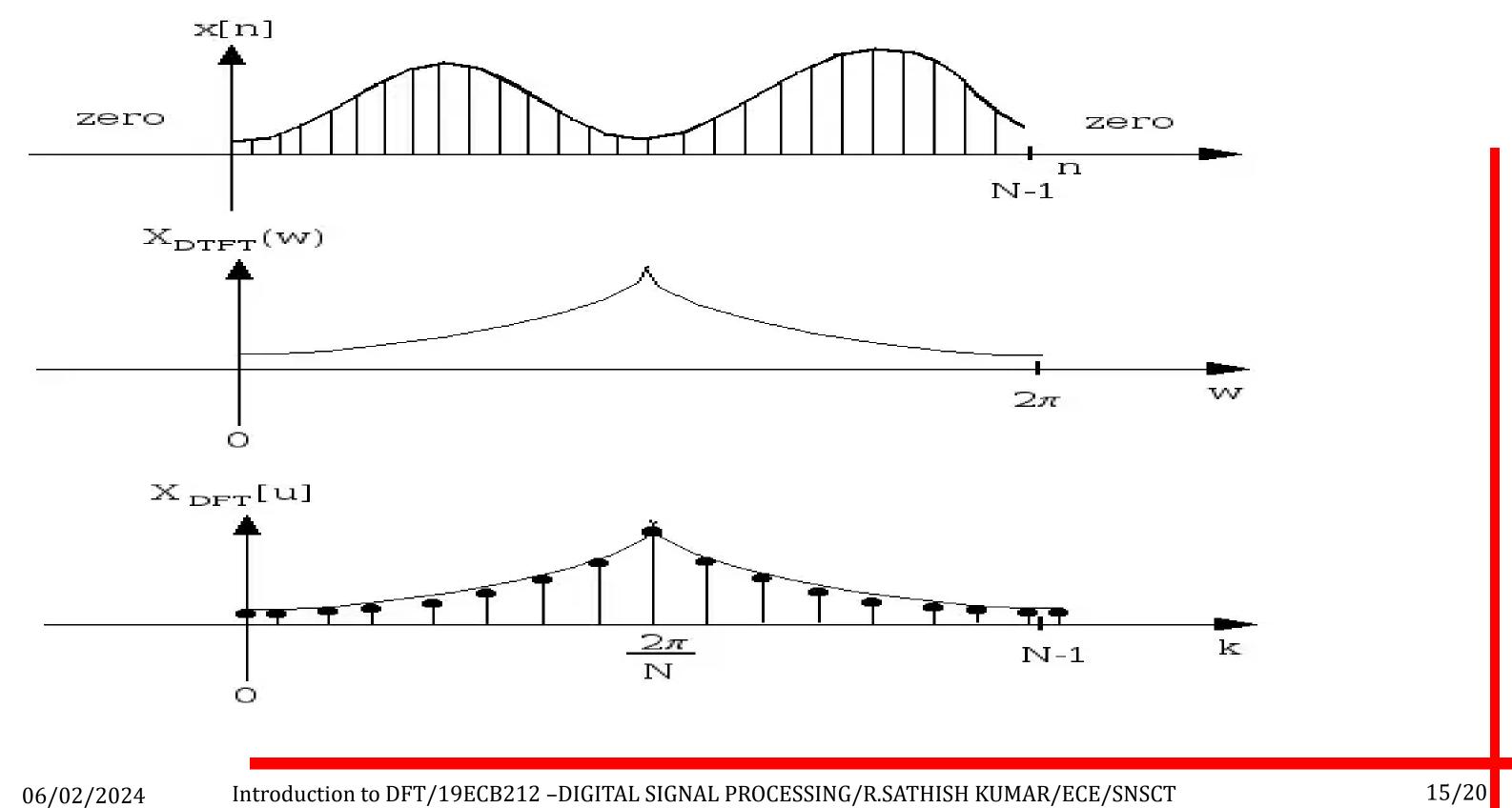
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#### **REPRESENTATION OF DTFT & DFT**









### **PROPERTIES OF DFT**

Property	Time Domai
1. Linearity	$ax_1[n] + bx_2[n]$
2. Time-shifting	x[n-m]
3. Frequency-shifting (modulation)	$e^{-j2\pi k_0 n/N} x[n]$
4. Time reversal	x[-n]
5. Conjugation	$x^*[n]$
6. Time-convolution	$x_1[n] \otimes x_2[n]$
7. Frequency-convolution	$x_1[n]x_2[n]$



## in Frequency Domain $aX_{1}[k] + bX_{2}[k]$ *i*] $e^{-j2\pi km}X(k)$ $X(k - k_0)$ X(-k) $X^*(-k)$ $X_1[k]X_2[k]$ $\frac{1}{N}X_1[k] \otimes X_2[k]$



### **APPLICATIONS OF DFT**

- 1. Spectral Analysis
- 2. Image Processing
- 3. Signal Processing

#### **Other Applications:**

- 1. Sound Filtering
- 2. Data Compression
- 3. Partial Differential Equations
- 4. Multiplication of large integers

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### DIFFERENCE B/W DFT & IDFT

DFT (Analysis transform)	IDFT (Synthesis tra
DFT is finite duration discrete frequency sequence that is obtained by sampling one period of FT. DFT equations are applicable to causal finite duration sequences. Mathematical Equation to calculate DFT is given by N-1 $X(k) = \sum_{n=0}^{N-1} x(n) e^{-j2} \prod_{n=0}^{N-1} kn / N$	IDFT is inverse DFT domain representation sequence) form of x( IDFT is used basic response of a filter transfer function. Mathematical Equat by N-1 $x(n) = 1/N \sum X (k) = 0$
Thus DFT is given by X(k)= [WN][xn]	In DFT and IDFT disign of exponent of two Thus $x(n)=1/N [WN]^{-1}[Y$





#### ansform)

T which is used to calculate time ion (Discrete time (k).

cally to determine sample for which we know only

tion to calculate IDFT is given

### $e^{j2} \prod kn / N$

lifference is of factor 1/N & widdle factor.

#### XK]



### ASSESSMENT

- **Define DFT** 1.
- What is meant by IDFT. 2.
- Give some applications of Discrete Fourier Transform. 3.
- Define DFT Pair. 4.
- 5. The DTFT (Discrete Time FT) for sequences having
- Mention the Properties of DFT. 6.





# THANK YOU

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