

SNS COLLEGE OF TECHNOLOGY An Autonomous Institution Coimbatore-35

Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A+' Grade Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING 19ECB212 – DIGITAL SIGNAL PROCESSING

II YEAR/ IV SEMESTER

UNIT 1 – DISCRETE FOURIER TRANSFORM

TOPIC – Circular Convolution

CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT









CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT



Linear







CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT









3-Mar-24

CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT









NEED FOR CONVOLUTION



find the output of a system with input and impulse response of the system To

linear convolution is used

Circular Convolution can be applied for periodic signals and to obtain Convolution through Circular padding of zeros are done





linear



The circular convolution of two periodic discrete time sequences ullet

 $X_1(n)$ and $X_2(n)$ with periodicity of N sample is defined as

$$y(n) = x(n) * h(n) = \sum_{k=0}^{N-1} x(k) \cdot h(n-k) \qquad x_3(n) = \sum_{m=0}^{N-1} x_1(m) x_2[((n-m))_N]$$

• If x (n) and h(n) two finite duration signals with length M and P respectively then the length of y(n) = x(n) * h(n) is **N=M+P-1** samples







If x (n) and h(n) two periodic signals with period N then the length of

 $y(n) = x(n) \circledast h(n)$ is also N

The convolution of two periodic signal is also periodic and is circular \bullet convolution.

y(n) = x(n) ↔ h(n)

Linear Convolution can be obtained by circular convolution by changing the length of both signals x(n) and h(n) to N by zero padding





Compute the circular convolution using time domain approach for the following sequence: $X_1(n) = \{2,3,1,1\}$ and $X_2(n) = \{1,3,5,3\}$









CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT









CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT









CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT









CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT

3-Mar-24







CIRCULAR CONVOLUTION - MATRIX **APPROACH**

$$y[n] = \begin{bmatrix} h(0) & h(N-1) & \dots & h \\ h(1) & h(0) & \dots & h(0) \\ \vdots & \vdots & \ddots & \vdots \\ h(N-1) & h(N-2) & \dots & h(0) \\ e.g. & h(n) = \{2,3,1,1\} \text{ and } x(n) = \{1, 0, 0\} \\ \vdots & y[n] = \begin{bmatrix} 2 & 1 & 1 & 3 \\ 3 & 2 & 1 & 1 \\ 1 & 3 & 2 & 1 \\ 1 & 1 & 3 & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 3 \\ 5 \\ 3 \\ 5 \\ 3 \\ 5 \\ 3 \\ 5 \\ 3 \\ 5 \\ 1 + 9 + 10 + 3 \\ 1 + 3 + 15 + 6 \end{bmatrix} = \begin{bmatrix} 2 + 3 + 5 + 9 \\ 3 + 6 + 5 + 3 \\ 1 + 9 + 10 + 3 \\ 1 + 3 + 15 + 6 \end{bmatrix} = \begin{bmatrix} 2 + 3 + 5 + 9 \\ 3 + 6 + 5 + 3 \\ 1 + 9 + 10 + 3 \\ 1 + 3 + 15 + 6 \end{bmatrix}$$

CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT





i(1)x(0)(2)*x*(1) x(N-1)v(0),3,5,3}

19 17 23 25





CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT









CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT









CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT









CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT







DIFFERENCE B/W LINEAR & CIRCULAR CONVOLUTION

S.No.	Linear Convolution	(
1	In case of convolution two signal sequences input signal x(n) and impulse response h(n) given by the same system, output y(n) is calculated	Multiplica circular co
2	Multiplication of two sequences in time domain is called as Linear convolution	Multiplica frequency convolutio
3	Linear Convolution of two signals returns N-1 elements where N is sum of elements in both sequences.	Circular number of
4	$y(n) = \sum_{k=-\infty}^{\infty} x(k) h(n-k)$	$x_{3}(n) =$

CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT





Circular Convolution

tion of two DFT s is called as onvolution.

ition of two sequences in domain is called as circular on.

convolution returns same f elements that of two signals.

$$=\sum_{m=0}^{N-1}x_1(m)x_2[((n-m))_N]$$



ASSESSMENT

- Define Circular Convolution. 1.
- If x (n) and h(n) two finite duration signals with length M and P respectively then 2. the length of y(n) = x(n) * h(n) is ------ samples
- 3. Mention some applications of Circular Convolution.
- Determine circular convolution of $X_1(n) = \{2, 1, 2, 1\}$ and $X_2(n) = \{1, 2, 3, 4\}$ 4.
- 5. What is the difference between linear convolution and circular convolution.





THANK YOU

3-Mar-24

CIRCULAR CONVOLUTION/19ECB212 – DIGITAL SIGNAL PROCESSING/J.PRABAKARAN/ECE/SNSCT





