



(An Autonomous Institution)
Coimbatore – 35

DEPARTMENT OF MATHEMATICS UNIT – II TESTING OF HYPOTHESIS

CAI - SQUARE TEST :

$$\chi^{2} = \underbrace{\Xi[0:-E:]^{2}}_{E:}$$
where $0: \rightarrow Observed$ frequency
$$E: \rightarrow Enyeinmental frequency or Enjected frequency
perfect & freedom, $v = n - 1$$$

properties:

1) The mean 2 12 dist. is equal to the no. q cleyers q freedom

ii) The variance of 8° dist. is twice the degrees q freedom

iii) The variance of 8° dist. is twice the degrees q freedom

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the 0 272 is a garrina variate with parameter 1/2.

iv) standard To variate tinds to standard normal variate

as n \rightarrow 8.

Applications:

1) To test of the hypothetical value of the population variance

is To test of the hypothetical value of the population variance

ii) To test the spoodness of fit.

iii) To test the show yenicity of incluse. estimates of the

population variance.

Degrees of freedom! No. 2 values on a set which may be

assigned autitually.





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1) The table below eyou's the number of accept accidents that occurred during the various days of the week. Test whether the accidents are uniformly distributed over the week.

Pays: Mon Tues Weel Thurs Fri Sat

No q accidents: 14 18 12 11 15 14

Soln:

Lyven, total no of accidents = 84

No . of days = 6

Expected frequencies of the accidents = 84

Corete (Oi-Ei)2 (Oi-Ei)2

14 14 0 0/14: 0

Step1: Harmilate Ho & H , :

Ho: The accidents are uniformly distributed.

ctip 2 : Los at x = 5 %.

step 3: Test statisfie, $\chi^2 = \underbrace{\Xi(Q_1 - E_1)^2}_{E_1} = 2.1428$





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step 4: Degrees of freedom, v = n-1

Tab value is 11:04 = 00

Step 5: Conclusion:

x= 2.1428 < 11.04 = x2

.. Ho is accepted at 5% Los as the accident.

are uniquembly distributed.

2) A clie was thrown 498 times. Denoting n to be the number appearing on the top face quit, The observed frequency of n is ywen below:

91: 1 2 3 4 5 6 7: 69 48 85 82 86 98

what opinion you would form for the accuracy of The

Soln: Criven, Expected frequency, Ei = Total frequence

= 498 = 83





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step 1: Formulate Ho & H ,:

Ho: A sie is unbiased

H, : A sie is not unbiased is biqued.

step 2: Los at x = 5%.

sty 3: Test Statustic, 22 = \(\(\text{Oi-Ei} \) = 5.542.

step 4: Degrees of freedom, v=n-1

· . 22 = 11.04.

step 5: Conclusion; $\chi^2 = 5.542 \times 11.04 = \chi^2_{\chi}$

: Ho is accepted at 5% Los @ A die is unliqued





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CHI SQUARE TEST FOR INDEPENDENCE OF ATTRIBUTES.

Doe the basis of information noted below, find out whether the new treatment is comparatively superior to the conventional one.

	Favourable.	Not Favoruable	weal
New	60	30	90
Conventional	40	70	110
n: total	100	100 ->	200

90 × 100 : 45	90 x 100 : 45	
110 × 100	110 × 100 : 55	. simmy or the co





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00 Ei 0i-Ei (0i-Ei) / Ei

60 45 15 5

30 45 -15 5

40 55 -15 4.09

40 55 15 4.09

$$\sum_{EL} (a_1 - a_2)^2 \cdot 18.18$$

step 1: Formulating Ho & H .:

Ho: There is no difference believen mew & conventional treatment.

HI: There is difference heteren men & conventinal breatment.

step 2. Los at x = 5%.

slep 3: Test statistics, 22 = \(\frac{(0:-Ei)^2}{Ei} \)
= 18.18

step 4: Degrees of Freedom, N = ((3-1)+(+-1))

V= (2-1 * 2-1)

= 1 *1

. . tab value, Xx = 3.841

top 5 : Conclusion:

X2 = 18.18 > 3.841 = 72

. Ho is rejected at 5 1/. Los

treatment.





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2) Two resease	cheis A	and B ac	dopted differen	t techniques
	14. 151d	ent. leve	1. Can you see	y meet me
1 1 00 00	untell in	them on	e myrufican	5
1	polous	ava. A	lvg. Above my	. Genius notal
Kuseuceres	40	3	33	
	20	./~	60 44	10 200
В	FA 1 24	and the	6.01	12 300
-to-tal	126	9.	69	
To for	ol r.			V Feeth
10 Pa			or was to	
	100 x 126: 4	2 100 × 93	· 31 100×69: 2	3 300 4
	200 x 126.8	4 200×93	: 62 200×69 :4	6 200x19 .g
	300	300	300	300
0:	Eį	Oc - E:	(0:-Ei)/E:	
40	42	-2	0.0952	
33	31	2	0-129	
25	23	2	0-173	
2	4	- 2	1	
86	84	Q	0.047	
60	62	- 2	0.064	
44	46	- 2	0.086	
16	8	2		V 19
		5 (oi	-Ec)2: 2 097	





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Step 1: Formulating Ho and HI:

Ho: There is no difference tretween the two

H.: There is difference between the two revearchers

(step 2 : Los at x = 5%.

step 3: Test statuties, $\chi^2 = \underbrace{\mathbb{E}\left(0i-\epsilon_i\right)^2}_{Ei}$

step 4: peyers of freedom, v = ((4-1) * (2-1))

= (3 * 1) ..

: Tab value is 2 = 4.115

glap 5: Conclusion.

82 = 2.097 <1115 = 22x

: Ho is accepted at 5% Los

(a) There is no difference between The two serearchers,