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DEPARTMENT OF MATHEMATICS UNIT - II TESTING OF HYPOTHESIS

DEST OF SIGNIFICENCE OF SMALL BAMPLES!

VARIANCE RATIO TEST (OT) F- Test JOR EQUALITY OF YARIAN

Null Thypothesis : Ho: T,2= 022

Test startics: $F = \frac{S_1^2}{S_2^2}$ where $S_1^2 > S_2^2$.

where $S_1^2 = \frac{n_1 s_1^2}{n_1 - 1}$ of $S_1^2 = \frac{\sum (x_1 - \overline{x_1})^2}{n_1 - 1}$ &

 $\frac{S_2^2 = n_2 S_2^2}{n_2 - 1} \text{ of } S_2^2 = \frac{\sum (n_2 - \bar{n}_2)^2}{n_2 - 1}$

Deglee & Freedom, (V, V2)

where 1 = (n,-1), 1/2 = (n,-1)

Note 1:- F Greater than your always.

Note 2: - Suppose S_2^2 greater than S_1^2 , then $F = \frac{S_2^2}{S_1^2}$ with degree 9 greadom, $V_1 = n_2 - 1$, $V_2 = n_1 - 1$

from the same population.





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) two landom sample 9 11 and 9 items show that the sample standard deviations 9 their weights as 0.8 & 0.5 neighboring. Assuming that the weight distributions are normal, test the hypothesis that the true variances are equal, against the alternative hypothesis that they are not Son: Given · · n, = 11 , 3, = 0.8 no = 9 , 80 = 0.5 $S_1^2 = \frac{0.61^2}{0.1-1} = \frac{11(0.8)^2}{11-1} = 0.404$ B22 = 1 262 = 9(0.5)2 = 0.2812 Step 1 -> Formulate Ho & HI. Ho: 5,2=0,2 para to the to the H1: 52 + 5. 2 stip 2 -> Los at x = 5 y. slip 3 > Test Statistic, F = 812 = 0.704 = 2.5 step 4 -> Degrees & freedom (1,12) (n.-1, n2-1) = 12 Ceincalvalue, Ftab : Fx = 3.35 Step 5 -> conclusion: F=2.5 < 3.35= Fx :. Ho is accepted at x:5%.





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) Two tandom samples yave the following lexulte: sample size samplemean sum à squeres à desiation from the means. 10 15 90 Yest whether The samples came from the same population. goln: n=12 , x1 = 14 , \((x1-\overline{x}_1)^2 = 108 no = 10, no = 15 & (no- No)= 90 $S_1^2 = \frac{\mathcal{L}(\eta_1 - \bar{\eta}_1)^2}{\Omega_{-1}} = \frac{108}{10.1} = 9.818$ $S_{3}^{2} = \frac{5(n_{3} - \overline{n}_{3})^{2}}{n_{3-1}} = \frac{90}{10-1} = 10$ 3,2 <5,2 step 1: Formulate Ho and Hi: Ho: 52=52 H1: V12 + 022 stip 2: Los at a = 5%. step 3: test statestics, = = \frac{82^2}{5.2} = \frac{10}{9.818}





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critical value, Fx = 2.90

Sty & : Conclusion:

.. Ho is accepted at 5% Los.

(11) t - Test:

step 1: Hormulate Ho & HI:

Now
$$S^2 = \underbrace{\xi(x_1 - \overline{x}_1)^2 + \xi(x_2 - \overline{x}_2)^2}_{n_1 + n_2 - \varrho}$$





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$$S_1^2 = \frac{\sum (n_1 - \overline{n}_1)^2}{n_1 - 1} = \frac{141.5}{7} = 5.9286$$

$$S_2^2 = \frac{\sum (n_2 - \overline{n}_2)^2}{n_2 - 1} = \frac{101.7148}{6} = 16.9524$$

$$S_1^2 < S_2^2$$

$$Step 1 : \text{ formulate Ho & Hi :}$$

$$H_0 : \nabla_1^2 = \nabla_2^2$$

$$H_1 : \nabla_1^2 \neq G_2^2$$

$$Step 2 : \text{ Los at } S = 1 \text{ y}.$$

$$Step 3 : \text{ Test statistic, } F = \frac{S_2^2}{S_1^2}$$

$$= \frac{16.9524}{5.9286} := 2.86$$

$$\text{Otep 4 : } \text{ Respects } q \text{ Freedom, : } (v_1, v_2)$$

$$= (n_2 - 1, n_1 - 1)$$

$$= (6, 4)$$

$$\text{Step 5 : Conclusion, } F = 2.86 < 7.19 = Fx$$

$$\text{Ho & accepted at Ho at } 1 \text{ y. 20s.}$$