

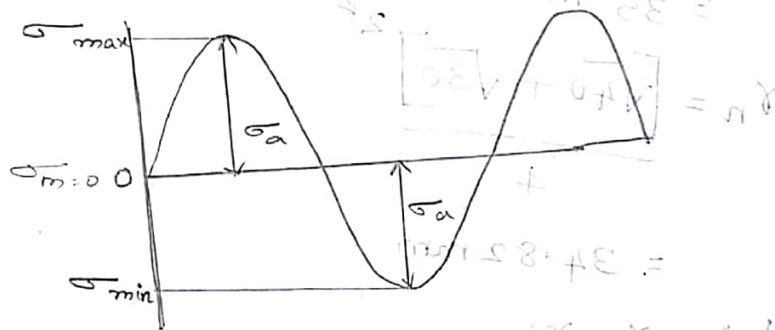
## Variable stresses.

The load in which the magnitude and direction changes with respect to time (eg) Axle shaft, Crank shaft, Connecting rod, springs, Pinion Teeth etc.

### Types

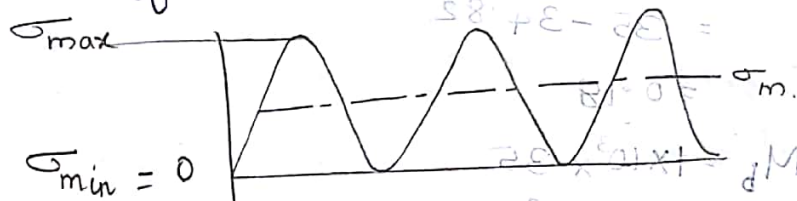
#### Reversed or Cyclic Stress

The stress that varies from one value of tensile to the same value of compression.

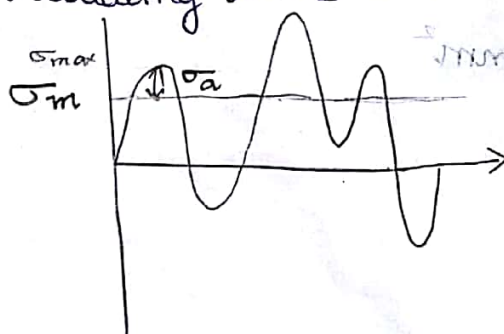


#### Repeated stress :-

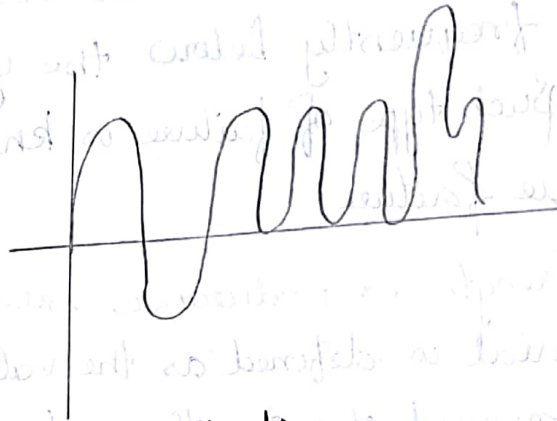
The stress which varies from zero to maximum value of same nature



#### Fluctuating Stress



Alternative stress.



Stress Concentration

Stress Concentration Factor:-

Whenever sudden change in cross section the maximum stress will induce. The ratio of Maximum stress to the normal stress is called as stress concentration factor.

$$(K_t) = \frac{\sigma_{max}}{\sigma_0}$$

Variable Loading (Fatigue stress)

Method to avoid stress concentration  
Avoid sharp edges.

Fatigue Failure

The load which varies in magnitude or direction with respect to time is known as fatigue or fluctuating or alternative load.

The variable stress induced in the component are known as fluctuating load  $\pm \frac{\sigma}{2}$

The mechanical component subjected to fluctuating load, it fail at stress

$$n = \frac{\sigma}{\sigma_0} + n \left( \frac{\sigma}{\sigma_0} \right)$$

considerably below the ultimate strength and quite frequently below the yield strength. Such type of failure is known as fatigue failure

Fatigue strength or Endurance strength of a material is defined as the value of completely reversed stress, the standard test specimen can withstand without failure for a given number of cycles

Endurance limit or Fatigue limit:

It is defined as maximum value of completely reversed test the standard test specimen can withstand without failure to an infinite number of cycles

S<sub>n</sub> curve used to find the endurance limit

$\sigma_1$  - endurance limit

Soderberg Relationship

$$\frac{\sigma_m}{\sigma_y} + \frac{\sigma_a}{\sigma_e} = \frac{1}{n}$$

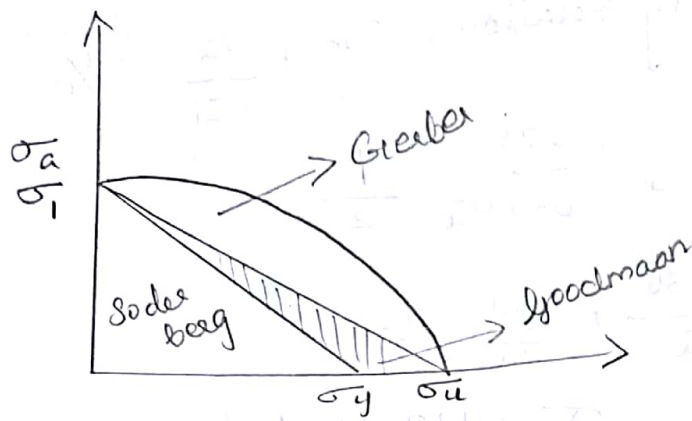
Goodman

$$\frac{\sigma_m}{\sigma_u} + \frac{\sigma_a}{\sigma_e} = \frac{1}{n}$$

Gerber

$$\left(\frac{\sigma_m}{\sigma_u}\right)^2 + \frac{\sigma_a}{\sigma_e} = \frac{1}{n}$$





Most preferable Goodman

1. Machine component is subjected to fluctuating stress which have fluctuating between  $300 \text{ MN/m}^2$  and  $-150 \text{ MN/m}^2$ . Determine the value of maximum ultimate strength according to Gerber relationship, Goodman relationship, Soderberg relationship.

Take  $\sigma_y = 0.55$  ultimate strength.  $\sigma_{-1} = 0.5 \sigma_u$

FOS = 2.

Given :-

$$\sigma_{\max} = 300 \text{ MN/m}^2$$

$$\sigma_{\min} = -150 \text{ MN/m}^2$$

$$\sigma_y = 0.55 \sigma_u$$

$$\sigma_{-1} = 0.5 \sigma_u$$

$$n = 2$$

Solu :-

$$\sigma_m = \frac{\sigma_{\max} + \sigma_{\min}}{2}$$

$$= \frac{300 - 150}{2} = 75 \text{ MN/m}^2$$

$$\sigma_a = \frac{\sigma_{\max} - \sigma_{\min}}{2} = \frac{300 + 150}{2}$$

$$= 225 \text{ MN/m}^2$$

Soderberg Relation.  $\frac{\sigma_m}{\sigma_y} + \frac{\sigma_a}{\sigma_{-1}} = \frac{1}{n}$

$$\frac{75}{0.55 \sigma_u} + \frac{225}{0.5 \sigma_u} = \frac{1}{2}$$

$$\frac{136.36}{\sigma_u} + \frac{450}{\sigma_u} = \frac{1}{2}$$

$$\sigma_u = 1172 \text{ MN/m}^2$$

Goodman Relation

$$\frac{\sigma_m}{\sigma_u} + \frac{\sigma_a}{\sigma_{-1}} = \frac{1}{n}$$

$$\frac{75}{\sigma_u} + \frac{225}{0.5 \sigma_u} = \frac{1}{2}$$

$$\sigma_u = 1050 \text{ MN/m}^2$$

Gerber Relationship

$$\frac{1}{n} = \left( \frac{\sigma_m}{\sigma_u} \right)^2 + \frac{\sigma_a}{\sigma_{-1}}$$

$$\left( \frac{75}{\sigma_u} \right)^2 \times 2 + \frac{225}{0.5 \sigma_u} = \frac{1}{2}$$

$$\frac{11250}{\sigma_u^2} + \frac{450}{\sigma_u} = \frac{1}{2}$$

$$2(11250 + 450 \sigma_u) = \sigma_u^2$$

$$22500 + 900 \sigma_u = \sigma_u^2$$

$$\sigma_u^2 - 900 \sigma_u - 22500 = 0$$

$$\sigma_u = 924 \text{ MN/m}^2$$

2. A cantilever beam of circular cross section is subjected to cyclic load varies from <sup>(bending moment)</sup>  $-50 \text{ N}$  to  $150 \text{ N}$ . Determine the diameter of rod by: i) Goodman relationship ii) Soderberg relationship. Use the following data.  
 Ultimate strength =  $550 \text{ MPa}$  Yield strength =  $320 \text{ MPa}$   
 Endurance limit =  $275 \text{ MPa}$ . Size correction factor =  $0.85$ . Surface correction factor =  $0.9$   
 Theoretical stress Concentration =  $1.4$ . Notch sensitivity factor =  $0.9$ . Factor of safety =  $2$ .

Soln :-

$$\sigma_u = 550 \text{ MPa}$$

$$\sigma_y = 320 \text{ MPa}$$

$$\sigma_{-1}' = 275 \text{ MPa}$$

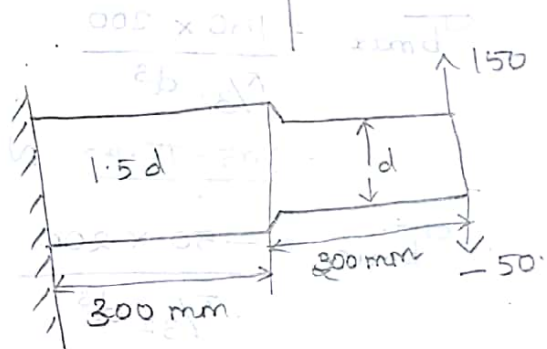
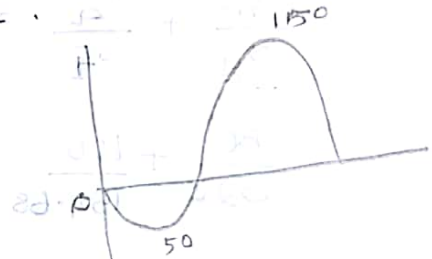
$$K_{sz} = 0.85$$

$$K_{SF} = 0.9$$

$$K_t = 1.4$$

$$q = 0.9$$

$$F_s = 2$$



$$\sigma_{-1} = \frac{\sigma_{-1}' \times K_L \times K_R \times K_{sz} \times K_{SF} \times K_t}{K_f}$$

$$K_f = 1 + q(K_t - 1)$$

$$= 1 + 0.9(1.4 - 1)$$

$$= 1.36$$

$$\sigma_{-1} = \frac{275 \times 1 \times 1 \times 0.85 \times 0.9}{1.36}$$

$$= 154.68 \text{ MPa} + \frac{m^2}{d^2} = \frac{1}{4}$$

$$\sigma_m = \frac{150 - 50}{2}$$

$$= 50 \text{ MPas}$$

$$\sigma_a = \frac{150 + 50}{2}$$

$$= 100 \text{ MPas}$$

Soderberg

$$\frac{\sigma_m}{\sigma_y} + \frac{\sigma_a}{\sigma_u} = \frac{1}{n}$$

$$\frac{50}{320} + \frac{100}{154.68}$$

$$\sigma_{bmax} = \frac{150 \times 200}{\pi/32 d^3}$$

$$= \frac{305577.45}{d^3} \text{ N/mm}^2$$

$$\sigma_{bmin} = \frac{-50 \times 200}{\pi/32 d^3}$$

$$= \frac{-101859.16}{d^3} \text{ N/mm}^2$$

$$\sigma_{mean} = \frac{\sigma_{bmax} + \sigma_{bmin}}{2} = \frac{101859.14}{d^3}$$

$$\sigma_a = \frac{\sigma_{max} - \sigma_{min}}{2} \cdot \frac{P+1}{P \cdot 0 + 1}$$

$$\sigma_a = \frac{203718.325}{d^3} \text{ N/mm}^2$$

Soderberg Relationship:

$$\frac{1}{n} = \frac{\sigma_m}{\sigma_y} + \frac{\sigma_a}{\sigma_u}$$



$$\Rightarrow \frac{1}{2} = \frac{\frac{101859 \cdot 14}{d^3}}{320} + \frac{\frac{203718 \cdot 325}{d^3}}{154 \cdot 69}$$

$$\frac{1}{2} = \frac{318 \cdot 3}{d^3} + \frac{1316 \cdot 9}{d^3}$$

$$d^3 = 3270 \cdot 49$$

$$d = 14.84 \text{ mm}$$

$$\frac{1}{n} = \frac{\sigma_m}{\sigma_u} + \frac{\sigma_a}{\sigma_{-1}}$$

$$\frac{1}{2} = \frac{\frac{101858 \cdot 9}{d^3}}{550} + \frac{\frac{203718 \cdot 325}{d^3}}{154 \cdot 69}$$

$$d^3 = 3004 \cdot 276$$

$$d = 14.42 \text{ mm}$$

The shaft subjected to bending moment varies from -200 Nm to 500 Nm and twisting moment varying from 50 Nm to 175 Nm. The material used is  $\sigma_u = 600 \text{ MPa}$ ; Endurance limit = 300 MPa, Size correction factor = 0.76, Surface finish factor = 0.8, Load factor = 0.897, Stress concentration factor = 1.85, Non sensitive factor = 0.95. Find diameter of shaft by using Vonmises Herze Theory. FOS = 1.5.



$$M_{bmax} = 500 \text{ N}\cdot\text{m}$$

$$M_{bmin} = -200 \text{ N}\cdot\text{m}$$

$$T_{max} = 175 \text{ N}\cdot\text{m}$$

$$T_{min} = 50 \text{ N}\cdot\text{m}$$

$$\begin{aligned} \sigma_{bmax} &= \frac{500 \times 10^3}{\frac{\pi}{32} d^3} \\ &= \frac{5.093 \times 10^6}{d^3} \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \sigma_{bmin} &= \frac{-200 \times 10^3}{\frac{\pi}{32} d^3} \\ &= \frac{-2.037 \times 10^6}{d^3} \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \sigma_{-1} &= \frac{\sigma_{-1}' \times k_L \times k_K \times k_{SF} \times k_{SZ}}{k_F} \\ &= \frac{300 \times 1 \times 0.897 \times 0.76 \times 0.85}{1 + 0.95(1.85 - 1)} \end{aligned}$$

$$= 96.20 \text{ MPa}$$

$$\sigma_{mean} = \frac{\sigma_{max} + \sigma_{min}}{2}$$

$$= \frac{1.528 \times 10^6}{d^3} \text{ N/mm}^2$$

$$\sigma_{eq} = \frac{\sigma_m + \sigma_a \sigma_y}{\sigma_{-1}}$$

$$= \frac{1.52}{d^3} + \frac{3.56}{d^3} \times 400$$

$$95.45$$

Assume  $\sigma_y = 400$

$$\sigma_{eq} = \frac{16 \cdot 43}{d^3} \text{ N/mm}^2.$$

$$\tau_{max} = \frac{16 T_{max}}{\pi d^3}$$

$$= \frac{16 \times 175 \times 10^3}{\pi d^3}$$

$$= \frac{8.91 \times 10^5}{d^3} \text{ N/mm}^2.$$

$$\tau_{min} = \frac{16 T_{min}}{\pi d^3}$$

$$= \frac{2.54 \times 10^5}{d^3} \text{ N/mm}^2.$$

$$\tau_{mean} = \frac{\tau_{max} - \tau_{min}}{2}$$

$$= \frac{3.18 \times 10^5}{d^3} \text{ N/mm}^2$$

$$\tau_{eq} = \tau_m + \frac{\tau_a \tau_y}{\tau_1}$$

$$= \frac{5.72 \times 10^5}{d^3} + \frac{3.18 \times 10^5}{d^3} \times \boxed{240}$$

$$95.45$$

$$= \frac{13.71 \times 10^5}{d^3} \text{ N/mm}^2.$$

$$= \frac{1.371 \times 10^6}{d^3} \text{ N/mm}^2$$

$$\tau_1 = \sigma_{-1}$$

$$\tau_y = 0.6 \sigma_y$$

$$= 400 \times 0.6$$

$$= 240$$

$$\sigma_1 = \frac{1}{2} \left[ \sigma_{eq} + \sqrt{(\sigma_{eq})^2 + 4(\tau_{eq})^2} \right]$$

$$\sigma_1 = \frac{1368.0 \times 10^3}{d^3}$$

$$\frac{1368 \times 10^3}{d^3} = 400$$

$$d^3 = 3420.02$$

$$d = 15.067 \text{ mm}$$

$$\frac{10 \times 10^3 \times 10}{\epsilon_b} = \dots$$

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- 1-0 = 1J
- 2-0 = 2J
- 3-0 = 3J
- 4-0 = 4J

$$\frac{10 \times 10^3 \times 10}{\epsilon_b} = \dots$$

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