



**SNS College of Technology(Autonomous)
Coimbatore-35
Academic Year 2023 – 2024 (Even)**



UNIT 2 QUANTITATIVE ABILITY IV

T2: BASE CONVERSION

Many number systems are in use in digital technology. The most common are :

- Decimal (Base 10)
- Binary (Base 2)
- Octal (Base 8)
- Hexadecimal (Base 16)
- The decimal system is the number system that we use everyday

Decimal system uses 10 symbols (digits) 0, 1, 2, 3, 4, 5, 6, 7, 8, 9

- Octal System uses eight symbols 0, 1, 2, 3, 4, 5, 6, 7
- Binary System uses only two symbols 0 and 1
- Hexadecimal System uses sixteen symbols 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F to represent any number, no matter how large or how small.

Introduction

- Many number systems are in use in digital technology. The most common are :
 - ▮ Decimal (Base 10)
 - ▮ Binary (Base 2)
 - ▮ Octal (Base 8)
 - ▮ Hexadecimal (Base 16)
- The *decimal system* is the number system that we use everyday

Number System

- **Decimal system** uses 10 symbols (*digits*)
0, 1, 2, 3, 4, 5, 6, 7, 8, 9
- **Octal System** uses eight symbols
0, 1, 2, 3, 4, 5, 6, 7
- **Binary System** uses only two symbols
0 and 1
- **Hexadecimal System** uses sixteen symbols
0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F

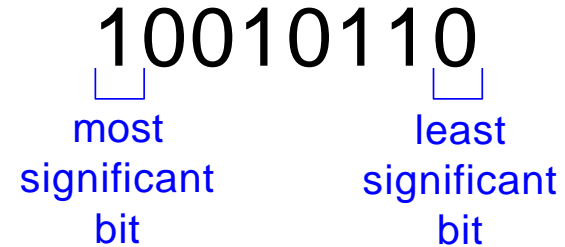
to represent any number, no matter how large or how small.

Familiar System

Octal System (Base – 8 ns)	Hexa decimal Number System (Base – 16)	Decimal Number (Base-10)	Binary Equivalent (Base-2)	Base 4 number System (Base -4)
0	0	0	0	0
1	1	1	1	1
2	2	2	10	2
3	3	3	11	3
4	4	4	100	10
5	5	5	101	11
6	6	6	110	12
7	7	7	111	13
10	8	8	1000	20
11	9	9	1001	21
12	A	10	1010	22
13	B	11	1011	23
14	C	12	1100	30
15	D	13	1101	31
16	E	14	1110	32
17	F	15	1111	33

Bits, Bytes, Nibbles

- Bits (b)



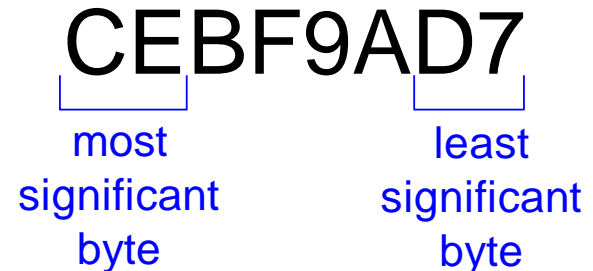
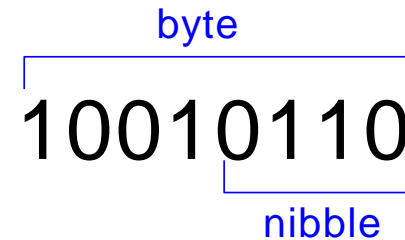
- Bytes & Nibbles

- ▮ Byte (B) = 8 bits

- Used everyday

- ▮ Nibble (N) = 4 bits

- Not commonly used



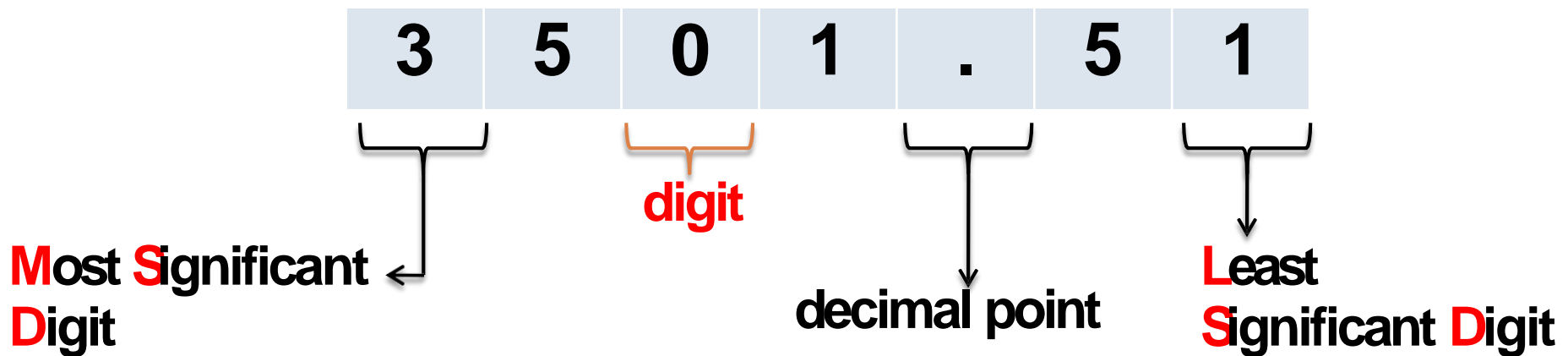
KB, MB, GB

...

- In computer, the basic unit is byte (B)
- And, we use KB, MB, GB many many many times
 - ▮ $2^{10} = 1024 =$ **1KB (kilobyte)**
 - ▮ $2^{20} = 1024 \times 1024 =$ **1MB (megabyte)**
 - ▮ $2^{30} = 1024 \times 1024 \times 1024 =$ **1GB (gigabyte)**
- How about these?
 - ▮ $2^{40} =$ **1TB (terabyte)**
 - ▮ $2^{50} =$ **1PB (petabyte)**
 - ▮ $2^{60} =$ **1EB (exabyte)**
 - ▮ $2^{70} =$ **1ZB (zettabyte)**
 - ▮ ...

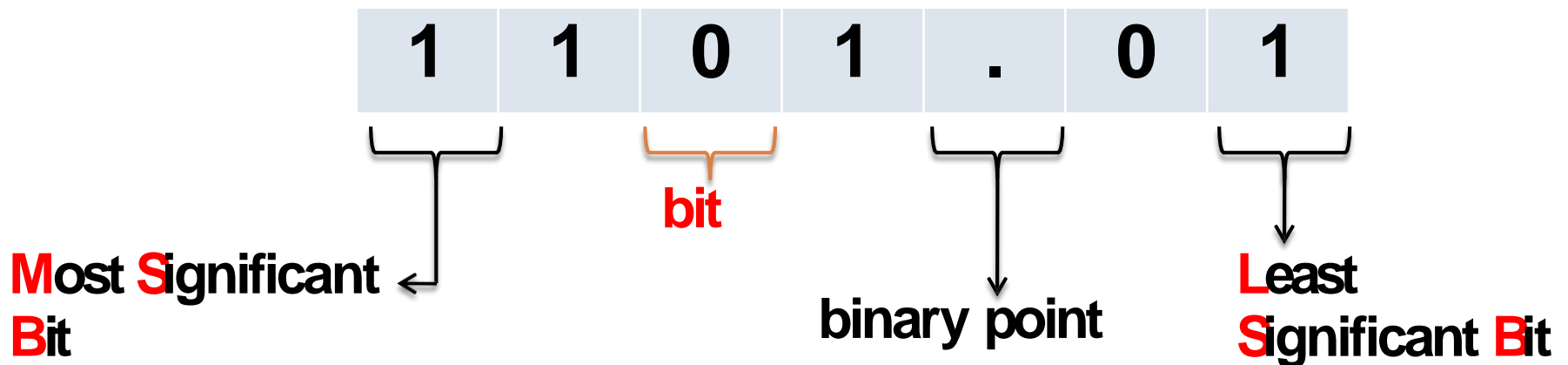
Decimal System

- The **decimal system** is composed of 10 numerals or symbols. These 10 symbols are 0,1,2,3,4,5,6,7,8,9; using these symbols as digits of a number, we can express any quantity.
- **Example : 3501.51**



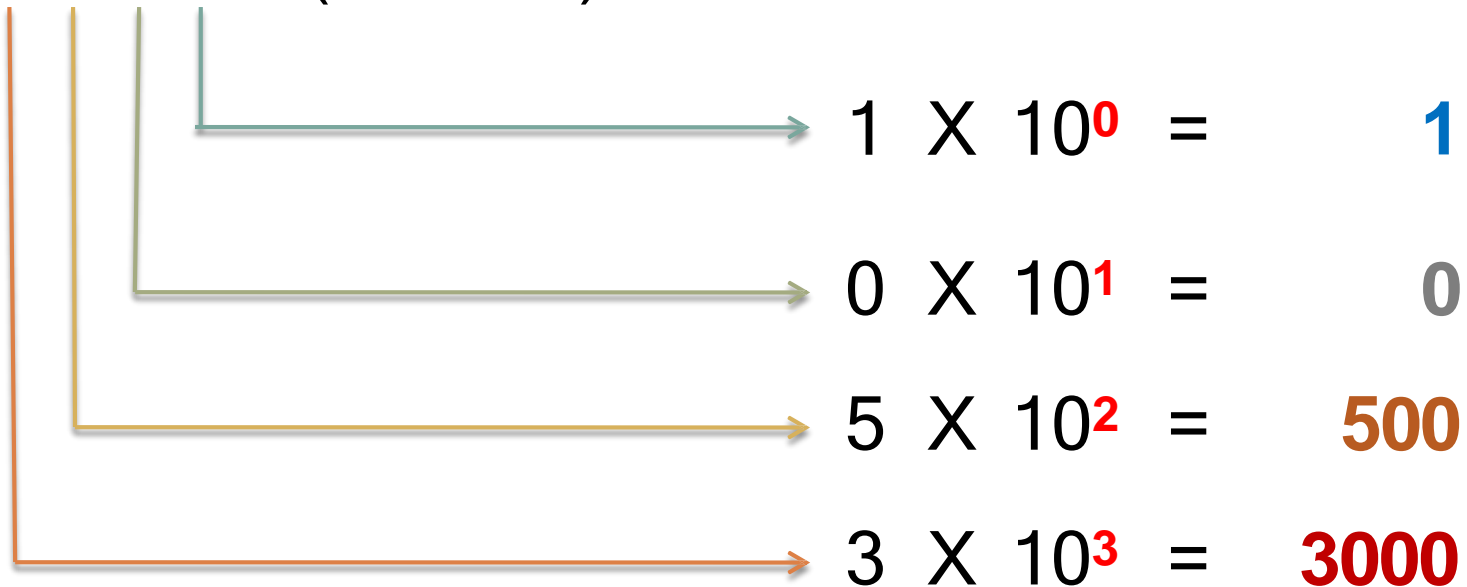
Binary System

- The **binary system** is composed of 2 numerals or symbols 0 and 1; using these symbols as digits of a number, we can express any quantity.
- **Example : 1101.01**



Decimal Number Quantity (positional number)

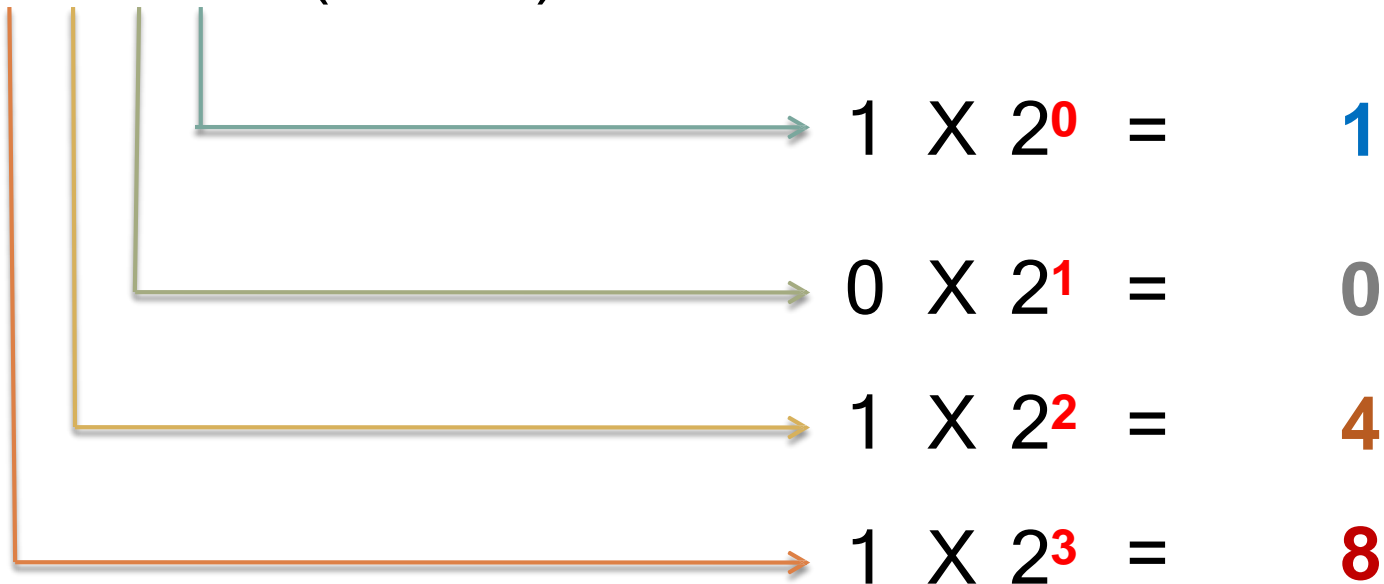
□ 3 5 0 1 (base-10)



$$3000 + 500 + 0 + 1 = 3501$$

Binary-to-Decimal Conversion

□ 1 1 0 1 (base-2)

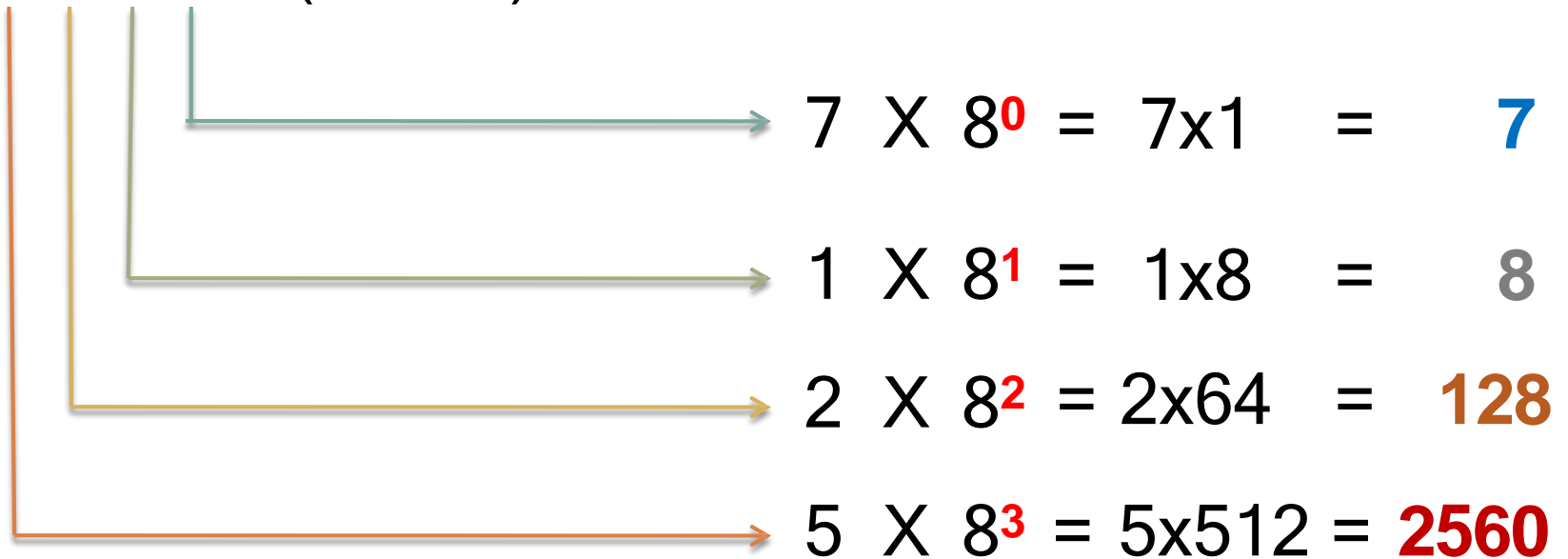


$$8 + 4 + 0 + 1 = 13$$

$$1101_2 = 13_{10}$$

Octal-to-Decimal Conversion

□ 5 2 1 7 (base-8)

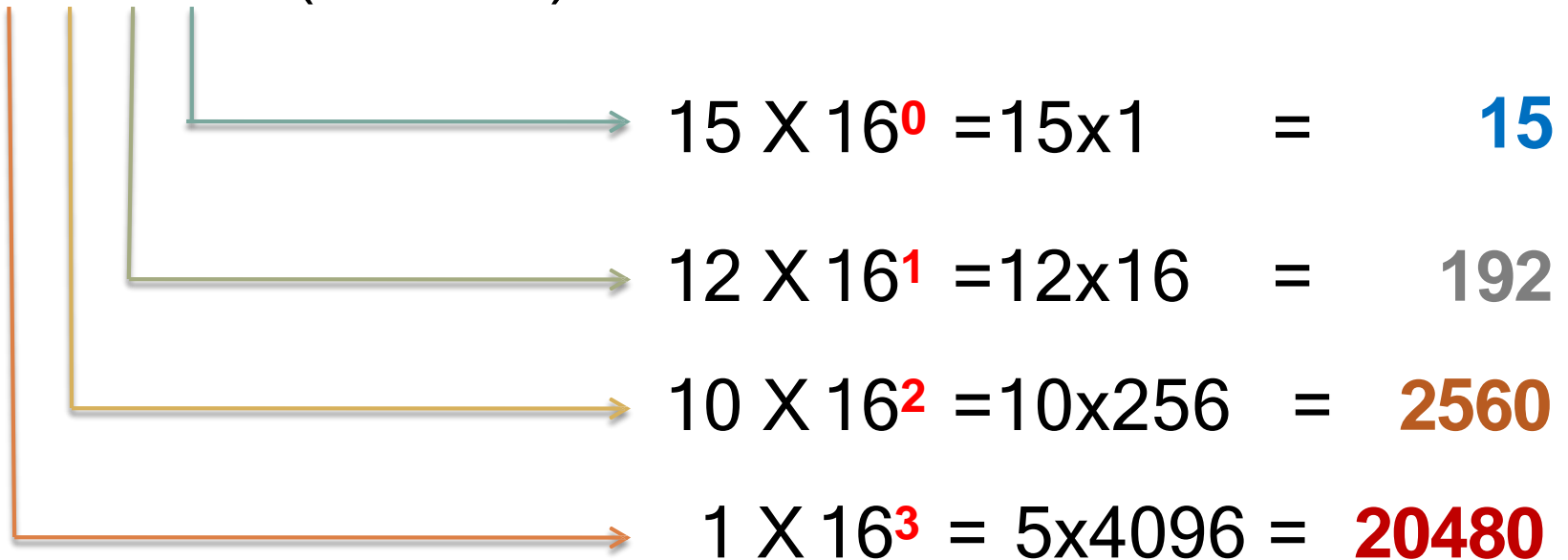


$$2560 + 128 + 8 + 7 = 2703$$

$$5217_8 = 2703_{10}$$

Hexadecimal-to-Decimal Conversion

□ 1 A C F (base-16) [A = 10, B = 11, C = 12, D = 13, E = 14, F = 15]

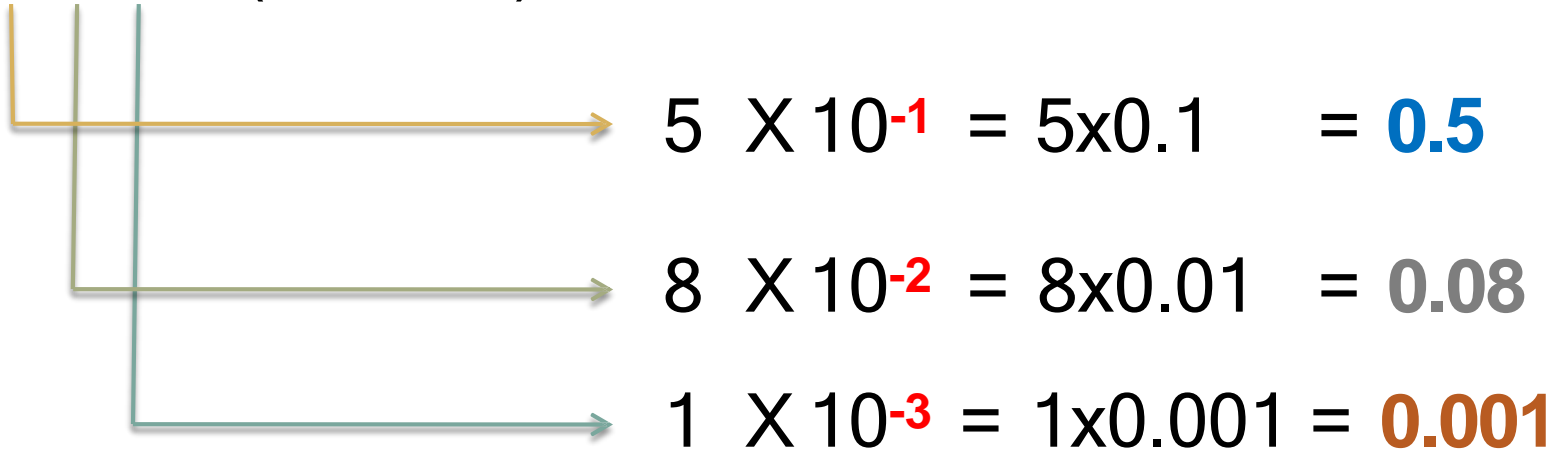


$$20480 + 2560 + 192 + 15 = 23247$$

$$1ACF_{16} = 23247_{10}$$

Decimal Number Quantity (fractional number)

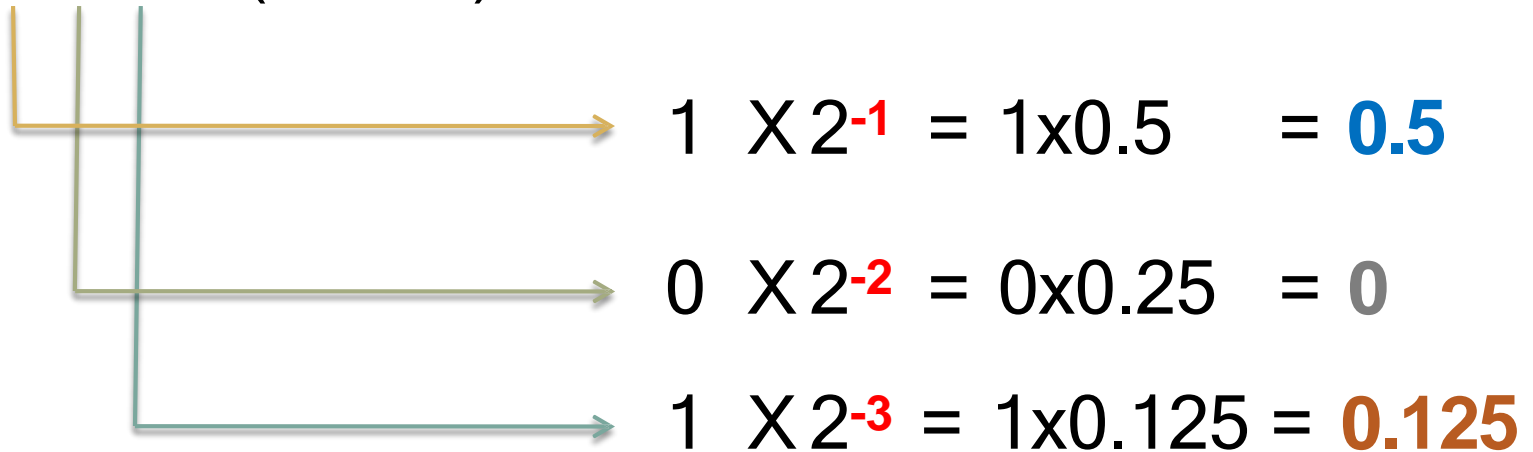
□ . 5 8 1 (base-10)



$$0.5 + 0.08 + 0.001 = 0.581$$

Binary-to-Decimal Conversion

□ . 1 0 1 (base-2)



$$0.5 + 0 + 0.125 = 0.625$$

$$0.101_2 = 0.625_{10}$$

Octal-to-Decimal Conversion

□ . 2 5 (base-8)

$2 \times 8^{-1} = 2 \times 0.125 = 0.25$

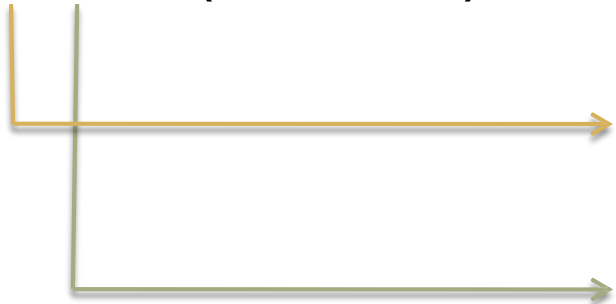
$5 \times 8^{-2} = 5 \times 0.015625 = 0.017825$

$$0.25 + 0.017825 = 0.267825$$

$$0.25_8 = 0.267825_{10}$$

Hexadecimal-to-Decimal Conversion

□ . F5 (base-16)



$$15 \times 16^{-1} = 15 \times 0.0625 = \mathbf{0.9375}$$

$$5 \times 16^{-2} = 5 \times 0.00390625 = \mathbf{0.01953125}$$

$$0.9375 + 0.01953125 = 0.95703125$$

$$0.F5_{16} = 0.95703125_{10}$$

Exercise

1

- Convert these binary system numbers to decimal system numbers

a) 100101101

b) 11100.1001

c) 111111

d) 100000.0111

- b)

$$1x2^4 + 1x2^3 + 1x2^2 + 0x2^1 + 0x2^0 + 1x2^{-1} + 0x2^{-2} + 0x2^{-3} + 1x2^{-4}$$

$$= 16 + 8 + 4 + 0 + 0 + 0.5 + 0 + 0 + 0.0625$$

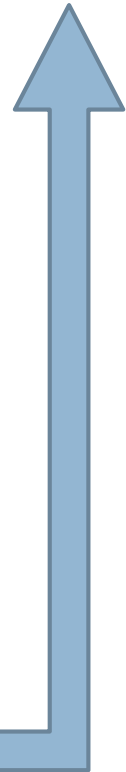
$$= 28.5625$$

Decimal-to-Binary Conversion (positional number)

□ 250

$$250_{10} = 11111010_2$$

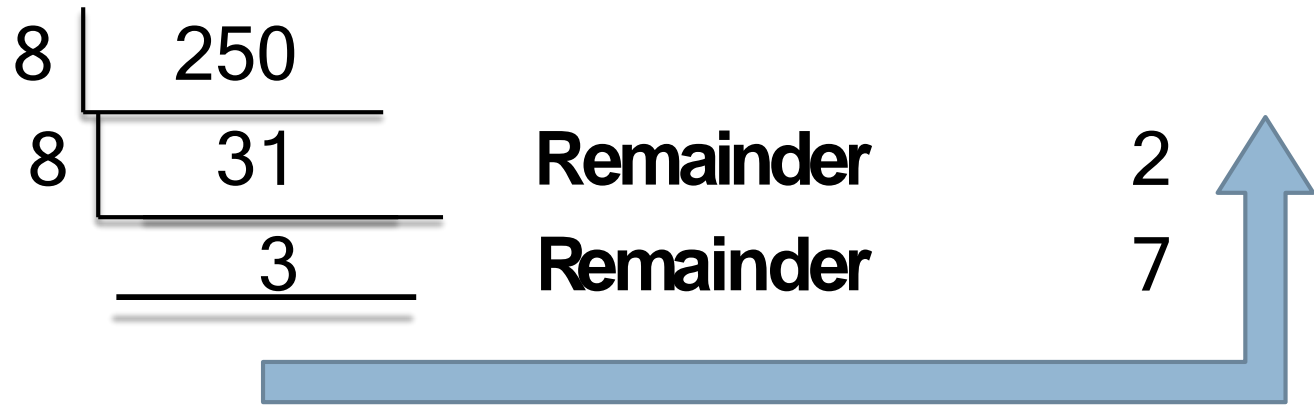
2	250		
2	125	Remainder	0
2	62	r	1
2	31	Remainder	0
2	15	Remainder	1
2	7	Remainder	1
2	3	Remainder	1
	1	Remainder	1



Remainder

Decimal-to-Octal Conversion

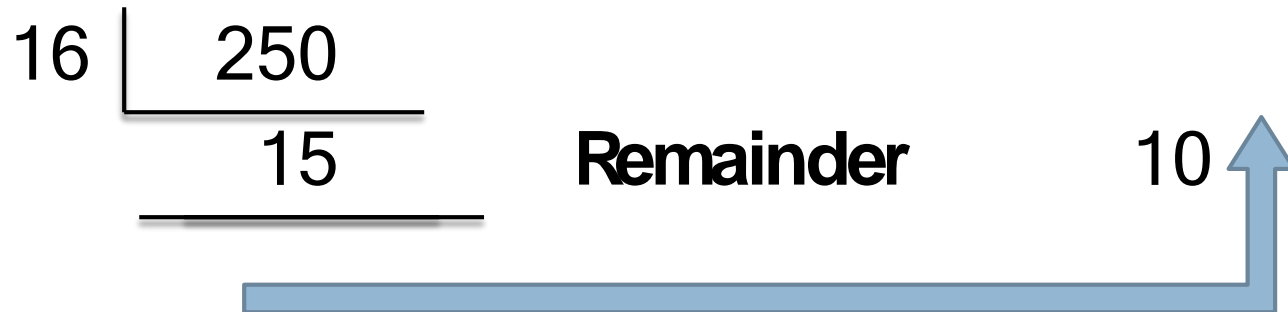
□ 250



$$250_{10} = 372_8$$

Decimal-to-Hexadecimal Conversion

□ 250



$$\begin{aligned} 250_{10} &= 15 \ 10_{16} \ ? \\ &= \mathbf{FA}_{16} \end{aligned}$$

Decimal-to-Binary Conversion (fractional number)

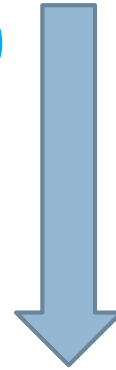
□ 0 . 4375

$$0.4375 \times 2 = 0.8750$$

$$0.8750 \times 2 = 1.75$$

$$0.75 \times 2 = 1.5$$

$$0.5 \times 2 = 1.0$$



$$0.4375_{10} = 0.0111_2$$

Decimal-to-Octal Conversion

□ 0.4375

$$\begin{array}{rcl} 0.4375 \times 8 & = & 3.5 \\ 0.5 \quad \times 8 & = & 4.0 \end{array} \quad \downarrow$$

$$0.4375_{10} = 0.34_8$$

Decimal-to-Hexadecimal Conversion

□ 0 . 4375

$$0.4375 \times 16 = 7.0$$


$$0.4375_{10} = 0.7_{16}$$

Example :Decimal-to-Binary Conversion (Estimation)

□ 0.782

$$0.782 \times 2 = 1.564$$

$$0.564 \times 2 = 1.128$$

$$0.128 \times 2 = 0.256$$

$$0.256 \times 2 = 0.512$$

$$0.512 \times 2 = 1.024$$

$$0.024 \times 2 = 0.048$$

$$0.048 \times 2 = 0.096$$

$$0.192 \times 2 = 0.384$$

$$0.384 \times 2 = 0.768$$

$$0.768 \times 2 = 1.536$$

$$\begin{aligned} 11001_2 &\rightarrow 2^{-1} + 2^{-2} + 2^{-5} \\ &\rightarrow 0.5 + 0.25 + 0.03125 \\ &\rightarrow \mathbf{0.78125} \end{aligned}$$

$$\begin{aligned} 1100100001_2 &\rightarrow 2^{-1} + 2^{-2} + 2^{-5} + 2^{-10} \\ &\rightarrow 0.5 + 0.25 + 0.03125 + \\ &\quad 0.0009765625 \\ &\rightarrow \mathbf{0.7822265625} \end{aligned}$$

Exercise

2

- Convert these decimal system numbers to binary system numbers

a) 127

b) 38

c) 22.5

d) 764.375

$$c) (22.5)_{10} = (?)_2$$

2	22	
	<u>11</u>	0
2	5	1
	<u>2</u>	1
	1	0

$$0.5 \times 2 = 1.0$$

$$\Rightarrow (22.5)_{10} = (10110.1)_2$$