



Ampere's circuital Law



Ampere's Circuital Law:

Ampere's circuital law states that the line integral of the magnetic field \vec{H} (circulation of H) around a closed path is the net current enclosed by this path. Mathematically,

$$\oint \vec{H} \cdot d\vec{l} = I_{enc}$$

The total current I_{enc} can be written as,

$$I_{enc} = \int_S \vec{J} \cdot d\vec{s}$$

By applying Stoke's theorem, we can write

$$\begin{aligned} \oint \vec{H} \cdot d\vec{l} &= \int_S \nabla \times \vec{H} \cdot d\vec{s} \\ \therefore \int_S \nabla \times \vec{H} \cdot d\vec{s} &= \int_S \vec{J} \cdot d\vec{s} \\ \therefore \nabla \times \vec{H} &= \vec{J} \end{aligned}$$

which is the Ampere's law in the point form.