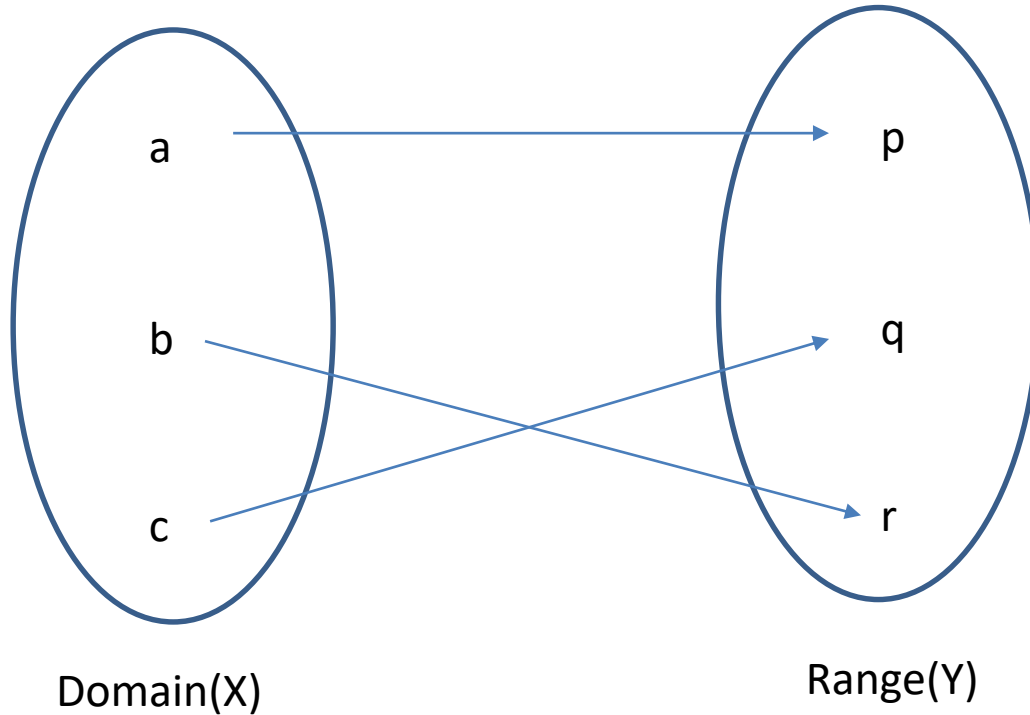


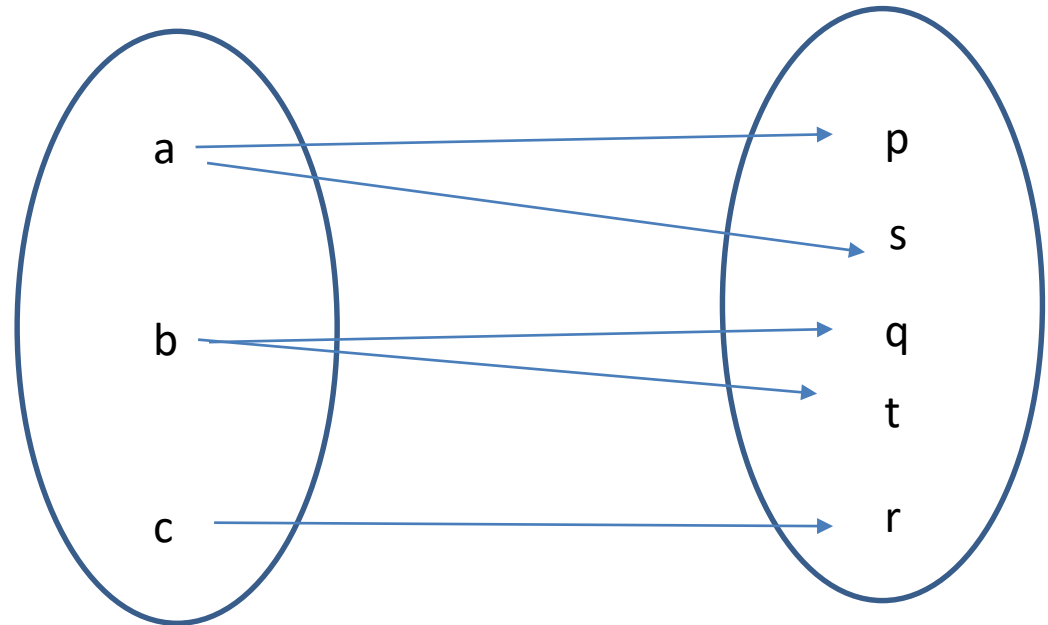


## Multi Valued Dependencies and Fourth Normal Form

**COURSE** : 23CAT- Database Management System  
**UNIT III** : Database Design  
**CLASS** : I Semester / I MCA



- **Domain** is a set of all possible values of X
- **Range** is a set of all possible values of Y





- ❑ Multivalued dependency would occur whenever two separate attributes in a given table happen to be independent of each other.
- ❑ And yet, both of these depend on another third attribute.
- ❑ The multivalued dependency contains at least two of the attributes dependent on the third attribute.
- ❑ It is represented by  $x \twoheadrightarrow y$

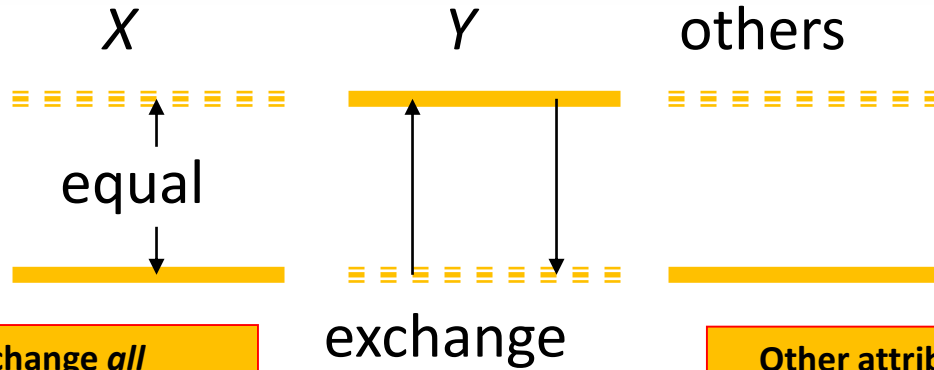
for some single value of the attribute 'x', multiple values of attribute 'y' can exist.



- ❑ Multi-valued dependencies (MVDs) express a condition among tuples of a relation that exists when the table (relation) is trying to represent
  - more than one many-many relationship.
  - then certain columns (attributes) become independent of one another
  - and their values must appear in all combinations.



- A multi-valued dependency (MVD)  $X \twoheadrightarrow Y$  :
  - if an assertion that if two rows of a table agree on all the attributes of X,
  - then their components may be swapped in the set of attributes Y,
  - and the result will be two tuples that are also in the relation



We must exchange *all* components of Ys (not just some)

Other attributes get copied remain the same

If there is an FD  $X \rightarrow Y$ , then swapping Ys components doesn't change anything.



Every FD is an MVD.





- ❑ A relation R is in 4NF if whenever  $X \twoheadrightarrow Y$  is a nontrivial MVD, then X is a superkey.
  - Nontrivial means that:
    1. Y is not a subset of X  
(swapping components does not change tuples)
    2. X and Y are not, together, all the attributes.  
(swapping components yields the same tuples)
- ❑ Note that the definition of “superkey” still depends on FDs only.

1.It should be in BCNF.  
2.There should be no Multi-valued Dependency





- ❑ A relation R is in 4NF if whenever  $X \twoheadrightarrow Y$  is a nontrivial MVD, then X is a superkey.
  - Nontrivial means that:
    1. Y is not a subset of X  
(swapping components does not change tuples)
    2. X and Y are not, together, all the attributes.  
(swapping components yields the same tuples)
- ❑ Note that the definition of “superkey” still depends on FDs only.

1.It should be in BCNF.  
2.There should be no Multi-valued Dependency



- ❑ Remember that
  - Every FD  $X \rightarrow Y$  is also an MVD,  $X \twoheadrightarrow Y$ .
- ❑ Thus, if R is in 4NF, it is certainly in BCNF.
  - Because any BCNF violation is a 4NF violation.
- ❑ However, R could be in BCNF and not 4NF, because MVDs are “invisible” to BCNF.



- ❑ Customers(name, addr, phones, sodasLiked)
  - FD: name  $\rightarrow$  addr
  - MVDs: name  $\rightarrow\rightarrow$  phones, name  $\rightarrow\rightarrow$  sodasLiked
  
- ❑ Key is {name, phones, sodasLiked}.
  
- ❑ All dependencies violate 4NF because name is not a superkey.



- ❑ Decompose using name  $\rightarrow$  addr:
  1. Customers1(name, addr)
    - In 4NF, only dependency is name  $\rightarrow$  addr.
  2. Customers2(name, phones, sodasLiked)
    - Not in 4NF because MVDs
      - name  $\rightarrow\rightarrow$  phones and name  $\rightarrow\rightarrow$  sodasLiked apply.
    - No FD's, so all three attributes form the key.



### Recall

- Customers2(name, phones, sodasLiked)

### Either MVD

- name  $\rightarrow\rightarrow$  phones
- name  $\rightarrow\rightarrow$  sodasLiked

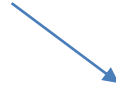
### tells us to decompose to:

- Customers3(name, phones)
- Customers4(name, sodasLiked)



### ❑ 4th Normal Form Consists of:

- Customers1(name, addr)
  - Contact
- Customers3(name, phones)
  - Phone
- Customers4(name, sodasLiked)
  - Likes



5

### ❑ The following FD and MVDs are satisfied:

❑ FD:            name → addr

❑ MVDs:        name →→ phones

name →→ sodasLiked



# Boyce – Codd Normal Form (BCNF)

- ❑ Developed in 1974 by Raymond F.Boyce and Edgar F.Codd
- ❑ BCNF is a stricter form of 3NF
- ❑ It applies to tables with more than one candidate key
- ❑ A relation is in BCNF if every determinant in the table is a candidate key.  
I.e LHS is super key
- ❑ If a table contains single candidate key, the 3NF and BCNF are equivalent









□

□





