



# SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution)



COIMBATORE-35

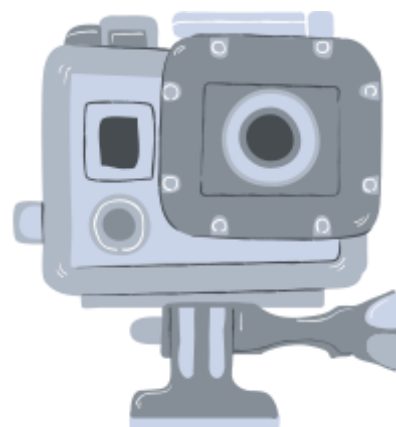
Accredited by NBA-AICTE and Accredited by NAAC – UGC with A+ Grade  
Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRICAL & ELECTRONICS ENGINEERING

UNIT 2

## Network Modelling

19EET302 – Power System 1  
III year / V Semester





# INTRODUCTION

---

## *Bus Frame Analysis*

FORMATION OF Y BUS AND Z BUS

1. Rule of Inspection
2. Singular Transformation
3. Non-Singular Transformation
4. ZBUS Building Algorithms, etc



# Frames of Reference



**Bus Frame of Reference:** There are  $b$  independent equations ( $b = \text{no. of buses}$ ) relating the bus vectors of currents and voltages through the bus impedance matrix and bus admittance matrix:

$$V_{BUS} = Z_{BUS} I_{BUS}$$

$$I_{BUS} = Y_{BUS} V_{BUS}$$

**Branch Frame of Reference:** There are  $b$  independent equations ( $b = \text{no. of branches of a selected Tree sub-graph of the system Graph}$ )

$$V_{BR} = Z_{BR} I_{BR}$$

$$I_{BR} = Y_{BR} V_{BR}$$

**Loop Frame of Reference:** There are  $b$  independent equations ( $b = \text{no. of branches of a selected Tree sub-graph of the system Graph}$ )

$$V_{LOOP} = Z_{LOOP} I_{LOOP}$$

$$I_{LOOP} = Y_{LOOP} V_{LOOP}$$

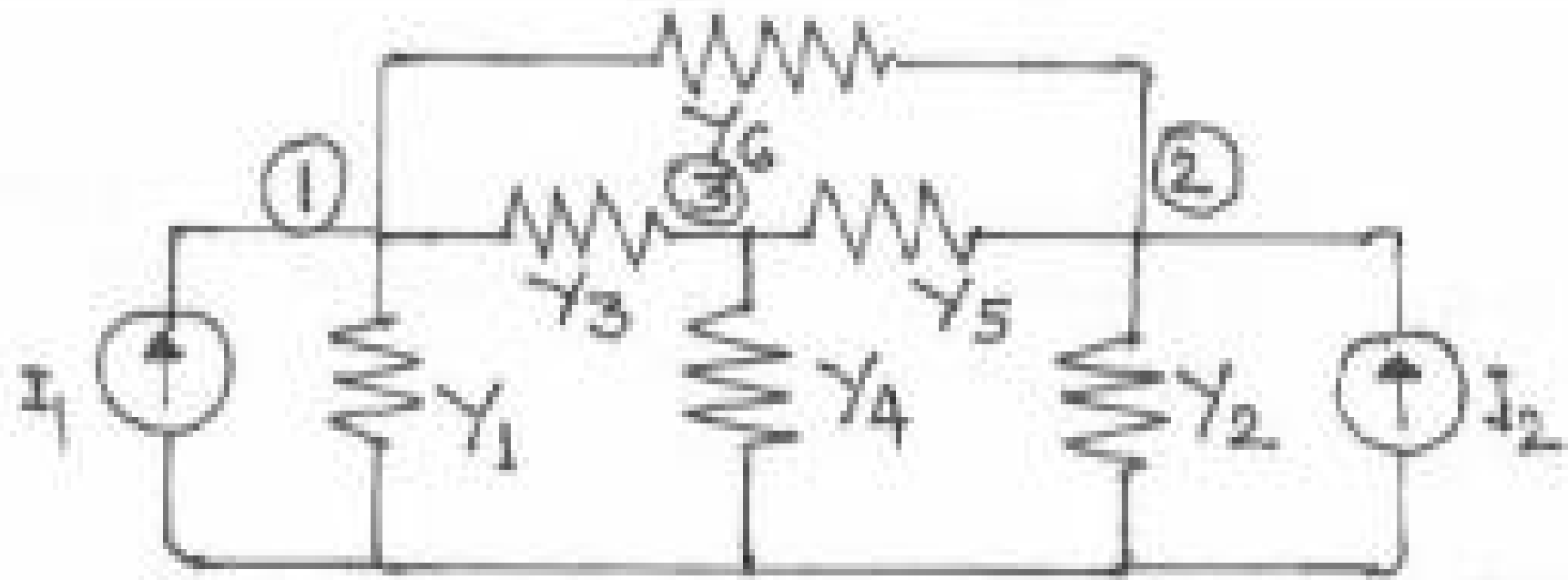
Of the various network matrices referred above,

the bus admittance matrix ( $Y_{BUS}$ ) and the bus impedance matrix ( $Z_{BUS}$ ) are determined for a given power system



# Rule of Inspection -Inspection Method

Consider the 3-node admittance network as shown in figure 5. Using the basic branch relation:  $I = (YV)$ , for all the elemental currents and applying Kirchhoff's Current Law principle at the nodal points, we get the relations as under:



$$\text{At node 1: } I_1 = Y_1 V_1 + Y_3 (V_1 - V_3) + Y_6 (V_1 - V_2)$$

$$\text{At node 2: } I_2 = Y_2 V_2 + Y_5 (V_2 - V_3) + Y_6 (V_2 - V_1)$$

$$\text{At node 3: } 0 = Y_3 (V_3 - V_1) + Y_4 V_3 + Y_5 (V_3 - V_2)$$





# Inspection Method



$$\begin{bmatrix} I_1 \\ I_2 \\ 0 \end{bmatrix} = \begin{bmatrix} (Y_1+Y_3+Y_6) & -Y_6 & -Y_3 \\ -Y_6 & (Y_2+Y_5+Y_6) & -Y_5 \\ -Y_3 & -Y_5 & (Y_3+Y_4+Y_5) \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix}$$

$$IBUS = YBUS VBUS$$

Where, YBUS is the bus admittance matrix, IBUS & VBUS are the bus current and bus voltage vectors respectively.

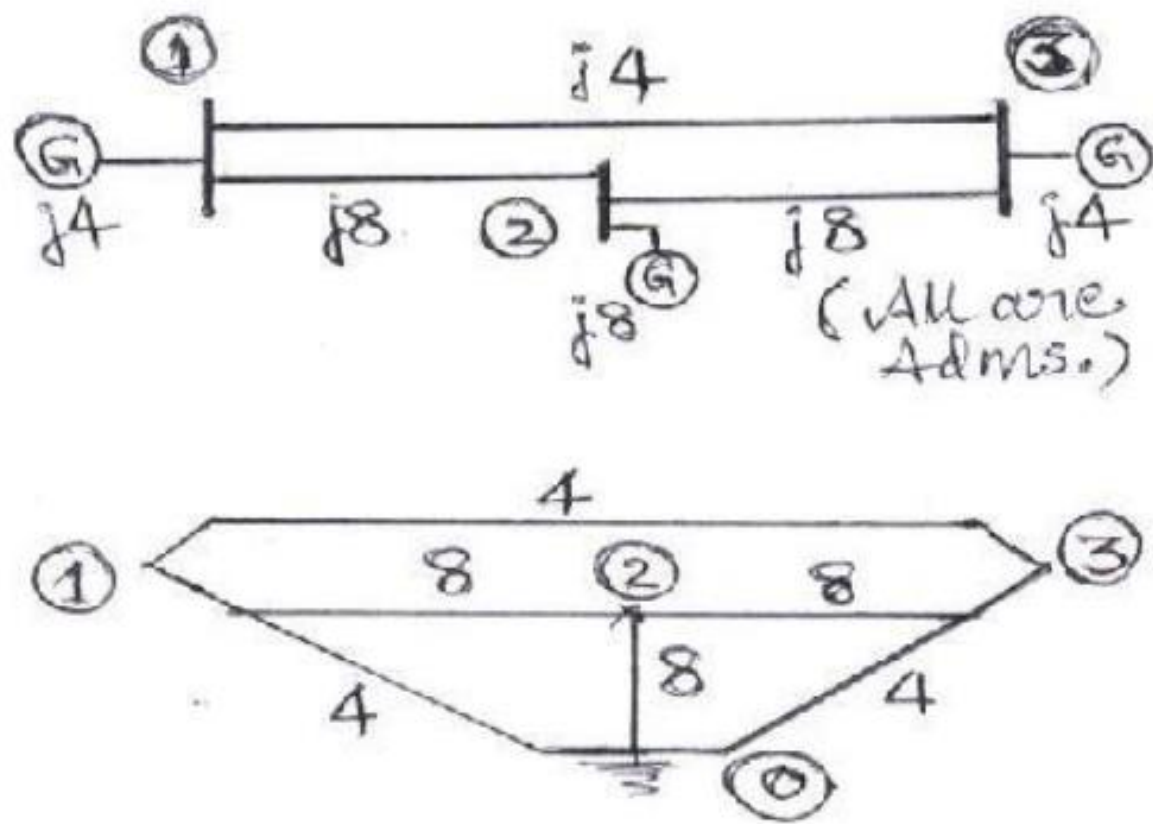
**Diagonal elements:** A diagonal element ( $Y_{ii}$ ) of the bus admittance matrix, YBUS, is equal to the sum total of the admittance values of all the elements incident at the bus/node  $i$ ,

**Off Diagonal elements:** An off-diagonal element ( $Y_{ij}$ ) of the bus admittance matrix, YBUS, is equal to the negative of the admittance value of the connecting element present between the buses  $i$  and  $j$ , if any.



# Problem 1

- Obtain the bus admittance matrix for the admittance network shown aside by the rule of inspection



$$Y_{BUS} = \begin{vmatrix} 16 & -8 & -4 \\ -8 & 24 & -8 \\ -4 & -8 & 16 \end{vmatrix}$$



# Summary

---



## Activity



**KEEP  
LEARNING..  
Thank u**

SEE YOU IN NEXT CLASS