

TURBINES

Hydraulic machines are defined as those machines which convert either hydraulic energy (energy possessed by water) into mechanical energy (which is further converted into electrical energy) or mechanical energy into hydraulic energy. The hydraulic machines, which convert the hydraulic energy into mechanical energy, are called turbines while the hydraulic machines which convert the mechanical energy into hydraulic energy. The study of hydraulic machines consists of turbines and pumps.

Turbines are defined as the hydraulic machines which convert hydraulic energy into mechanical energy. This, mechanical energy is used in running an electric generator which is directly coupled to the shaft of the turbine. Thus the mechanical energy is converted into electrical energy. The electric power which is obtained from the hydraulic energy (energy of water) is known as Hydroelectric power. At present the generation of hydroelectric power is the cheapest as compared by the power generated by other sources such as oil, coal etc.

General Layout of a Hydroelectric Power Plant

1. A dam constructed across a river to store water.
2. Pipes of large diameters called penstocks, which carry water under pressure from the storage reservoir to the turbines. These pipes are made of steel or reinforced concrete.
3. Turbines having different types of vanes fitted to the wheels.
4. Tail race, which is a channel which carries water away from the turbines after the water has worked on the turbines. The surface of water in the tail race channel is also known as tail race.

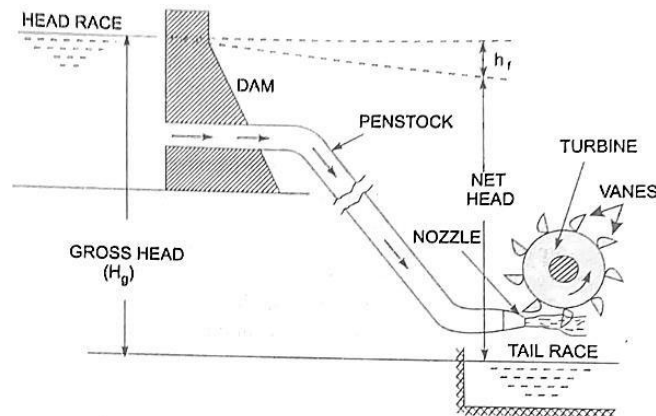


Fig. Layout of hydroelectric power plant

Definitions of Heads and Efficiencies of a Turbine

1. Gross Head. The difference between the head race level and tail race level when no water is flowing is known as Gross Head. It is denoted by 'H_g'.
2. Net Head. It is also called effective head and is defined as the head available at the inlet of the turbine, when water is flowing from head race to the turbine, a loss of head due to friction between water and penstock occurs. Though there are other losses also such as loss due to bend, Pipes, fittings, loss at the entrance of penstock etc., yet they are having small magnitude as compared to head loss due to friction. In 'h_f' is the head loss due to friction between penstocks and water then net head on turbine is given by

$$H = H_g - h_f$$

where H_g = Gross head, $h_f = \frac{4 \times f \times L \times V^2}{D \times 2g}$,

in which

V = Velocity of flow in penstock,

L = Length of penstock,

D = Diameter of penstock.

Efficiencies of a Turbine.

(a) **Hydraulic Efficiency (η_h).**

$$\eta_h = \frac{\text{Power delivered to runner}}{\text{Power supplied at inlet}} = \frac{\text{R.P.}}{\text{W.P.}}$$

Power supplied at the inlet of turbine in S.I. units is known as water power. It is given by

$$\text{W.P.} = \frac{\rho \times g \times Q \times H}{1000} \text{ kW}$$

R.P. = Power delivered to runner *i.e.*, runner power

$$= \frac{W [V_{w_1} \pm V_{w_2}] \times u}{g \times 1000} \text{ kW} \quad \dots \text{for Pelton Turbine}$$

$$= \frac{W [V_{w_1} u_1 \pm V_{w_2} u_2]}{g \times 1000} \text{ kW} \quad \dots \text{for a radial flow turbine}$$

(b) **Mechanical Efficiency (η_m).**

$$\eta_m = \frac{\text{Power at the shaft of the turbine}}{\text{Power delivered by water to the runner}} = \frac{\text{S.P.}}{\text{R.P.}}$$

(c) **Volumetric Efficiency (η_v).**

$$\eta_v = \frac{\text{Volume of water actually striking the runner}}{\text{Volume of water supplied to the turbine}}$$

(d) **Overall Efficiency (η_o).**

$$\eta_o = \frac{\text{Volume available at the shaft of the turbine}}{\text{Power supplied at the inlet of the turbine}} = \frac{\text{Shaft power}}{\text{Water power}}$$

$$= \frac{\text{S.P.}}{\text{W.P.}}$$

$$= \eta_m \times \eta_h$$

CLASSIFICATION OF HYDRAULIC TURBINES

1. According to the type of energy at inlet :
 - (a) Impulse turbine, and (b) Reaction turbine.
2. According to the direction of flow through runner :
 - (a) Tangential flow turbine, (b) Radial flow turbine,
 - (c) Axial flow turbine, and (d) Mixed flow turbine.
3. According to the head at the inlet of turbine :
 - (a) High head turbine, (b) Medium head turbine, and
 - (c) Low head turbine.
4. According to the specific speed of the turbine :
 - (a) Low specific speed turbine, (b) Medium specific speed turbine, and
 - (c) High specific speed turbine.

Impulse Turbine	Reaction Turbine
<ol style="list-style-type: none"> 1. All the available energy of the fluid is converted into kinetic energy by an efficient nozzle that forms a free jet. 2. The jet is unconfined and at atmospheric pressure throughout the action of water on the runner, and during its subsequent flow to the tail race. 3. Blades are only in action when they are in front of the nozzle. 4. Water may be allowed to enter a part or whole of the wheel circumference. 5. The wheel does not run full and air has free access to the buckets. 6. Casing has no hydraulic function to perform; it only serves to prevent splashing and to guide the water to the tail race. 7. Unit is installed above the tail race. 8. Flow regulation is possible without loss. 9. When water glides over the moving blades, its relative velocity either remains constant or reduces slightly due to friction. 	<ol style="list-style-type: none"> 1. Only a portion of the fluid energy is transformed into kinetic energy before the fluid enters the turbine runner. 2. Water enters the runner with an excess pressure, and then both the velocity and pressure change as water passes through the runner. 3. Blades are in action all the time. 4. Water is admitted over the circumference of the wheel. 5. Water completely fills the vane passages throughout the operation of the turbine. 6. Pressure at inlet to the turbine is much higher than the pressure at outlet ; unit has to be sealed from atmospheric conditions and, therefore, casing is absolutely essential. 7. Unit is kept entirely submerged in water below the tail race. 8. Flow regulation is always accompanied by loss. 9. Since there is continuous drop in pressure during flow through the blade passages, the relative velocity does increase.

PELTON WHEEL (OR TURBINE)

The Pelton wheel or Pelton turbine is a tangential flow impulse turbine. The water strikes the bucket along the tangent of the runner. The energy available at the inlet of the turbine is only kinetic energy. The pressure at the inlet and outlet of the turbine is atmospheric. This turbine is used for high heads and is named after L.A. Pelton, an American Engineer.

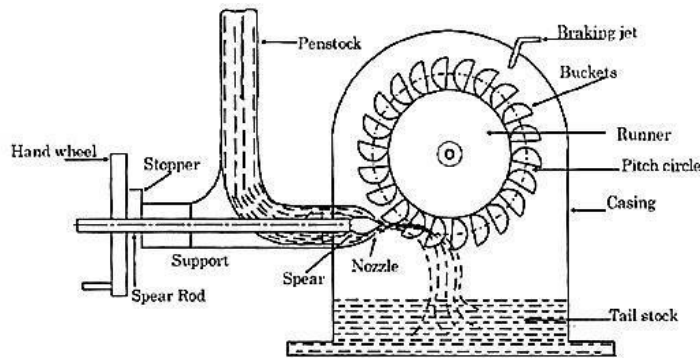
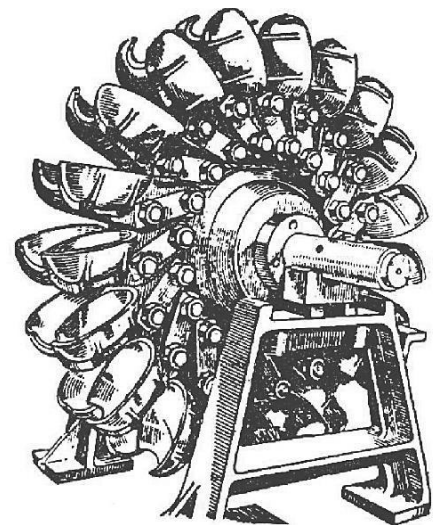


Fig. : Pelton Turbine



Main parts of Pelton Wheel

1. Nozzle and Flow Regulating Arrangement. The amount of water striking the buckets (vanes) of the runner is controlled by providing a spear in the nozzle as shown in Fig. 18.2. The spear is a conical needle which is operated either by a hand wheel or automatically in an axial direction depending upon the size of the unit. When the spear is pushed forward into the nozzle the amount of water striking the runner is reduced. On the other hand, if the spear is pushed back, the amount of water striking the runner increases.

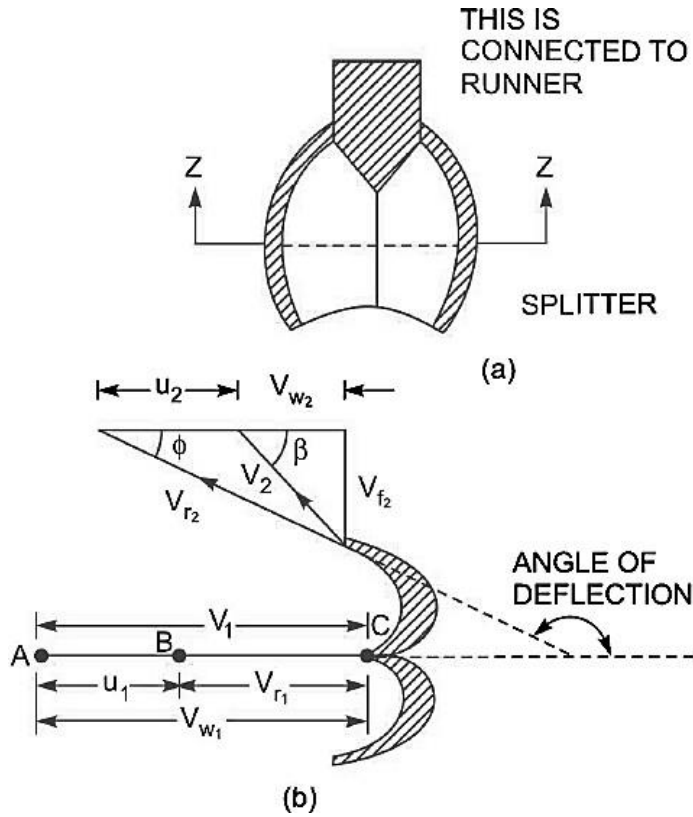
2. Runner with Buckets. Fig. 18.3 shows the runner of a Pelton wheel. It consists of a circular disc on the periphery of which a number of buckets evenly spaced are fixed. The shape of the buckets is of a double hemispherical cup or bowl. Each bucket is divided into two symmetrical parts by a dividing wall which is known as splitter.

The jet of water strikes on the splitter. The splitter divides the jet into two equal parts and the jet comes out at the outer edge of the bucket. The buckets are shaped in such a way that the jet gets deflected through 160° or 170° . The buckets are made of cast iron, cast steel bronze or stainless steel depending upon the head at the inlet of the turbine.

3. Casing. Fig. 18.4 shows a Pelton turbine with a casing. The function of the casing is to prevent the splashing of the water and to discharge water to tail race. It also acts as safeguard against accidents. It is made of cast iron or fabricated steel plates. The casing of the Pelton wheel does not perform any hydraulic function.

4. Breaking Jet.

Velocity Triangles and Work done for Pelton Wheel.



Let

$$H = \text{Net head acting on the Pelton wheel} \\ = H_g - h_f$$

where $H_g = \text{Gross head}$ and $h_f = \frac{4fLV^2}{D^* \times 2g}$

where $D^* = \text{Dia. of Penstock}, \quad N = \text{Speed of the wheel in r.p.m.},$
 $D = \text{Diameter of the wheel}, \quad d = \text{Diameter of the jet.}$

Then

$$V_1 = \text{Velocity of jet at inlet} = \sqrt{2gH}$$

$$u = u_1 = u_2 = \frac{\pi DN}{60}$$

The velocity triangle at inlet will be a straight line where

$$V_{r1} = V_1 - u_1 = V_1 - u$$

$$V_{w1} = V_1$$

$$\alpha = 0^\circ \text{ and } \theta = 0^\circ$$

From the velocity triangle at outlet, we have

$$V_{r2} = V_{r1} \text{ and } V_{w2} = V_{r2} \cos \phi - u_2.$$

The force exerted by the jet of water in the direction of motion is given by equation

$$F_x = \rho a V_1 [V_{w1} + V_{w2}]$$

As the angle β is an acute angle, +ve sign should be taken.

$$a = \text{Area of jet} = \frac{\pi}{4}d^2.$$

Now work done by the jet on the runner per second

$$= F_x \times u = \rho a V_1 [V_{w_1} + V_{w_2}] \times u \text{ Nm/s}$$

Power given to the runner by the jet

$$= \frac{\rho a V_1 [V_{w_1} + V_{w_2}] \times u}{1000} \text{ kW}$$

Work done/s per unit weight of water striking/s

$$\begin{aligned} &= \frac{\rho a V_1 [V_{w_1} + V_{w_2}] \times u}{\text{Weight of water striking/s}} \\ &= \frac{\rho a V_1 [V_{w_1} + V_{w_2}] \times u}{\rho a V_1 \times g} = \frac{1}{g} [V_{w_1} + V_{w_2}] \times u \end{aligned}$$

The energy supplied to the jet at inlet is in the form of kinetic energy and is equal to $\frac{1}{2}mV^2$

$$\therefore \text{K.E. of jet per second} = \frac{1}{2} (\rho a V_1) \times V_1^2$$

$$\therefore \text{Hydraulic efficiency, } \eta_h = \frac{\text{Work done per second}}{\text{K.E. of jet per second}}$$

$$= \frac{\rho a V_1 [V_{w_1} + V_{w_2}] \times u}{\frac{1}{2} (\rho a V_1) \times V_1^2} = \frac{2 [V_{w_1} + V_{w_2}] \times u}{V_1^2}$$

$$\text{Now } V_{w_1} = V_1, V_{r_1} = V_1 - u_1 = (V_1 - u)$$

$$\therefore V_{r_2} = (V_1 - u)$$

$$\text{and } V_{w_2} = V_{r_2} \cos \phi - u_2 = V_{r_2} \cos \phi - u = (V_1 - u) \cos \phi - u$$

Substituting the values of V_{w_1} and V_{w_2} in equation

$$\begin{aligned} \eta_h &= \frac{2 [V_1 + (V_1 - u) \cos \phi - u] \times u}{V_1^2} \\ &= \frac{2 [V_1 - u + (V_1 - u) \cos \phi] \times u}{V_1^2} = \frac{2(V_1 - u) [1 + \cos \phi] u}{V_1^2} \end{aligned}$$

The efficiency will be maximum for a given value of V_1 when

$$\frac{d}{du}(\eta_h) = 0 \quad \text{or} \quad \frac{d}{du} \left[\frac{2u(V_1 - u)(1 + \cos \phi)}{V_1^2} \right] = 0$$

$$\text{or} \quad \frac{(1 + \cos \phi)}{V_1^2} \frac{d}{du} (2uV_1 - 2u^2) = 0 \quad \text{or} \quad \frac{d}{du} [2uV_1 - 2u^2] = 0 \quad \left(\because \frac{1 + \cos \phi}{V_1^2} \neq 0 \right)$$

$$2V_1 - 4u = 0 \quad \text{or} \quad u = \frac{V_1}{2}$$

substituting the value of $u = \frac{V_1}{2}$

$$\begin{aligned} \text{Max. } \eta_h &= \frac{2 \left(V_1 - \frac{V_1}{2} \right) (1 + \cos \phi) \times \frac{V_1}{2}}{V_1^2} \\ &= \frac{2 \times \frac{V_1}{2} (1 + \cos \phi) \frac{V_1}{2}}{V_1^2} = \frac{(1 + \cos \phi)}{2}. \end{aligned}$$

Points to be Remembered for Pelton Wheel

(i) The velocity of the jet at inlet is given by $V_1 = C_v \sqrt{2gH}$
where C_v = Co-efficient of velocity = 0.98 or 0.99

H = Net head on turbine

(ii) The velocity of wheel (u) is given by $u = \phi \sqrt{2gH}$
where ϕ = Speed ratio. The value of speed ratio varies from 0.43 to 0.48.

(iii) The angle of deflection of the jet through buckets is taken at 165° if no angle of deflection is given.

(iv) The mean diameter or the pitch diameter D of the Pelton wheel is given by

$$u = \frac{\pi DN}{60} \quad \text{or} \quad D = \frac{60u}{\pi N}$$

(v) **Jet Ratio.** It is defined as the ratio of the pitch diameter (D) of the Pelton wheel to the diameter of the jet (d). It is denoted by 'm' and is given as

$$m = \frac{D}{d} \quad (= 12 \text{ for most cases})$$

(vi) Number of buckets on a runner is given by

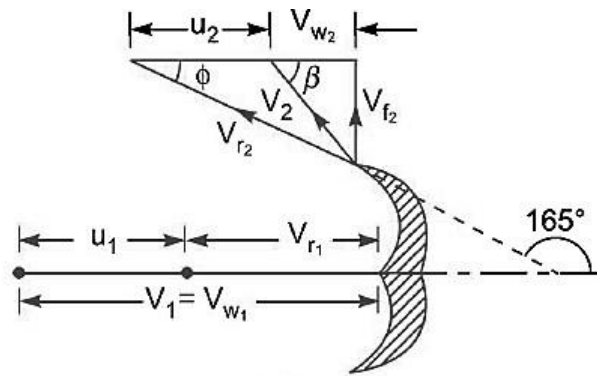
$$Z = 15 + \frac{D}{2d} = 15 + 0.5m \quad \dots(18.17)$$

where m = Jet ratio

(vii) **Number of Jets.** It is obtained by dividing the total rate of flow through the turbine by the rate of flow of water through a single jet.

Example A Pelton wheel has a mean bucket speed of 10 metres per second with a jet of water flowing at the rate of 700 litres/s under a head of 30 metres. The buckets deflect the jet through an angle of 160° . Calculate the power given by water to the runner and the hydraulic efficiency of the turbine. Assume co-efficient of velocity as 0.98.

Speed of bucket, $u = u_1 = u_2 = 10 \text{ m/s}$
 Discharge, $Q = 700 \text{ litres/s} = 0.7 \text{ m}^3/\text{s}$, Head of water, $H = 30 \text{ m}$
 Angle of deflection $= 160^\circ$
 \therefore Angle, $\phi = 180^\circ - 160^\circ = 20^\circ$
 Co-efficient of velocity, $C_v = 0.98$.
 The velocity of jet, $V_1 = C_v \sqrt{2gH} = 0.98 \sqrt{2 \times 9.81 \times 30} = 23.77 \text{ m/s}$



$$\therefore \begin{aligned} V_{r1} &= V_1 - u_1 = 23.77 - 10 \\ &= 13.77 \text{ m/s} \\ V_{w1} &= V_1 = 23.77 \text{ m/s} \end{aligned}$$

From outlet velocity triangle,

$$\begin{aligned} V_{r2} &= V_{r1} = 13.77 \text{ m/s} \\ V_{w2} &= V_{r2} \cos \phi - u_2 \\ &= 13.77 \cos 20^\circ - 10.0 = 2.94 \text{ m/s} \end{aligned}$$

Work done by the jet per second on the runner is given by equation (18.9) as

$$\begin{aligned} &= \rho a V_1 [V_{w1} + V_{w2}] \times u \\ &= 1000 \times 0.7 \times [23.77 + 2.94] \times 10 \quad (\because aV_1 = Q = 0.7 \text{ m}^3/\text{s}) \\ &= 186970 \text{ Nm/s} \end{aligned}$$

$$\therefore \text{ Power given to turbine} = \frac{186970}{1000} = \mathbf{186.97 \text{ kW. Ans.}}$$

The hydraulic efficiency of the turbine is given by equation (18.12) as

$$\begin{aligned} \eta_h &= \frac{2[V_{w1} + V_{w2}] \times u}{V_1^2} = \frac{2[23.77 + 2.94] \times 10}{23.77 \times 23.77} \\ &= \mathbf{0.9454 \text{ or } 94.54\% \text{ Ans.}} \end{aligned}$$

Example A Pelton wheel is to be designed for the following specifications :

Shaft power = 11,772 kW ; Head = 380 metres ; Speed = 750 r.p.m. ; Overall efficiency = 86% ; Jet diameter is not to exceed one-sixth of the wheel diameter. Determine :

- (i) The wheel diameter, (ii) The number of jets required, and
(iii) Diameter of the jet.

Take $K_{v_1} = 0.985$ and $K_{u_1} = 0.45$

Shaft power, S.P. = 11,772 kW
Head , $H = 380$ m
Speed, $N = 750$ r.p.m.
Overall efficiency, $\eta_0 = 86\%$ or 0.86

Ratio of jet dia. to wheel dia. $= \frac{d}{D} = \frac{1}{6}$

Co-efficient of velocity, $K_{v_1} = C_v = 0.985$

Speed ratio, $K_{u_1} = 0.45$

The velocity of wheel, $u = u_1 = u_2$

$$= \text{Speed ratio} \times \sqrt{2gH} = 0.45 \times \sqrt{2 \times 9.81 \times 380} = 38.85 \text{ m/s}$$

$$u = \frac{\pi DN}{60} \quad \therefore \quad 38.85 = \frac{\pi DN}{60}$$

$$D = \frac{60 \times 38.85}{\pi \times N} = \frac{60 \times 38.85}{\pi \times 750} = \mathbf{0.989 \text{ m.}}$$

But $\frac{d}{D} = \frac{1}{6}$

\therefore Dia. of jet, $d = \frac{1}{6} \times D = \frac{0.989}{6} = \mathbf{0.165 \text{ m. Ans.}}$

Discharge of one jet, $q = \text{Area of jet} \times \text{Velocity of jet}$

$$= \frac{\pi}{4} d^2 \times V_1 = \frac{\pi}{4} (.165)^2 \times 85.05 \text{ m}^3/\text{s} = 1.818 \text{ m}^3/\text{s}$$

Now $\eta_o = \frac{\text{S.P.}}{\text{W.P.}} = \frac{11772}{\frac{\rho g \times Q \times H}{1000}}$

$$0.86 = \frac{11772 \times 1000}{1000 \times 9.81 \times Q \times 380}, \text{ where } Q = \text{Total discharge}$$

\therefore Total discharge, $Q = \frac{11772 \times 1000}{1000 \times 9.81 \times 380 \times 0.86} = 3.672 \text{ m}^3/\text{s}$

\therefore Number of jets $= \frac{\text{Total discharge}}{\text{Discharge of one jet}} = \frac{Q}{q} = \frac{3.672}{1.818} = \mathbf{2 \text{ jets. Ans.}}$

Example The penstock supplies water from a reservoir to the Pelton wheel with a gross head of 500 m. One third of the gross head is lost in friction in the penstock. The rate of flow of water through the nozzle fitted at the end of the penstock is $2.0 \text{ m}^3/\text{s}$. The angle of deflection of the jet is 165° . Determine the power given by the water to the runner and also hydraulic efficiency of the Pelton wheel. Take speed ratio = 0.45 and $C_v = 1.0$.

Solution. Given :

Gross head, $H_g = 500 \text{ m}$

Head lost in friction, $h_f = \frac{H_g}{3} = \frac{500}{3} = 166.7 \text{ m}$

\therefore Net head, $H = H_g - h_f = 500 - 166.7 = 333.30 \text{ m}$

Discharge, $Q = 2.0 \text{ m}^3/\text{s}$

Angle of deflection $= 165^\circ$

\therefore Angle, $\phi = 180^\circ - 165^\circ = 15^\circ$

Speed ratio $= 0.45$

Co-efficient of velocity, $C_v = 1.0$

Velocity of jet, $V_1 = C_v \sqrt{2gH} = 1.0 \times \sqrt{2 \times 9.81 \times 333.3} = 80.86 \text{ m/s}$

Velocity of wheel, $u = \text{Speed ratio} \times \sqrt{2gH}$

or $u = u_1 = u_2 = 0.45 \times \sqrt{2 \times 9.81 \times 333.3} = 36.387 \text{ m/s}$

\therefore $V_{r_1} = V_1 - u_1 = 80.86 - 36.387$
 $= 44.473 \text{ m/s}$

Also $V_{w_1} = V_1 = 80.86 \text{ m/s}$

From outlet velocity triangle, we have

$$V_{r_2} = V_{r_1} = 44.473$$

$$V_{r_2} \cos \phi = u_2 + V_{w_2}$$

$$44.473 \cos 15^\circ = 36.387 + V_{w_2}$$

or $V_{w_2} = 44.473 \cos 15^\circ - 36.387 = 6.57 \text{ m/s}$.

Work done by the jet on the runner per second is given by equation (18.9) as

$$\rho a V_1 [V_{w_1} + V_{w_2}] \times u = \rho Q [V_{w_1} + V_{w_2}] \times u \quad (\because a V_1 = Q)$$

$$= 1000 \times 2.0 \times [80.86 + 6.57] \times 36.387 = 6362630 \text{ Nm/s}$$

$$= \frac{95.6475 \times 1000}{1000 \times 9.81 \times Q \times 60}$$

$$Q = \frac{95.6475 \times 1000}{\eta_o \times 1000 \times 9.81 \times 60} = \frac{95.6475 \times 1000}{0.85 \times 1000 \times 9.81 \times 60} = 0.1912 \text{ m}^3/\text{s}$$

But the discharge,

$$Q = \text{Area of jet} \times \text{Velocity of jet}$$

$$\therefore 0.1912 = \frac{\pi}{4} d^2 \times V_1 = \frac{\pi}{4} d^2 \times 33.62$$

$$\therefore d = \sqrt{\frac{4 \times 0.1912}{\pi \times 33.62}} = 0.085 \text{ m} = \mathbf{85 \text{ mm.}}$$

(iii) *Size of buckets*

$$\text{Width of buckets} = 5 \times d = 5 \times 85 = 425 \text{ mm}$$

$$\text{Depth of buckets} = 1.2 \times d = 1.2 \times 85 = \mathbf{102 \text{ mm.}}$$

(iv) *Number of buckets on the wheel* is given by equation (18.17) as

$$Z = 15 + \frac{D}{2d} = 15 + \frac{1.44}{2 \times 0.085} = 15 + 8.5 = \mathbf{23.5 \text{ say } 24.}$$

FRANCIS TURBINE

The Francis turbine is a mixed flow reaction turbine. This turbine is used for medium heads with medium discharge. Water enters the runner and flows towards the center of the wheel in the radial direction and leaves parallel to the axis of the turbine.

Turbines are subdivided into impulse and reaction machines. In the impulse turbines, the total head available is converted into the kinetic energy. In the reaction turbines, only some part of the available total head of the fluid is converted into kinetic energy so that the fluid entering the runner has pressure energy as well as kinetic energy. The pressure energy is then converted into kinetic energy in the runner.

The Francis turbine is a type of reaction turbine that was developed by James B. Francis. Francis turbines are the most common water turbine in use today. They operate in a water head from 40 to 600 m and are primarily used for electrical power production. The electric generators which most often use this type of turbine have a power output which generally ranges just a few kilowatts up to 800 MW.

Main components of Francis turbine

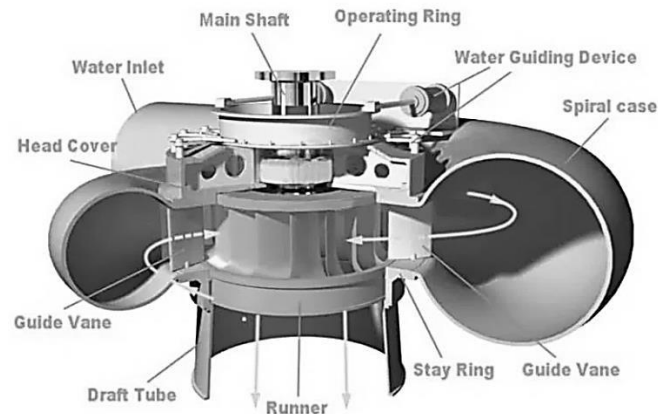
1. Spiral Casing

The water flowing from the reservoir or dam is made to pass through this pipe with high pressure. The blades of the turbines are circularly placed, which means the water striking the blades of the turbine should flow in the circular axis for efficient striking. So, the spiral casing is used, but due to the circular movement of the water, it loses its pressure.

To maintain the same pressure, the diameter of the casing is gradually reduced, to maintain the pressure uniformly, thus uniform momentum or velocity striking the runner blades.

2. Stay Vanes

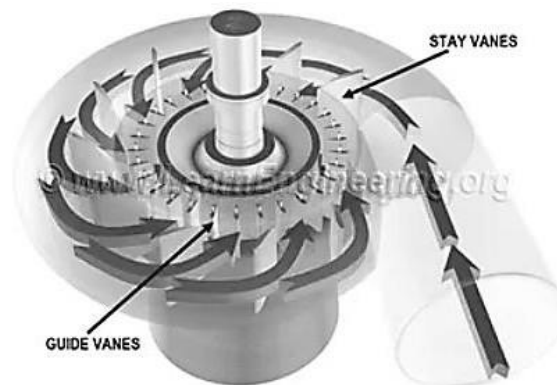
This guides the water to the runner blades. Stay vanes remain stationary at their position and reduces the swirling of water due to radial flow and as it enters the runner blades. Hence, makes the turbine more efficient.



Francis Turbine

3. Guide Vanes

Guide vanes are also known as wicket gates. The main function or usages of the guide vanes are to guide the water towards the runner and it also regulates the quantity of water supplied to runner. It also guides the water to flow at an angle and that is appropriate for the design.



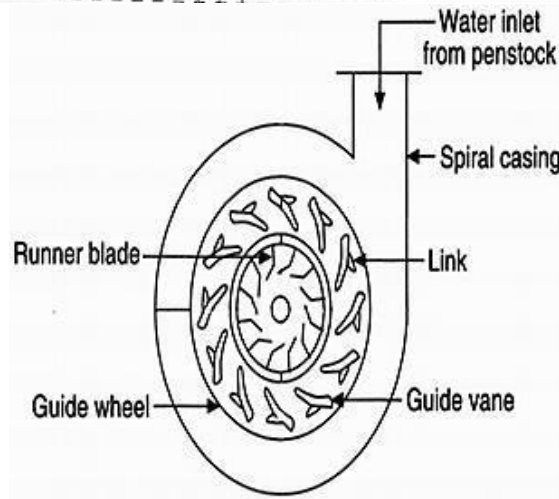
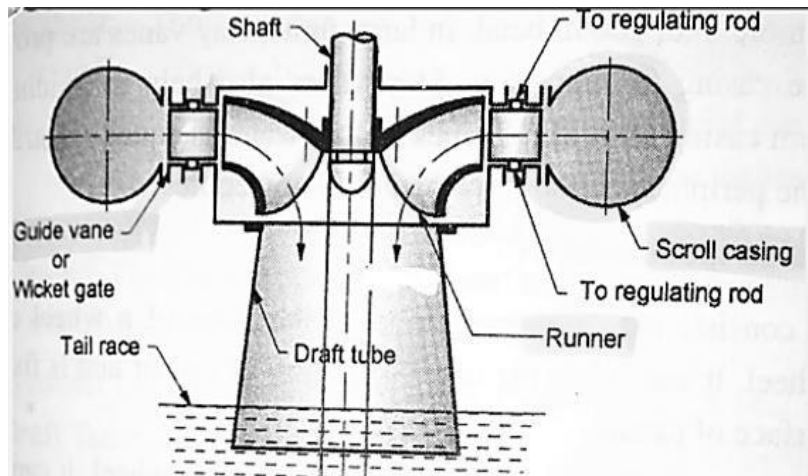
4. Runner Blades:

Absorbs the energy from the water and converts it to rotational motion of the main shaft. The runner blades design decides how effectively a turbine is going to perform. The runner blades are divided into two parts. The lower half is made in the shape of a small bucket so that it uses the impulse action of water to rotate the turbine.

The upper part of the blades uses the reaction force of water flowing through it. These two forces together make the runner rotate.

Draft Tube

The draft tube is an expanding tube which is used to discharge the water through the runner and next to the tailrace. The main function of the **draft tube** is to reduce the water velocity at the time of discharge. Its cross-section area increases along its length, as the water coming out of runner blades, is at considerably low pressure, so its expanding cross-section area helps it to recover the pressure as it flows towards the tailrace.



Working principles of Francis turbine

- The water is admitted to the runner through guide vanes or wicket gates. The opening between the vanes can be adjusted to vary the quantity of water admitted to the turbine. This is done to suit the load conditions.
- The water enters the runner with a low velocity but with a considerable pressure. As the water flows over the vanes the pressure head is gradually converted into velocity head.
- This kinetic energy is utilized in rotating the wheel. Thus the hydraulic energy is converted into mechanical energy.
- The outgoing water enters the tailrace after passing through the draft tube. The draft tube enlarges gradually and the enlarged end is submerged deeply in the tailrace water.
- Due to this arrangement a suction head is created at the exit of the runner.

Velocity Triangle

velocity of whirl at outlet (*i.e.*, V_{w_2}) will be zero. Hence the work done by water on the runner per second will be

$$= \rho Q [V_{w_1} u_1]$$

And work done per second per unit weight of water striking/s = $\frac{1}{g} [V_{w_1} u_1]$

Hydraulic efficiency will be given by, $\eta_h = \frac{V_{w_1} u_1}{gH}$.

Example A Francis turbine with an overall efficiency of 75% is required to produce 148.25 kW power. It is working under a head of 7.62 m. The peripheral velocity = $0.26 \sqrt{2gH}$ and the radial velocity of flow at inlet is $0.96 \sqrt{2gH}$. The wheel runs at 150 r.p.m. and the hydraulic losses in the turbine are 22% of the available energy. Assuming radial discharge, determine :

(i) The guide blade angle, (ii) The wheel vane angle at inlet,
 (iii) Diameter of the wheel at inlet, and (iv) Width of the wheel at inlet.

Overall efficiency	$\eta_o = 75\% = 0.75$
Power produced,	S.P. = 148.25 kW
Head,	$H = 7.62$ m
Peripheral velocity,	$u_1 = 0.26 \sqrt{2gH} = 0.26 \times \sqrt{2 \times 9.81 \times 7.62} = 3.179$ m/s
Velocity of flow at inlet,	$V_{f_1} = 0.96 \sqrt{2gH} = 0.96 \times \sqrt{2 \times 9.81 \times 7.62} = 11.738$ m/s.
Speed,	$N = 150$ r.p.m.
Hydraulic losses	= 22% of available energy
Discharge at outlet	= Radial
	$V_{w_2} = 0$ and $V_{f_2} = V_2$

Hydraulic efficiency is given as

$$\eta_h = \frac{\text{Total head at inlet} - \text{Hydraulic loss}}{\text{Head at inlet}}$$

$$= \frac{H - 0.22H}{H} = \frac{0.78H}{H} = 0.78$$

But

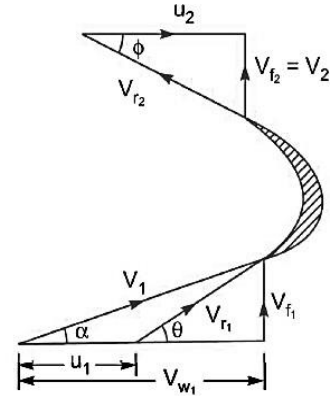
$$\eta_h = \frac{V_{w_1} u_1}{gH}$$

\therefore

$$\frac{V_{w_1} u_1}{gH} = 0.78$$

\therefore

$$V_{w_1} = \frac{0.78 \times g \times H}{u_1} = \frac{0.78 \times 9.81 \times 7.62}{3.179} = 18.34 \text{ m/s.}$$



(i) The guide blade angle, i.e., α . From inlet velocity triangle,

$$\tan \alpha = \frac{V_{f_1}}{V_{w_1}} = \frac{11.738}{18.34} = 0.64$$

\therefore

$$\alpha = \tan^{-1} 0.64 = 32.619^\circ \text{ or } 32^\circ 37'. \text{ Ans.}$$

(ii) The wheel vane angle at inlet, i.e., θ

$$\tan \theta = \frac{V_{f_1}}{V_{w_1} - u_1} = \frac{11.738}{18.34 - 3.179} = 0.774$$

\therefore

$$\theta = \tan^{-1} .774 = 37.74 \text{ or } 37^\circ 44.4'. \text{ Ans.}$$

(iii) Diameter of wheel at inlet (D_1).

Using the relation,

$$u_1 = \frac{\pi D_1 N}{60}$$

$$D_1 = \frac{60 \times u_1}{\pi \times N} = \frac{60 \times 3.179}{\pi \times 50} = 0.4047 \text{ m. Ans.}$$

(iv) Width of the wheel at inlet (B_1)

$$\eta_o = \frac{\text{S.P.}}{\text{W.P.}} = \frac{148.25}{\text{W.P.}}$$

But

$$\text{W.P.} = \frac{WH}{1000} = \frac{\rho \times g \times Q \times H}{1000} = \frac{1000 \times 9.81 \times Q \times 7.62}{1000}$$

\therefore

$$\eta_o = \frac{148.25}{\frac{1000 \times 9.81 \times Q \times 7.62}{1000}} = \frac{148.25 \times 1000}{1000 \times 9.81 \times Q \times 7.62}$$

$$Q = \frac{148.25 \times 1000}{1000 \times 9.81 \times 7.62 \times \eta_o} = \frac{148.25 \times 1000}{1000 \times 9.81 \times 7.62 \times 0.75} = 2.644 \text{ m}^3/\text{s}$$

$$Q = \pi D_1 \times B_1 \times V_{f_1}$$

$$2.644 = \pi \times .4047 \times B_1 \times 11.738$$

$$B_1 = \frac{2.644}{\pi \times .4047 \times 11.738} = 0.177 \text{ m.}$$

Example The following data is given for a Francis Turbine. Net head $H = 60$ m ; Speed $N = 700$ r.p.m.; shaft power = 294.3 kW ; $\eta_o = 84\%$; $\eta_h = 93\%$; flow ratio = 0.20 ; breadth ratio $n = 0.1$; Outer diameter of the runner = 2 \times inner diameter of runner. The thickness of vanes occupy 5% of circumferential area of the runner, velocity of flow is constant at inlet and outlet and discharge is radial at outlet. Determine :

- (i) Guide blade angle, (ii) Runner vane angles at inlet and outlet,
 (iii) Diameters of runner at inlet and outlet, and (iv) Width of wheel at inlet.

Net head, $H = 60$ m
 Speed, $N = 700$ r.p.m.
 Shaft power = 294.3 kW
 Overall efficiency, $\eta_o = 84\% = 0.84$
 Hydraulic efficiency, $\eta_h = 93\% = 0.93$

Flow ratio, $\frac{V_{f1}}{\sqrt{2gH}} = 0.20$

$$\therefore V_{f1} = 0.20 \times \sqrt{2gH}$$

$$= 0.20 \times \sqrt{2 \times 9.81 \times 60} = 6.862 \text{ m/s}$$

Breadth ratio, $\frac{B_1}{D_1} = 0.1$

Outer diameter, $D_1 = 2 \times \text{Inner diameter} = 2 \times D_2$

Velocity of flow, $V_{f1} = V_{f2} = 6.862$ m/s.

Thickness of vanes = 5% of circumferential area of runner

\therefore Actual area of flow = $0.95 \pi D_1 \times B_1$

Discharge at outlet = Radial

$\therefore V_{w2} = 0$ and $V_{f2} = V_2$

Using relation, $\eta_o = \frac{\text{S.P.}}{\text{W.P.}}$

$$0.84 = \frac{294.3}{\text{W.P.}}$$

$\therefore \text{W.P.} = \frac{294.3}{0.84} = 350.357$ kW.

But $\text{W.P.} = \frac{WH}{1000} = \frac{\rho \times g \times Q \times H}{1000} = \frac{1000 \times 9.81 \times Q \times 60}{1000}$

$$\therefore \frac{1000 \times 9.81 \times Q \times 60}{1000} = 350.357$$

$$\therefore Q = \frac{350.357 \times 1000}{60 \times 1000 \times 9.81} = 0.5952 \text{ m}^3/\text{s}.$$

Using equation (18.21), $Q = \text{Actual area of flow} \times \text{Velocity of flow}$

$$= 0.95 \pi D_1 \times B_1 \times V_{f1}$$

$$= 0.95 \times \pi \times D_1 \times 0.1 D_1 \times V_{f2}$$

$$(\because B_1 = 0.1 D_1)$$

or $0.5952 = 0.95 \times \pi \times D_1 \times 0.1 \times D_1 \times 6.862 = 2.048 D_1^2$

$\therefore D_1 = \sqrt{\frac{0.5952}{2.048}} = 0.54 \text{ m}$

But $\frac{B_1}{D_1} = 0.1$

$\therefore B_1 = 0.1 \times D_1 = 0.1 \times .54 = .054 \text{ m} = 54 \text{ mm}$

Tangential speed of the runner at inlet,

$$u_1 = \frac{\pi D_1 N}{60} = \frac{\pi \times 0.54 \times 700}{60} = 19.79 \text{ m/s.}$$

Using relation for hydraulic efficiency,

$$\eta_h = \frac{V_{w_1} u_1}{gH} \text{ or } 0.93 = \frac{V_{w_1} \times 19.79}{9.81 \times 60}$$

$\therefore V_{w_1} = \frac{0.93 \times 9.81 \times 60}{19.79} = 27.66 \text{ m/s.}$

(i) Guide blade angle (α)

From inlet velocity triangle, $\tan \alpha = \frac{V_{f_1}}{V_{w_1}} = \frac{6.862}{27.66} = 0.248$

$\therefore \alpha = \tan^{-1} 0.248 = 13.928^\circ \text{ or } 13^\circ 55.7'. \text{ Ans.}$

(ii) Runner vane angles at inlet and outlet (θ and ϕ)

$$\tan \theta = \frac{V_{f_1}}{V_{w_1} - u_1} = \frac{6.862}{27.66 - 19.79} = 0.872$$

$\therefore \theta = \tan^{-1} 0.872 = 41.09^\circ \text{ or } 41^\circ 5.4'. \text{ Ans.}$

From outlet velocity triangle, $\tan \phi = \frac{V_{f_2}}{u_2} = \frac{V_{f_1}}{u_2} = \frac{6.862}{u_2} \dots(i)$

But $u_2 = \frac{\pi D_2 N}{60} = \frac{\pi \times D_1}{2} \times \frac{N}{60} \left(\because D_2 = \frac{D_1}{2} \text{ given} \right)$

$$= \pi \times \frac{.54}{2} \times \frac{700}{60} = 9.896 \text{ m/s.}$$

Substituting the value of u_2 in equation (i),

$$\tan \phi = \frac{6.862}{9.896} = 0.6934$$

$\therefore \phi = \tan^{-1} .6934 = 34.74 \text{ or } 34^\circ 44.4'. \text{ Ans.}$

(iii) Diameters of runner at inlet and outlet

$$D_1 = 0.54 \text{ m, } D_2 = 0.27 \text{ m. Ans.}$$

(iv) Width of wheel at inlet

$$B_1 = 54 \text{ mm. Ans.}$$