

## SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)
Coimbatore – 35

#### **DEPARTMENT OF MATHEMATICS**

**UNIT - IV FUNCTIONS OF SEVERAL VARIABLES** 

# TOTAL DERIVATIVE

1) 
$$f_{x} u = f(n, y)$$
 then total differential of  $u$  is  $du = \frac{\partial u}{\partial n} dn + \frac{\partial u}{\partial y} dy$ .

2) 
$$g = g(x,y)$$
 where  $x = g(t)$ ,  $y = g_2(t)$  then
$$\frac{du}{dt} = \frac{\partial u}{\partial x} \cdot \frac{dx}{dt} + \frac{\partial u}{\partial y} \cdot \frac{dy}{dt}$$

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3) 
$$f_{y} u = f(x,y)$$
 where  $y$  is a function  $g$   $x$  then
$$\frac{du}{dx} = \frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} \cdot \frac{\partial y}{\partial z} \quad \text{and} \quad \frac{\partial u}{\partial x} = \frac{\partial u}{\partial x} \cdot \frac{\partial u}{\partial y} + \frac{\partial u}{\partial y}$$

$$\frac{du}{dy} = \frac{\partial u}{\partial x} \cdot \frac{\partial x}{\partial y} + \frac{\partial u}{\partial y}$$

Défferentiation of Implicit Junction:

De f(x,y)=c where c may be zero or non-zero & an implicit function of x & y then

$$\frac{dy}{dn} = \frac{\partial y}{\partial x}$$

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Type ?

Now 
$$u = n^2 + y^2$$
 then find total differential of  $u$ .

Solon:  $u = x^2 + y^2$ 
 $\frac{\partial u}{\partial x} = 2\pi$ .

 $\frac{\partial u}{\partial y} = 2y$ .

Find 
$$\frac{dy}{dt} = \frac{y}{u} = x^2 + y^2 + 3^2$$
 where  $x = e^t$ ,  $y = e^t s^{in}t$ .

 $\frac{3}{3} = e^t cost}$ 
 $\frac{80 \ln i}{2\pi} = 2\pi$ ,  $\frac{3u}{3y} = 2y$ ,  $\frac{3u}{3y} = 23$ .

 $\frac{3u}{3\pi} = 2\pi$ ,  $\frac{3u}{3y} = 2y$ ,  $\frac{3u}{3y} = 23$ .

 $\frac{4ni}{3t} = e^t$ ,  $y = e^t s^{in}t$ .

 $\frac{dx}{dt} = e^t$   $\frac{dy}{dt} = e^t cost + e^t s^{in}t$   $\frac{dz}{dt} = -e^t s^{in}t + e^t cost$ 



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$$\frac{du}{dt} = \frac{\partial u}{\partial n} \cdot \frac{\partial u}{\partial t} + \frac{\partial u}{\partial y} \cdot \frac{\partial y}{\partial t} + \frac{\partial u}{\partial z} \cdot \frac{\partial z}{\partial t}$$

$$= 2n \cdot e^{t} + 2y \cdot (e^{t} \cos t + e^{t} \sin t) + 2z \cdot (e^{t} \cos t - e^{t} \sin t)$$

$$= 2e^{t} \cdot e^{t} + 2e^{t} \cdot \sinh t \cdot (e^{t} \cos t + e^{t} \sin t) + 2e^{t} \cdot \cosh t \cdot (e^{t} \cos t - e^{t} \sin t)$$

$$= 2e^{2t} + 2e^{2t} \cdot \sinh t \cos t + 2e^{2t} \cdot \sin^{2} t + 2e^{2t} \cos^{2} t - 2e^{t} \cdot \cosh t$$

$$= 2e^{2t} + 2e^{2t} = 4e^{2t}$$

$$\frac{\partial h}{\partial x} = \frac{1}{2} \frac{1}{3} \frac{1}{3$$