## SNS COLLEGE OF TECHNOLOGY

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## DEPARTMENT OF AUTOMOBILE ENGINEERING

## COURSE NAME : 23MET101 - ENGINEERING MECHANICS

I YEAR / I SEMESTER
Topic - Equilibrium of Particle

## RESOLUTION OF FORCES

- It is defined as the process of splitting up the given force into a number of components, without changing its effect on the body is called resolution of a force.
- A force is, generally, resolved along two mutually perpendicular directions.


Components of $R$ along x axis Components of R along y axis

## Conditions for equilibrium

$$
\Sigma H=0
$$

$$
\Sigma V=0
$$

$$
R=0
$$

The forces $10 \mathrm{~N}, 20 \mathrm{~N}, 30 \mathrm{~N}$ and 40 N are acting on one of the vertices of a regular pentagon, towards the other four vertices taken in order. Find the Magnitude and direction of the resultant force $R$.

We know,
Sum of the interior angles of any regular polygon is $(2 n-4) \times 90^{\circ}$, where $n=$ number of sides. So, for. Regular Pentagon,

Sum of interior angles $=(2 \times 5-4) \times 90=540^{\circ}$
$\therefore$ Each included angle $=\frac{540}{5}=108^{\circ}$
Joining the vertices $B, C, D$ and $E$ with the vertex $A$, we get 3 equal angles $\theta$, as shown in fig 2.15. (a).

$$
\therefore \text { angle } \theta=\frac{108^{\circ}}{3}=36^{\circ}
$$



Hence the forces and their corresponding angles with $x$ axis are designated as below

$$
\begin{array}{ll}
F_{1}=10 \mathrm{~N} ; & \theta_{1}=0^{\circ} \\
F_{2}=20 \mathrm{~N} ; & \theta_{2}=36^{\circ} \\
F_{3}=30 \mathrm{~N} ; & \theta_{3}=(2 \times 36)=72^{\circ} \\
F_{4}=40 \mathrm{~N} ; & \theta_{4}=180-(3 \times 36)=72^{\circ}
\end{array}
$$

Resolved components of each force are given below:


$$
\begin{array}{ll}
F_{h}=30 \cos 72^{\circ} & F_{h}=-40 \cos 72^{\circ} \\
F_{v}=30 \sin 72^{\circ} & F_{v}=40 \sin 72^{\circ}
\end{array}
$$




Resolving the forces horizontally,

$$
\begin{aligned}
\Sigma H & =10+20 \cos 36^{\circ}+30 \cos 72^{\circ}-40 \cos 72^{\circ} \\
& =10+16.18+9.27-12.36 \\
& =23.09 \mathrm{~N}
\end{aligned}
$$

Resolving the forces vertically,

$$
\begin{aligned}
\Sigma V & =0+20 \sin 36^{\circ}+30 \sin 72^{\circ}+40 \sin 72^{\circ} \\
& =0+11.76+28.53+38.04
\end{aligned}
$$

Magnitude of Rcsultant forc, $R=\sqrt{(\Sigma H)^{2}+\left(\Sigma H^{2}\right.}$

$$
\therefore R=\sqrt{(23.09)^{2}+(7833)^{2}}
$$

$$
=81.67 \mathrm{~N}
$$

Dirction of Resulant force,

$$
a=\tan ^{-1}\left(\frac{\Sigma V}{\Sigma H}\right)=\tan ^{-1}\left(\frac{78.33}{23.09}\right)=73.50^{\circ}
$$



The three coplanar forces are acting at a point in the diagram. One of the forces is unknown and its magnitude is shown by $P$. The resultant is having a magnitude 500 N and is acting along Y axis (positive direction). Determine the unknown force P and its inclination with X -axis


It is given that the resultant force is 500 N , acts in the positive direction of $Y$ axis.
As Resultant force is a vertical force, it is equal to net vertical force and also the net horizontal force is zero.
i.e., $\quad \Sigma \mathrm{V}=R=500 \mathrm{~N}$ and $\Sigma H=0$.

Using these two conditions, two unknowns $P$ and $\theta$ are determined as follows.
Resolving the forces horizontally,

$$
\begin{align*}
\Sigma H & =P \cos \theta-775 \cos 0^{\circ}+800 \cos 20^{\circ} \\
0 & =P \cos \theta-775+751.75 \\
\therefore \quad P \cos \theta & =23.25 N \tag{i}
\end{align*}
$$

Resolving the forces vertically,

$$
\begin{align*}
\Sigma V & =P \sin \theta-800 \sin 20^{\circ} \\
500 & =P \sin \theta-273.61 \\
\therefore P \sin \theta & =773.61 N \tag{ii}
\end{align*}
$$

Solving the equations (i) and (ii)

$$
\frac{P \sin \theta}{P \cos \theta}=\frac{773.61}{23.25}
$$

$$
\tan \theta=33.27
$$

$$
\theta=\tan ^{-1}(33.27)
$$

$$
\theta=88.27^{\circ}
$$

Substituting $\theta=88.27^{\circ}$ in equation (i), $\quad P=770.13 \mathrm{~N}$

Two cables which have known tensions are attached to the top of a tower AB .A third cable $A C$ is used as a guy wire as shown in diagram. Determine the tension in AC if the resultant of the forces exerted at A by the three cables acts vertically downwards


It is given that the resultant force is acting vertically downwards. Hence, the net horizontal force is zero (i.e., $\Sigma H=O$ ) and the resultant force is equal to the net vertical force.

Angle of inclination of Guy wire $A C$ with reference to $X$ axis can be determined from the available data.
In right angled triangle $A B C$,

$$
\begin{aligned}
\tan \theta & =\frac{12}{8} \\
\theta & =\tan ^{-1}\binom{12}{8}=56.30^{\circ}
\end{aligned}
$$

Now, resolving the forces horizontally,

$$
\begin{aligned}
\Sigma H & =25 \cos 10^{\circ}-40 \cos 20^{\circ}+\mathrm{T} \cos \theta=0, & \text { here } \\
0 & =25 \cos 10^{\circ}-40 \cos 20^{\circ}+\mathrm{T} \cos 56.3^{\circ} & \Sigma H=0 \\
0 & =24.62-37.58+0.5557 & \Sigma V=R
\end{aligned}
$$

Solving, $T=23.35 N$.
$\therefore$ The tension in the Guy wire is $23.35 N$.

The forces shown in the figure are acting on a particle , and keep the particle in equilibrium .The magnitude of F1 is 250 N . Find the magnitude of F2and F3.

## Method (By Lami's theorem)

Here there are only three concurrent forces, acting outwards from a point. Hence, lami's theorem can be applied.

The angle opposite to $F_{1}$ force is $(90+30)=120^{\circ}$ similarly, angles opposite to $F_{2}$ and $F_{3}$ forces are $(90+60)=150^{\circ}$; and $(180-60-30)=90^{\circ}$ respectively.

By lami's theorem,

$$
\frac{F_{1}}{\sin 120}=\frac{F_{2}}{\sin 150}=\frac{F_{3}}{\sin 90}
$$


or $\frac{250}{\sin 120}=\frac{F_{2}}{\sin 150}=\frac{F_{3}}{\sin 90}$
solving we get

$$
F_{2}=144.33 \mathrm{~N} ; \quad F_{3}=288.67 \mathrm{~N}
$$

## Method II (By equations of Equilibrium)

The given system of force is coplanar concurrent. Hence, equations of equilibrum satisfied in this particular force system are $\Sigma H=0$ and $\Sigma V=0$

```
Applying \SigmaH=0 ( }\quad\textrm{m}+\boldsymbol{+
            F
or }\mp@subsup{F}{2}{}\operatorname{cos}30=\mp@subsup{F}{1}{}\operatorname{cos}6
            \thereforeF
            =144.33N
Applying \SigmaV =0 ( }\uparrow+\mathrm{ +)
    F
or 250 sin 60+144.33 sin 30 = F F3
                        \therefore\quadF3}=288.67\textrm{N
```

The forces shown in diagram are in equilibrium . Find the magnitude and direction of $\theta$ (theta) of the unknown forces $P$

The inclined forces are resolved into two components in horizontal and vertical directions and the algebraic sum of horizantal components ( i,e, $\Sigma H$ ) is equated to zero.
$\Sigma H=0(\rightarrow+)$
i.e, $25 \cos 45+18-30 \cos 30-P \cos \theta=0$

$$
\begin{align*}
17.68+18-25.98 & =P \cos \theta \\
\therefore \quad P \cos \theta & =9.7 \tag{i}
\end{align*}
$$

$\Sigma V=0 \quad(\uparrow+)$
i.e., $15+25 \sin 45-30 \sin 30-P \sin \theta=0$

$$
15+17.68-15=P \sin \theta
$$

$$
\begin{equation*}
\therefore \quad P \sin \theta=17.68 \tag{ii}
\end{equation*}
$$



Dividing eqn (ii) by eqn (i), we get

$$
\begin{aligned}
\frac{P \sin \theta}{P \cos \theta} & =\frac{17.68}{9.7} \\
\text { or } \tan \theta & =1.822 \\
\theta & =\tan ^{1}(1.822) \\
& =61.24^{\circ} \quad \text { (Ans) }
\end{aligned}
$$

Substituing the value of $\theta$ in eqn (i), we get

$$
\begin{aligned}
P \cos (61.24)^{\circ} & =9.7 \\
\therefore \quad P & =\frac{9.7}{\cos 61.24}=20.16 \mathrm{~N}
\end{aligned}
$$

(Ans)

## Thank You..

