

Series - Series Feedback Amplifier

First term series represent input

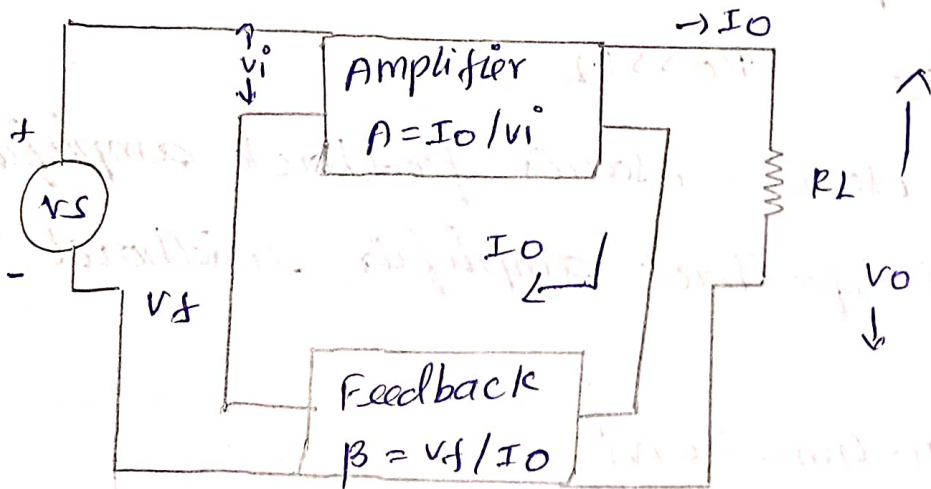
Input is voltage series

second term series represent output

Output is current series

So, it is also known as current-series feedback amplifier

Both the series, the input and output impedance are increased



Amplifier with gain

$$A = \frac{I_o \rightarrow \text{O/P}}{v_i \rightarrow \text{I/P}}$$

Feedback network with gain

$$\beta = v_f / I_o$$

$$v_f = \beta I_o$$

Here, Input is voltage and output is current, so

$$I_o \propto V_i$$

$$I_o = G_m V_i$$

$$G_m = I_o / V_i$$

This ratio of current & voltage act as Transfer conductance.

So it is also known as Transfer conductance feedback amplifier.

The Input impedance is high and output impedance are also high

$$R_i \gg R_s \quad R_o \gg R_L$$

gain of series-series feedback amplifier
 gain of feedback amplifier without feedback.

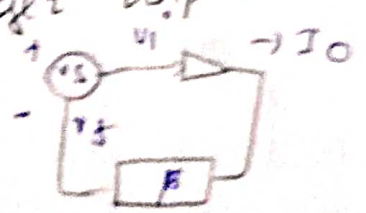
$$A = G_m = I_o / V_i$$

$$I_o = G_m V_i$$

gain of feedback amplifier with feedback.

$$\beta = \frac{V_f}{I_o} \quad V_f = \beta I_o$$

To get input voltage amplifier



$v_i =$ Actual Input voltage

to get a input voltage, subtracting feedback voltage from source voltage.

$$v_i^{\circ} = v_s - v_f$$

$$\therefore v_f = \beta I_O$$

$$v_i^{\circ} = v_s - \beta I_O$$

$$\therefore I_O = G_m v_i^{\circ}$$

$$v_i^{\circ} = v_s - \beta G_m v_i^{\circ}$$

$$v_s = v_i^{\circ} + \beta G_m v_i^{\circ}$$

$$v_s = v_i^{\circ} [1 + \beta G_m]$$

The gain of feedback amplifier

$$A_f = \frac{I_O}{v_s}$$

$$\therefore I_O = G_m v_i^{\circ}$$

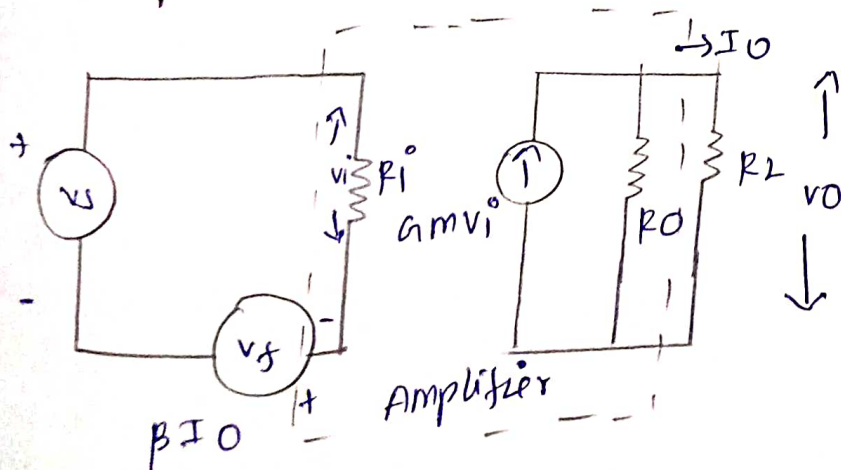
$$= \frac{G_m v_i^{\circ}}{v_i^{\circ} [1 + \beta G_m]}$$

$$v_s = v_i^{\circ} [1 + \beta G_m]$$

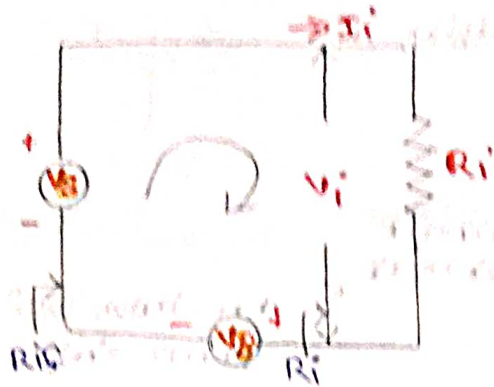
$$A_f = \frac{G_m}{1 + \beta G_m} \Rightarrow \frac{A}{1 + A\beta}$$

The gain of amplifier decrease $(1 + \beta G_m)$

to improve stability



Input Impedance



The input impedance without feedback

$$R_i = \frac{V_i}{I_i}$$

The input impedance with feedback is

$$R_{if} = \frac{V_s}{I_i} \rightarrow \text{I/P voltage}$$

$$I_i \rightarrow \text{I/P current}$$

Apply KVL to input circuit

$$V_s = I_i R_i + V_i$$

$$= I_i R_i + \beta I_o$$

$$= I_i R_i + \beta G_m V_i$$

$$= I_i R_i + \beta G_m I_i R_i$$

$$V_s = I_i R_i [1 + \beta G_m]$$

$$\frac{V_s}{I_i} = R_i [1 + \beta G_m R_i]$$

$$R_{if} = R_i [1 + G_m \beta]$$

Thus the input impedance of the amplifier is increased by the factor $(1 + G_m \beta)$ using series-series feedback

$$[\because V_s = \beta I_o]$$

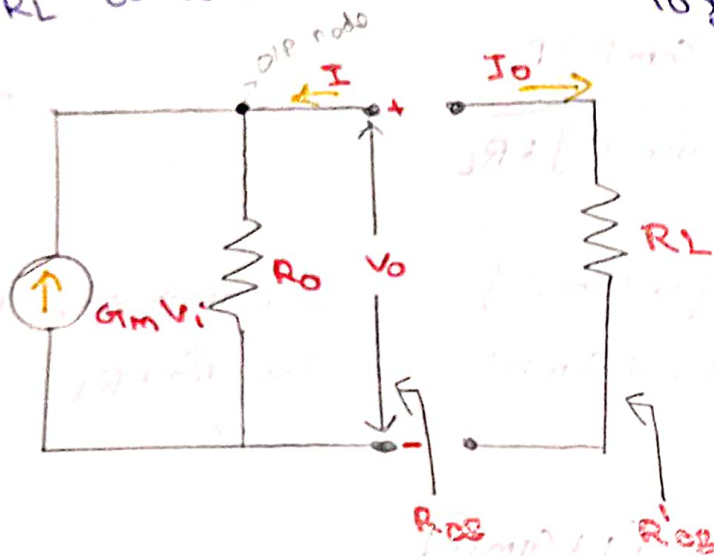
$$[I_o = G_m V_i]$$

$$[V_i = I_i R_i]$$

Output Impedance

For finding the output impedance we have to make two assumption here

- 1) output resistance can be measured by shorting the input source $V_S = 0$
- 2) Looking into the output terminals with R_L disconnected



To find $R_{o\beta}$

$$R_{o\beta} = \frac{V_o}{I_o}$$

Applying KCL to the output node $V_S = 0$

$$I_o = \frac{V_o}{R_o} - G_m V_i = \frac{V_o}{R_o} - G_m V_S \quad \left[\begin{array}{l} \because V_i = V_S - V_S \\ V_i = -V_S \end{array} \right]$$

$$= \frac{V_o}{R_o} - G_m \beta I_o \quad \left[\because V_S = \beta I_o \right]$$

$$\frac{V_o}{R_o} = I_o + G_m \beta I_o$$

$$\frac{V_o}{R_o} \Rightarrow I_o [1 + G_m \beta]$$

$$\frac{V_o}{I_o} = R_o [1 + G_m \beta]$$

$$R_{o\beta} = R_o [1 + G_m \beta]$$

Thus the output impedance is increased by the factor $(1 + G_m \beta)$ using series-series feedback

Output Impedance with R_L

Then we can include this R_L which is parallel to this R_{oS} to get R'_{oS}

$$R'_{oS} = R_{oS} \parallel R_L$$

$$= \frac{R_{oS} \times R_L}{R_{oS} + R_L}$$

$$= \frac{R_o [1 + G_m \beta] R_L}{R_o [1 + G_m \beta] + R_L}$$

$$= \frac{R_o R_L [1 + G_m \beta]}{R_o + R_L + G_m \beta R_o}$$

\div numerator and denominator by $R_o + R_L$

$$R'_{oS} = \frac{R_o R_L}{R_o + R_L} [1 + G_m \beta]$$

$$\frac{R_o + R_L}{R_o + R_L} + \frac{R_o G_m \beta}{R_o + R_L}$$

where

$$R_o' = \frac{R_o R_L}{R_o + R_L} = R_o \parallel R_L$$

$$G_m = \frac{R_o}{R_o + R_L} G_m \rightarrow \text{Gain of the amplifier without } R_L \text{ resistor}$$

\downarrow
Gain of the amplifier with R_L resistor

$$R'_{oS} = \frac{R_o' (1 + \beta G_m)}{(1 + \beta G_m)}$$