

## Analysis

The relative gain of a single tuned amplifier is given as

$$\left[ \frac{A_v}{A_v(\text{res})} \right] = \frac{1}{1 + j2\delta Q_{\text{eff}}}$$

$A_v \rightarrow$  voltage gain  
 $A_v(\text{res}) \rightarrow$  Voltage gain resonant frequency

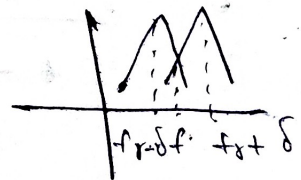
$Q_{\text{eff}} \rightarrow$  Effective Quality factor or  
Quality factor at resonant condition.

Assume,  $x = 2\delta Q_{\text{eff}}$

$$\left[ \frac{A_v}{A_v(\text{res})} \right] = \frac{1}{1 + jx}$$

Since one stage is tuned to frequency below  $f_r$  i.e.  $f_r - \delta$  and other stage is tuned to a frequency above  $f_r + \delta$

$$\left[ \frac{A_v}{A_v(\text{res})} \right]_1 = \frac{1}{1 + j(x-1)}$$



$$\left[ \frac{A_v}{A_v(\text{res})} \right]_2 = \frac{1}{1 + j(x+1)}$$

The overall gain of two stages is the product of individual gains of the two stages

$$\left[ \frac{A_v}{A_v(\text{res})} \right]_{\text{staggered tuned pair}} = \left[ \frac{A_v}{A_v(\text{res})} \right]_1 * \left[ \frac{A_v}{A_v(\text{res})} \right]_2$$

$$= \frac{1}{1+j(\alpha+1)} * \frac{1}{1+j(\alpha-1)}$$

$$= \frac{1}{(1+j\alpha+j)} * \frac{1}{(1+j\alpha-j)}$$

$$= \frac{1}{1 + j\alpha - j + j\alpha + j^2\alpha^2 - j^2\alpha}$$

$$+ j + j^2\alpha - j^2$$

$$= \frac{1}{1 + 2j\alpha - \alpha^2 + 1 - \alpha^2 + 1}$$

$$= \frac{1}{2 + 2j\alpha - \alpha^2}$$

$$= \frac{1}{2 - \alpha^2 + j2\alpha}$$

$$\left[ \frac{A_v}{A_v(\text{res})} \right]_{\text{staggered tuned pair}} = \frac{1}{\sqrt{(2-\alpha^2)^2 + (2\alpha)^2}}$$

$$= \frac{1}{4 + \alpha^4 - 4\alpha^2 + 4\alpha^2}$$

$$= \frac{1}{\sqrt{4 + \alpha^4}}$$

where  $\alpha = 2\delta Q_e$

$$= \frac{1}{\sqrt{4 + (2\delta Q_e)^4}}$$

$$= \frac{1}{\sqrt{4 + 16\delta^4 Q_e^4}}$$

$$= \frac{1}{2\sqrt{1 + 4\delta^4 Q_e^4}}$$

This is relative gain of stagger tuned amplifier.