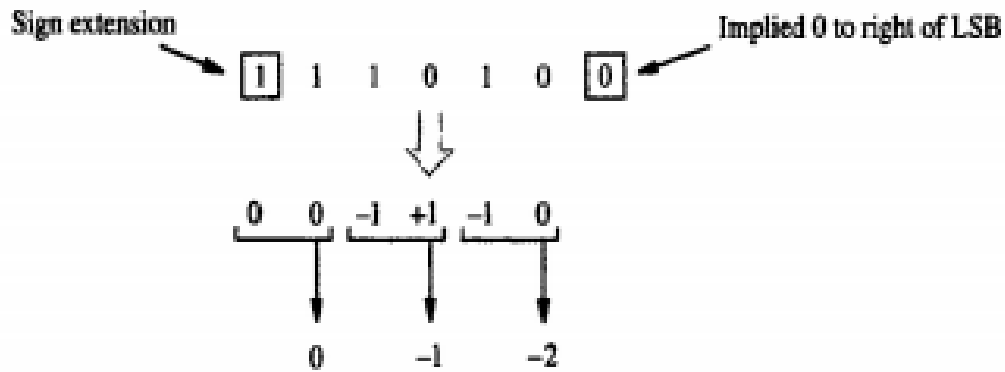


# Fast Multiplication

1. Bit-Pair Recoding of Multipliers
2. Carry-Save Addition of Summands

## Bit-Pair Recoding of Multipliers



(a) Example of bit-pair recoding derived from Booth recoding

Multiplier bit-pair		Multiplier bit on the right $i - 1$	Multiplicand selected at position $i$
$i + 1$	$i$		
0	0	0	$0 \times M$
0	0	1	$+1 \times M$
0	1	0	$+1 \times M$
0	1	1	$+2 \times M$
1	0	0	$-2 \times M$
1	0	1	$-1 \times M$
1	1	0	$-1 \times M$
1	1	1	$0 \times M$

(b) Table of multiplicand selection decisions

Figure 6.14 Multiplier bit-pair recoding.

$$\begin{array}{r}
 0\ 1\ 1\ 0\ 1\ (+13) \\
 \times 1\ 1\ 0\ 1\ 0\ (-6) \\
 \hline
 \end{array}$$



$$\begin{array}{r}
 0\ 1\ 1\ 0\ 1 \\
 0\ -1\ +1\ -1\ 0 \\
 \hline
 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0 \\
 1\ 1\ 1\ 1\ 1\ 0\ 0\ 1\ 1 \\
 0\ 0\ 0\ 0\ 1\ 1\ 0\ 1 \\
 1\ 1\ 1\ 0\ 0\ 1\ 1 \\
 0\ 0\ 0\ 0\ 0\ 0 \\
 \hline
 1\ 1\ 1\ 0\ 1\ 1\ 0\ 0\ 1\ 0\ (-78)
 \end{array}$$



$$\begin{array}{r}
 0\ 1\ 1\ 0\ 1 \\
 0\ -1\ -2 \\
 \hline
 1\ 1\ 1\ 1\ 1\ 0\ 0\ 1\ 1\ 0 \\
 1\ 1\ 1\ 1\ 0\ 0\ 1\ 1 \\
 0\ 0\ 0\ 0\ 0\ 0 \\
 \hline
 1\ 1\ 1\ 0\ 1\ 1\ 0\ 0\ 1\ 0
 \end{array}$$

**Figure 6.15** Multiplication requiring only  $n/2$  summands.