## SNS COLLEGE OF TECHNOLOGY COIMBATORE

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## DEPARTMENT OF MCA

Course Name : 19CAT609 - DATA BASE MANAGEMENT SYSTEM

Class: I Year / I Semester

Unit II - Introduction

Topic I - Relational Model

## Relational Model

$\square$ Data Representation
$\square$ The way integrity constraints expressed?
$\square$ Data creation, management and manipulation
$\square$ Extended Relational-Algebra-Operations

- Database design
$\square$ Data independence


## Example of a Relation

Main construct for representing data in the relational model is a relation.

- A relation consists of a relation schema and a relation instance
$\square$ A relation schema describes the column heads for the table
$\square$ Students(sid: string, name: string, login: string, age: integer, gpa: real)
$\square$ An instance of a relation is a set of tuples, also called records
$\square$ A relation instance can be thought of as a table in which each tuple is a row, and all rows have the same number of fields
$\square$ Degree, also called arity, of a relation is the number of fields. The cardinality of a relation instance is the number of tuples in it


## Example of a Relation



## Relation schema

$\square$ It specifies the domain of each field or column in the relation instance
$\square$ domain constraints in the schema specify an important condition that we want each instance of the relation to satisfy
$\square$ Domain of a field is essentially the type of that field

## Basic Structure

- let $\mathrm{R}(\mathrm{f} 1: \mathrm{D} 1, \ldots, \mathrm{fn}: \mathrm{Dn})$ be a relation schema,

For each fi, $1 \leq \mathrm{i} \leq \mathrm{n}$, let Domi be the set of values associated with the domain named Di
$\square$ An instance of $R$ that satisfies the domain constraints in the schema is a set of tuples with $n$ fields

$$
\left\{\left\langle f_{1}: d_{1}, \ldots, f_{n}: d_{n}\right\rangle \mid d_{1} \in \operatorname{Dom}_{1}, \ldots, d_{n} \in \operatorname{Dom}_{n}\right\}
$$

$\square$ angular brackets $h . .$. identify the fields of a tuple
$\square \quad\{\ldots\}$ denote a set (of tuples)
$\square$ vertical bar \| should be read 'such that,' the symbol $\in$ should be read 'in,

## Relation schema

A relational database is a collection of relations with distinct relation
names


## Relation Schema

$A_{1}, A_{2}, \ldots, A_{n}$ are attributes
$R=\left(A_{1}, A_{2}, \ldots, A_{n}\right)$ is a relation schema
Example:
Customer_schema $=($ customer_name, customer_street, customer_city $)$
$r(R)$ denotes a relation $r$ on the relation schema $R$
Example:
customer (Customer_schema)

## Database

- A database consists of multiple relations
$\square$ Information about an enterprise is broken up into parts, with each relation storing one part of the information. For instance
account: stores information about accounts
depositor: stores information about which customer owns which account
customer: stores information about customers
$\square$ Storing all information as a single relation such as
bank(account_number, balance, customer_name, ..) results in repetition of information
$\square$ Normalization theory deals with how to design relational schemas


## The customer Relation

| customer_name | customer_street | customer_city |
| :--- | :---: | :---: |
| Adams | Spring | Pittsfield |
| Brooks | Senator | Brooklyn |
| Curry | North | Rye |
| Glenn | Sand Hill | Woodside |
| Green | Walnut | Stamford |
| Hayes | Main | Harrison |
| Johnson | Alma | Palo Alto |
| Jones | Main | Harrison |
| Lindsay | Park | Pittsfield |
| Smith | North | Rye |
| Turner | Putnam | Stamford |
| Williams | Nassau | Princeton |

## The depositor Relation

| customer_name | account_number |
| :--- | :---: |
| Hayes | A-102 |
| Johnson | A-101 |
| Johnson | A-201 |
| Jones | A-217 |
| Lindsay | A-222 |
| Smith | A-215 |
| Turner | A-305 |

- Let $K \subseteq R$
$\square K$ is a superkey of $R$ if values for $K$ are sufficient to identify a unique tuple of each possible relation $r(R)$
$\square$ by "possible $r$ " we mean a relation $r$ that could exist in the enterprise we are modeling.
$\square$ Example: \{customer_name, customer_street\} and \{customer_name\}
are both superkeys of Customer, if no two customers can possibly have the same name

I In real life, an attribute such as customer_id would be used instead of customer_name to uniquely identify customers

- $K$ is a candidate key if $K$ is minimal

Example: \{customer_name\} is a candidate key for Customer, since it is a superkey and no subset of it is a superkey.
$\square$ Primary key: a candidate key chosen as the principal means of identifying tuples within a relation
. Should choose an attribute whose value never, or very rarely, changes.
E.g. email address is unique, but may change

## Foreign Keys

A relation schema may have an attribute that corresponds to the primary key of another relation. The attribute is called a foreign key.
$\square$ E.g. customer_name and account_number attributes of depositor are foreign keys to customer and account respectively.


## Query Languages

$\square$ Language in which user requests information from the database.

- Categories of languages
- Procedural
- Non-procedural, or declarative
- "Pure" languages:
- Relational algebra
- Tuple relational calculus
- Domain relational calculus
- Pure languages form underlying basis of query languages that people use.


## Relational Algebra

Procedural language
Six basic operators
select: $\sigma$
project: $\Pi$
union: $\cup$
set difference: -
Cartesian product: x
rename: $\rho$
The operators take one or two relations as inputs and produce a new relation as a result.

- Relation r

| $A$ | $B$ | $C$ | $D$ |
| :--- | :--- | :--- | :--- |



## Select Operation

Notation: $\sigma_{p}(r)$
$p$ is called the selection predicate
Defined as:

$$
\sigma_{p}(\boldsymbol{r})=\{t \mid t \in r \text { and } p(t)\}
$$

Where $p$ is a formula in propositional calculus consisting of terms connected by : $\wedge$ (and), $\vee$ (or), $\neg$ (not)
Each term is one of:
<attribute> op <attribute> or <constant>
where op is one of: $=, \neq,>, \geq .<. \leq$
Example of selection:

$$
\sigma_{\text {branch_name="Perryridge" }}(\text { account })
$$

## Project Operation - Example

- Relation r

| $A$ | $B$ | $C$ |
| :---: | :---: | :---: |
| $\alpha$ | 10 | 1 |
| $\alpha$ | 20 | 1 |
| $\beta$ | 30 | 1 |
| $\beta$ | 40 | 2 |

$\cdot \prod_{A, C}(r)$

## Project Operation

## Notation:

where $A_{1}, A_{2}$ are attribute names and $r$ is a relation name.
The result is defined as the relation of $k$ columns obtained by erasing the columns that are not listed
Duplicate rows removed from result, since relations are sets Example: To eliminate the branch_name attribute of account
$\prod_{\text {account_number, balance }}$ (account)

## Union Operation - Example

- Relations $r$, $s$ :

| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 1 |
| $\alpha$ | 2 |
| $\beta$ | 1 |
| $r$ |  | | $A$ | $B$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $\alpha$ 2 <br> $\beta$ 3 |  | $s$ |  |

-r $\cup \mathrm{s}$ :

| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 1 |
| $\alpha$ | 2 |
| $\beta$ | 1 |
| $\beta$ | 3 |

## Union Operation

Notation: $r \cup s$
Defined as:

$$
r \cup s=\{t \mid t \in r \text { or } t \in s\}
$$

For $r \cup s$ to be valid.

1. $r, s$ must have the same arity (same number of attributes)
2. The attribute domains must be compatible (example: $2^{\text {nd }}$ column of $r$ deals with the same type of values as does the $2^{\text {nd }}$ column of $s$ )

Example: to find all customers with either an account or a loan
$\prod_{\text {customer_name }}$ (depositor) $\cup \prod_{\text {customer_name }}$ (borrower)

## Union Operation - Example

- Relations r, s:

| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 1 |
| $\alpha$ | 2 |
| $\beta$ | 1 |
| $r$ |  |


| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 2 |
| $\beta$ | 3 |

$S$
-r - s:

| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 1 |
| $\beta$ | 1 |

## Set Difference Operation

Notation $r-s$
Defined as:

$$
r-s=\{t \mid t \in r \text { and } t \notin s\}
$$

Set differences must be taken between compatible relations.
$r$ and $s$ must have the same arity
attribute domains of $r$ and $s$ must be compatible

## Cartesian-Product Operation - Example

Relations $\mathrm{r}, \mathrm{s}$ :


| $C$ | $D$ | $E$ |
| :---: | :---: | :---: |
| $\alpha$ | 10 | $a$ |
| $\beta$ | 10 | $a$ |
| $\beta$ | 20 | $b$ |
| $\gamma$ | 10 | $b$ |

- r x s:

| $A$ | $B$ | $C$ | $D$ | $E$ |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | 1 | $\alpha$ | 10 | $a$ |
| $\alpha$ | 1 | $\beta$ | 10 | $a$ |
| $\alpha$ | 1 | $\beta$ | 20 | $b$ |
| $\alpha$ | 1 | $\gamma$ | 10 | $b$ |
| $\beta$ | 2 | $\alpha$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 20 | $b$ |
| $\beta$ | 2 | $\gamma$ | 10 | $b$ |

## Cartesian-Product Operation

Notation $r \times s$
Defined as:

$$
r \times s=\{t q \mid t \in r \text { and } q \in s\}
$$

Assume that attributes of $r(R)$ and $s(S)$ are disjoint.
(That is, $R \cap S=\varnothing$ ).
If attributes of $r(R)$ and $s(S)$ are not disjoint, then renaming must be used.

## Composition of Operations

Can build expressions using multiple operations
Example: $\sigma_{A=C}(r x s)$ $r x s$

| $A$ | $B$ | $C$ | $D$ | $E$ |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | 1 | $\alpha$ | 10 | $a$ |
| $\alpha$ | 1 | $\beta$ | 10 | $a$ |
| $\alpha$ | 1 | $\beta$ | 20 | $b$ |
| $\alpha$ | 1 | $\gamma$ | 10 | $b$ |
| $\beta$ | 2 | $\alpha$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 20 | $b$ |
| $\beta$ | 2 | $\gamma$ | 10 | $b$ |


| $A$ | $B$ | $C$ | $D$ | $E$ |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | 1 | $\alpha$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 10 | $a$ |
| $\beta$ | 2 | $\beta$ | 20 | $b$ |

## Rename Operation

Allows us to name, and therefore to refer to, the results of relationalalgebra expressions.
Allows us to refer to a relation by more than one name. Example:

$$
\rho_{x}(E)
$$

returns the expression $E$ under the name $X$
If a relational-algebra expression $E$ has arity $n$, then returns the result of expression $E$ under the name $X$, and with the attributes renamed to $A_{1}, A_{2}, \ldots, A_{n}$.

## Banking Example

branch (branch_name, branch_city, assets) customer (customer_name, customer_street, customer_city) account (account_number, branch_name, balance) loan (loan_number, branch_name, amount) depositor (customer_name, account_number) borrower (customer_name, loan_number)

## Example Queries

- Find all loans of over \$1200

$$
\sigma_{\text {amount }>1200} \text { (loan) }
$$

- Find the loan number for each loan of an amount greater than $\$ 1200$

$$
\prod_{\text {loan_number }}\left(\sigma_{\text {amount > } 1200}(\text { loan })\right)
$$

- Find the names of all customers who have a loan, an account, or both, from the bank

$$
\Pi_{\text {customer_name }} \text { (borrower) } \cup \Pi_{\text {customer_name }} \text { (depositor) }
$$

## Example Queries

- Find the names of all customers who have a loan at the Perryridge branch.
- Query 1

$$
\begin{aligned}
& \prod_{\text {customer_name }}\left(\sigma_{\text {branch_name }}=\text { "Perryridge" }( \right. \\
& \left.\left.\sigma_{\text {borrower.loan_number }=\text { loan.loan_number }}(\text { borrower x loan })\right)\right)
\end{aligned}
$$

- Query 2

$$
\begin{array}{r}
\prod_{\text {customer_name }}\left(\sigma_{\text {loan.loan_number }}=\right.\text { borrower.loan_number } \\
\left.\left.\left(\sigma_{\text {branch_name }=\text { "Perryridge" }}(\text { loan })\right) \times \text { borrower }\right)\right)
\end{array}
$$

## Example Queries

- Find the largest account balance
-Strategy:
- Find those balances that are not the largest
-Rename account relation as $d$ so that we can compare each account balance with all others
- Use set difference to find those account balances that were not found in the earlier step.
-The query is:

```
\Pi balance}(\mathrm{ account) - - \account.balance
    ( }\mp@subsup{\sigma}{\mathrm{ account.balance < d.balance }}{}(\mathrm{ account x }\mp@subsup{\rho}{d}{}(account))
```


## Formal Definition

A basic expression in the relational algebra consists of either one of the following:

A relation in the database
A constant relation
Let $E_{1}$ and $E_{2}$ be relational-algebra expressions; the following are all relationalalgebra expressions:
$E_{1} \cup E_{2}$
$E_{1}-E_{2}$
$E_{1} \times E_{2}$
$\sigma_{p}\left(E_{1}\right), P$ is a predicate on attributes in $E_{1}$
$\Pi_{s}\left(E_{1}\right), S$ is a list consisting of some of the attributes in $E_{1}$
$\rho_{x}\left(E_{1}\right), \mathrm{x}$ is the new name for the result of $E_{1}$

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$\rho_{x}\left(E_{1}\right), \mathrm{x}$ is the new name for the result of $E_{1}$

## Additional Operations

We define additional operations that do not add any power to the relational algebra, but that simplify common queries.
$\checkmark$ Set intersection
$\checkmark$ Natural join
$\checkmark$ Division
$\checkmark$ Assignment

## Set-Intersection Operation

Notation: $r \cap s$
Defined as:
$r \cap s=\{t \mid t \in r$ and $t \in s\}$
Assume:
$r, s$ have the same arity
attributes of $r$ and $s$ are compatible
Note: $r \cap s=r-(r-s)$

## Set-Intersection Operation - Example



## Natural-Join Operation

## Notation: $\mathrm{r} \bowtie \mathrm{s}$

Let $r$ and $s$ be relations on schemas $R$ and $S$ respectively.
Then, $r \bowtie s$ is a relation on schema $R \cup S$ obtained as follows:
Consider each pair of tuples $t_{r}$ from $r$ and $t_{s}$ from $s$.
If $t_{r}$ and $t_{s}$ have the same value on each of the attributes in $R \cap S$, add a
tuple $t$ to the result, where
$t$ has the same value as $t_{r}$ on $r$
$t$ has the same value as $t_{s}$ on $s$
Example:
$R=(A, B, C, D)$
$S=(E, B, D)$
Result schema $=(A, B, C, D, E)$
$r \quad s$ is defined as:
$\prod_{r . A, r . B, r . C, r . D, s . E}\left(\sigma_{r . B=s . B} \wedge_{r . D=s . D}(r \times s)\right)$

Natural Join Operation - Example

Relations r, s:

| $A$ | $B$ | $C$ | $D$ |  |
| :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | 1 | $\alpha$ | a |  |
| $\beta$ | 2 | $\gamma$ | a |  |
| $\gamma$ | 4 | $\beta$ | b |  |
| $\alpha$ | 1 | $\gamma$ | a |  |
| $\delta$ | 2 | $\beta$ | b |  |
| $r$ |  |  |  |  |


| $\boldsymbol{B}$ | $\boldsymbol{D}$ | $\boldsymbol{E}$ |
| :---: | :---: | :---: |
| $\mathbf{1}$ | a | $\alpha$ |
| 3 | a | $\beta$ |
| 1 | a | $\gamma$ |
| 2 | b | $\delta$ |
| 3 | b | $\in$ |

- $r \bowtie s$

| A | B | C | D | $E$ |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{\alpha}$ | 1 | $\alpha$ | a | $\alpha$ |
| $\alpha$ | 1 | $\alpha$ | a | $\gamma$ |
| $\alpha$ | 1 | $\gamma$ | a | $\alpha$ |
| $\alpha$ | 1 | $\gamma$ | a | $\gamma$ |
| $\boldsymbol{\delta}$ | 2 | $\beta$ | b | $\delta$ |

S

## Join Operations

Join Operations:
A Join operation combines related tuples from different relations, if and only if a given join condition is satisfied. It is denoted by $\bowtie$.

## Example: EMPLOYEE

| EMP_CODE | EMP_NAME |
| :---: | :---: |
| 101 | Stephan |
| 102 | Jack |
| 103 | Harry |

## Join Operations

## Example: SALARY

| EMP_CODE | SALARY |
| :---: | :---: |
| 101 | 50000 |
| 102 | 30000 |
| 103 | 25000 |

Example: SALARY
Operation: (EMPLOYEE $\bowtie$ SALARY)

| EMP_CODE | EMP_NAME | SALARY |
| :---: | :---: | :---: |
| 101 | Stephan | 50000 |
| 102 | Jack | 30000 |
| 103 | Harry | 25000 |

## Types of Join operations



## 1. Natural Join

A natural join is the set of tuples of all combinations in $R$ and $S$ that are equal on their common attribute names.
It is denoted by $\bowtie$.
Example: Let's use the above EMPLOYEE table and SALARY table:
Input:
ПEMP_NAME, SALARY (EMPLOYEE $\bowtie$ SALARY)

## Output:

| EMP_NAME | SALARY |
| :---: | :---: |
| Stephan | 50000 |
| Jack | 30000 |
| Harry | 25000 |

## 2. Outer Join

The outer join operation is an extension of the join operation. It is used to deal with missing information.
Example: EMPLOYEE

| EMP_NAME | STREET | CITY |
| :---: | :---: | :---: |
| Ram | Civil line | Mumbai |
| Shyam | Park street | Kolkata |
| Ravi | M.G.Street | Delhi |
| Hari | Nehru nagar | Hyderabad |

## 2. Outer Join

FACT_WORKERS

| EMP_NAME | BRANCH | SALARY |
| :---: | :---: | :---: |
| Ram | Infosys | 10000 |
| Shyam | Wipro | 20000 |
| Kuber | HCL | 30000 |
| Hari | TCS | 50000 |

Input:
(EMPLOYEE $\bowtie$ FACT_WORKERS)

## 2. Outer Join

## Output:

| EMP_NAME | STREET | CITY | BRANCH | SALARY |
| :---: | :---: | :---: | :---: | :---: |
| Ram | Civil line | Mumbai | Infosys | 10000 |
| Shyam | Park street | Kolkata | Wipro | 20000 |
| Hari | Nehru nagar | Hyderabad | TCS | 50000 |

## Outer Join

An outer join is basically of three types:
-Left outer join

- Right outer join
-Full outer join


## Outer Join

a. Left outer join:

Left outer join contains the set of tuples of all combinations in $R$ and $S$ that are equal on their common attribute names.
In the left outer join, tuples in $R$ have no matching tuples in $S$.
It is denoted by $\searrow$.
Example: Using the above EMPLOYEE table and FACT_WORKERS table Input: EMPLOYEE $\bowtie$ FACT_WORKERS

| EMP_NAME | STREET | CITY | BRANCH | SALARY |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ram | Civil line | Mumbai | Infosys | 10000 |
| Shyam | Park street | Kolkata | Wipro | 20000 |
| Hari | Nehru street | Hyderabad | TCS | 50000 |
| Ravi | M.G. Street | Delhi | NULL | NULL |

## Outer Join

b. Right outer join:

Right outer join contains the set of tuples of all combinations in $R$ and $S$ that are equal on their common attribute names.
In right outer join, tuples in $S$ have no matching tuples in R.
It is denoted by $\bowtie$.
Example: Using the above EMPLOYEE table and FACT_WORKERS
Relation
Input: EMPLOYEE ® FACT_WORKERS

| EMP_NAME | BRANCH | SALARY | STREET | CITY |
| :---: | :---: | :---: | :---: | :---: |
| Ram | Infosys | 10000 | Civil line | Mumbai |
| Shyam | Wipro | 20000 | Park street | Kolkata |
| Hari | TCS | 50000 | Nehru street | Hyderabad |
| Kuber | HCL | 30000 | NULL | NULL |

## Outer Join

c. Full outer join:

Full outer join is like a left or right join except that it contains all rows from both tables.
In full outer join, tuples in $R$ that have no matching tuples in $S$ and tuples in $S$ that have no matching tuples in $R$ in their common attribute name. It is denoted by $\downarrow$.
Example: Using the above EMPLOYEE table and FACT_WORKERS table Input: EMPLOYEE D FACT_WORKERS

| EMP_NAME | STREET | CITY | BRANCH | SALARY |
| :---: | :---: | :---: | :---: | :---: |
| Ram | Civil line | Mumbai | Infosys | 10000 |
| Shyam | Park street | Kolkata | Wipro | 20000 |
| Hari | Nehru street | Hyderabad | TCS | 50000 |
| Ravi | M.G. Street | Delhi | NULL | NULL |
| Kuber | NULL | NULL | HCL | 30000 |

## 3. Equi join

3. Equi join:

It is also known as an inner join. It is the most common join. It is based on matched data as per the equality condition. The equi join uses the comparison operator(=).
Example: CUSTOMER RELATION

| CLASS_ID | NAME |
| :---: | :---: |
| 1 | John |
| 2 | Harry |
| 3 | Jackson |

PRODUCT

| PRODUCT_ID | CITY |
| :---: | :---: |
| 1 | Delhi |
| 2 | Mumbai |
| 3 | Noida |

## 3. Equi join

Input: CUSTOMER $\bowtie$ PRODUCT
Output:

| CLASS_ID | NAME | PRODUCT_ID | CITY |
| :---: | :---: | :---: | :---: |
| 1 | John | 1 | Delhi |
| 2 | Harry | 2 | Mumbai |
| 3 | Harry | 3 | Noida |

## Division Operation

Notation:
Suited to queries that include the phrase "for all".
Let $r$ and $s$ be relations on schemas $R$ and $S$ respectively where

$$
\begin{aligned}
& R=\left(A_{1}, \ldots, A_{m}, B_{1}, \ldots, B_{n}\right) \\
& S=\left(B_{1}, \ldots, B_{n}\right)
\end{aligned}
$$

The result of $r \div s$ is a relation on schema

$$
\begin{aligned}
& R-S=\left(A_{1}, \ldots, A_{m}\right) \\
& r \div s=\left\{t \mid t \in \prod_{R-S}(r) \wedge \forall u \in s(t u \in r)\right\}
\end{aligned}
$$

Where $t u$ means the concatenation of tuples $t$ and $u$ to produce a single tuple

## Division Operation - Example

-Relations r, s:

- $r \div s:$


| $A$ | $B$ |
| :---: | :---: |
| $\alpha$ | 1 |
| $\alpha$ | 2 |
| $\alpha$ | 3 |
| $\beta$ | 1 |
| $\gamma$ | 1 |
| $\delta$ | 1 |
| $\delta$ | 3 |
| $\delta$ | 4 |
| $\epsilon$ | 6 |
| $\epsilon$ | 1 |
| $\beta$ | 2 |
| $r$ |  |


| $B$ |
| :---: |
| 1 |
| 2 |
| $S$ |

## Another Division Example

-Relations r, s:

| $A$ | $B$ | $C$ | $D$ | $E$ |
| :--- | :--- | :--- | :--- | :--- |
| $\alpha$ | a | $\alpha$ | a | 1 |
| $\alpha$ | a | $\gamma$ | a | 1 |
| $\alpha$ | a | $\gamma$ | b | 1 |
| $\beta$ | a | $\gamma$ | a | 1 |
| $\beta$ | a | $\gamma$ | b | 3 |
| $\gamma$ | a | $\gamma$ | a | 1 |
| $\gamma$ | a | $\gamma$ | b | 1 |
| $\gamma$ | a | $\beta$ | b | 1 |
| \begin{tabular}{\|l}
\hline
\end{tabular}$\quad$a 1 <br> b $\quad$\begin{tabular}{\|c}
\hline
\end{tabular} |  |  |  |  |

- $r \div s:$


## Division Operation (Cont.)

Property
Let $q=r \div s$
Then $q$ is the largest relation satisfying $q \times s \subseteq r$
Definition in terms of the basic algebra operation
Let $r(R)$ and $s(S)$ be relations, and let $S \subseteq R$

$$
r \div s=\Pi_{R-S}(r)-\Pi_{R-S}\left(\left(\Pi_{R-S}(r) \times s\right)-\Pi_{R-S, S}(r)\right)
$$

To see why
$\Pi_{R-S, S}(r)$ simply reorders attributes of $r$
$\left.\Pi_{R-S}\left(\Pi_{R-S}(r) \times s\right)-\Pi_{R-S, S}(r)\right)$ gives those tuples $t$ in
$\Pi_{R-S}(r)$ such that for some tuple $u \in s, t u \notin r$.

## Assignment Operation

The assignment operation $(\leftarrow)$ provides a convenient way to express complex queries.
Write query as a sequential program consisting of
a series of assignments
followed by an expression whose value is displayed as a result of the query.
Assignment must always be made to a temporary relation variable.
Example: Write $r \div s$ as

$$
\begin{aligned}
& \quad \text { temp } 1 \leftarrow \prod_{R-S}(r) \\
& \text { temp } 2 \leftarrow \prod_{R-S}\left((\text { temp } 1 \times s)-\prod_{R-S, S}(r)\right) \\
& \text { result }=\text { temp } 1-\text { temp } 2
\end{aligned}
$$

The result to the right of the $\leftarrow$ is assigned to the relation variable on the left of the $\leftarrow$.

May use variable in subsequent expressions.

## Bank Example Queries

- Find the names of all customers who have a loan and an account at bank.

```
\Pi}\mp@subsup{\mathrm{ customer_name }}{}{\mathrm{ (borrower) }}\cap\mp@subsup{\prod}{\mathrm{ customer_name }}{}\mathrm{ (depositor)
```

- Find the name of all customers who have a loan at the bank and the loan amount
$\prod_{\text {customer_name, loan_number, amount }}$ (borrower $\bowtie$ loan)


## Bank Example Queries

- Find all customers who have an account from at least the "Downtown" and the Uptown" branches.

```
-Query 1
    \(\Pi_{\text {customer_name }}\left(\sigma_{\text {branch_name }}=\right.\) "Downtown" \((\) depositor \(\left.\bowtie a c c o u n t)\right) \cap\)
        \(\Pi_{\text {customer_name }}\left(\sigma_{\text {branch_name }}=\right.\) "Uptown" \((\) depositor \(\left.\bowtie a c c o u n t)\right)\)
        - Query 2
        \(\Pi_{\text {customer_name, branch_name }}(\) depositor \(\bowtie\) account)
    \(\div \rho_{\text {temp(branch_name) }}(\{(\) "Downtown") ) ("Uptown") \(\}\) )
    Note that Query 2 uses a constant relation
```


## Bank Example Queries

- Find all customers who have an account at all branches located in Brooklyn city.

$$
\begin{aligned}
& \left.\prod_{\text {customer_name, branch_name }} \text { (depositor } \bowtie \text { account }\right) \\
& \div \prod_{\text {branch_name }}\left(\sigma_{\text {branch_city }} \text { "Brooklyn" }(\text { branch })\right)
\end{aligned}
$$

## Extended Relational-Algebra-Operations

- Generalized Projection
- Aggregate Functions
- Outer Join


## Generalized Projection

Extends the projection operation by allowing arithmetic functions to be used in the projection list
$E$ is any relational-algebra expression
Each of $F_{1}, F_{2}, \ldots, F_{n}$ are are arithmetic expressions involving constants and attributes in the schema of $E$.
Given relation credit_info(customer_name, limit, credit_balance), find how much more each person can spend:

$$
\prod_{\text {customer_name, limit - credit_balance }} \text { (credit_info) }
$$

## Aggregate Functions and Operations

Aggregation function takes a collection of values and returns a single value as a result.
avg: average value
min: minimum value
max: maximum value
sum: sum of values
count: number of values
Aggregate operation in relational algebra

$$
G_{1, G_{2}, K, G_{n}} \vartheta_{h_{1}\left(A_{1}\right), F_{2}\left(A_{2}, K, F_{n}\left(A_{n}\right)\right.}(E)
$$

$E$ is any relational-algebra expression
$G_{1}, G_{2} \ldots, G_{n}$ is a list of attributes on which to group (can be empty)
Each $F_{i}$ is an aggregate function
Each $A_{i}$ is an attribute name

## Aggregate Operation - Example

Relation $r$ :

| $A$ | $B$ | $C$ |
| :---: | :---: | :---: |
| $\alpha$ | $\alpha$ | 7 |
| $\alpha$ | $\beta$ | 7 |
| $\beta$ | $\beta$ | 3 |
| $\beta$ | $\beta$ | 10 |

- $g_{\text {sum(c) }}(\mathrm{r})$

$$
\begin{gathered}
\operatorname{sum}(c) \\
\hline 27
\end{gathered}
$$

## Aggregate Operation - Example

Relation account grouped by branch-name:


## Aggregate Functions (Cont.)

-Result of aggregation does not have a name
-Can use rename operation to give it a name
-For convenience, we permit renaming as part of aggregate operation
branch_name $\boldsymbol{g}_{\text {sum(balance) as sum_balance }}$ (account)

## Outer Join

An extension of the join operation that avoids loss of information.
Computes the join and then adds tuples form one relation that does not match tuples in the other relation to the result of the join. Uses null values:
null signifies that the value is unknown or does not exist
All comparisons involving null are (roughly speaking) false by definition.

We shall study precise meaning of comparisons with nulls later

## Outer Join

-Relation loan
loan_numberbranch_name amount

| L-170 | Downtown | 3000 |
| :--- | :--- | :--- |
| L-230 | Redwood | 4000 |
| L-260 | Perryridge | 1700 |

- Relation borrower

| customer_name | loan_number |
| :--- | :--- |
| Jones | $\mathrm{L}-170$ |
| Smith | $\mathrm{L}-230$ |
| Hayes | $\mathrm{L}-155$ |

## Outer Join - Example

Join

| Ioan $\bowtie$ borrower | loan_number | branch_name | amount | customer_name |
| ---: | :--- | :--- | :--- | :--- |
|  | L-170 Downtown 3000 Jones <br> L-230 Redwood 4000 Smith |  |  |  |

- Left Outer Join
loan $\bowtie$ borrower

| loan_number | branch_name | amount | customer_name |
| :--- | :--- | :---: | :--- |
| L-170 | Downtown | 3000 | Jones |
| L-230 | Redwood | 4000 | Smith |
| L-260 | Perryridge | 1700 | null |

## Outer Join - Example

- Right Outer Join

|  | - Ioan_number | branch_name | amount | customer_name |
| :--- | :--- | :--- | :--- | :---: | :--- |
|  | L-170 | Downtown | 3000 | Jones |
|  | L- 230 | Redwood | 4000 | Smith |
|  | L-155 | null | null | Hayes |

- Full Outer Join

| Ioan -W_ $_{-}$borrower | loan_number | branch_name | amount | customer_name |
| :---: | :--- | :--- | :---: | :--- |
|  | L-170 | Downtown | 3000 | Jones |
|  | L-230 | Redwood | 4000 | Smith |
|  | L-260 | Perryridge | 1700 | null |
|  | L-155 | null | null | Hayes |

## Null Values

-It is possible for tuples to have a null value, denoted by null, for some of their attributes
-null signifies an unknown value or that a value does not exist.
-The result of any arithmetic expression involving null is null.

- Aggregate functions simply ignore null values (as in SQL)
-For duplicate elimination and grouping, null is treated like any other value, and two nulls are assumed to be the same (as in SQL)


## Null Values

Comparisons with null values return the special truth value: unknown
If false was used instead of unknown, then not ( $A<5$ ) would not be equivalent to $\quad A>=5$
Three-valued logic using the truth value unknown:
OR: (unknown or true) = true,
(unknown or false) = unknown
(unknown or unknown) = unknown
AND: (true and unknown) = unknown, (false and unknown) = false, (unknown and unknown) = unknown
NOT: (not unknown) = unknown
In SQL " $P$ is unknown" evaluates to true if predicate $P$ evaluates to unknown Result of select predicate is treated as false if it evaluates to unknown

## Modification of the Database

The content of the database may be modified using the following operations:

Deletion
Insertion
Updating
All these operations are expressed using the assignment operator.

## Deletion

A delete request is expressed similarly to a query, except instead of displaying tuples to the user, the selected tuples are removed from the database.
Can delete only whole tuples; cannot delete values on only particular attributes
A deletion is expressed in relational algebra by:

$$
r \leftarrow r-E
$$

where $r$ is a relation and $E$ is a relational algebra query.

- Delete all account records in the Perryridge branch.

$$
\text { account } \leftarrow \text { account }-\sigma_{\text {branch_name }=\text { "Perryridge" }}(\text { account })
$$

- Delete all loan records with amount in the range of 0 to 50
- Delete all accounts at branches located in Needham.

$$
\begin{aligned}
& r_{1} \leftarrow \sigma_{\text {branch_city }=\text { "Needham" }}(\text { account } \bowtie \text { branch }) \\
& r_{2} \leftarrow \prod_{\text {account_number, branch_name, balance }}\left(r_{1}\right) \\
& r_{3} \leftarrow \prod_{\text {customer_name, account_number }}\left(r_{2} \bowtie \text { depositor }\right) \\
& \text { account } \leftarrow \text { account }-r_{2} \\
& \text { depositor } \leftarrow \text { depositor }-r_{3}
\end{aligned}
$$

## Insertion

- Insert information in the database specifying that Smith has $\$ 1200$ in account A-973 at the Perryridge branch.

$$
\begin{aligned}
& \text { account } \leftarrow \text { account } \cup\{(\text { "A-973", "Perryridge", 1200) }\} \\
& \text { depositor } \leftarrow \text { depositor } \cup\left\{\left({ }^{\prime} \text { Smith", "A-973") }\right\}\right.
\end{aligned}
$$

- Provide as a gift for all loan customers in the Perryridge branch, a $\$ 200$ savings account. Let the loan number serve as the account number for the new savings account.

$$
\begin{aligned}
& r_{1} \leftarrow\left(\sigma_{\text {branch_name }}=\right.\text { "Perryridge" } \\
& \text { account } \leftarrow \text { account } \cup \prod_{\text {loan_number, branch_name, } 200}\left(r_{1}\right) \\
& \text { depositor } \leftarrow \text { depositor } \cup \prod_{\text {customer_name, loan_number }}\left(r_{1}\right)
\end{aligned}
$$

## Updating

A mechanism to change a value in a tuple without charging all values in the tuple
Use the generalized projection operator to do this task
Each $F_{i}$ is either
the $I^{\text {th }}$ attribute of $r$, if the $I^{\text {th }}$ attribute is not updated, or, if the attribute is to be updated $F_{i}$ is an expression, involving only constants and the attributes of $r$, which gives the new value for the attribute

## Update Examples

- Make interest payments by increasing all balances by 5 percent.

```
account }\leftarrow\mp@subsup{\Pi}{\mathrm{ account_number, branch_name, balance * 1.05 (account)}}{\mathrm{ ( }
```

- Pay all accounts with balances over $\$ 10,0006$ percent interest and pay all others 5 percent

```
account \(\leftarrow \prod_{\text {account_number, branch_name, balance }{ }^{1.06}\left(\sigma_{\text {BAL }}>10000(\text { account })\right)}\)
    \(\cup \prod_{\text {account_number, branch_name, balance }{ }^{*} 1.05}\left(\sigma_{\text {BAL }} \leq 10000(\right.\) account \(\left.)\right)\)
```

Figure 2.3. The branch relation

| branch_name | branch_city | assets |
| :--- | :--- | ---: |
| Brighton | Brooklyn | 7100000 |
| Downtown | Brooklyn | 9000000 |
| Mianus | Horseneck | 400000 |
| North Town | Rye | 3700000 |
| Perryridge | Horseneck | 1700000 |
| Pownal | Bennington | 300000 |
| Redwood | Palo Alto | 2100000 |
| Round Hill | Horseneck | 8000000 |

## Figure 2.6: The Ioan relation

| loan_number | branch_name | amount |
| :---: | :--- | ---: |
| L-11 | Round Hill | 900 |
| L-14 | Downtown | 1500 |
| L-15 | Perryridge | 1500 |
| L-16 | Perryridge | 1300 |
| L-17 | Downtown | 1000 |
| L-23 | Redwood | 2000 |
| L-93 | Mianus | 500 |

Figure 2.7: The borrower relation

| customer_name | loan_number |
| :--- | :---: |
| Adams | $\mathrm{L}-16$ |
| Curry | $\mathrm{L}-93$ |
| Hayes | $\mathrm{L}-15$ |
| Jackson | $\mathrm{L}-14$ |
| Jones | $\mathrm{L}-17$ |
| Smith | $\mathrm{L}-11$ |
| Smith | $\mathrm{L}-23$ |
| Williams | $\mathrm{L}-17$ |

Figure 2.9 Result of $\sigma_{\text {branch_name }=\text { "Perryridge" }}($ loan $)$

| loan_number | branch_name | amount |
| :---: | :---: | :---: |
| L-15 | Perryridge | 1500 |
| L-16 | Perryridge | 1300 |

Figure 2.10: Loan number and the amount of the loan

| loan_number | amount |
| :---: | :---: |
| $\mathrm{L}-11$ | 900 |
| $\mathrm{~L}-14$ | 1500 |
| $\mathrm{~L}-15$ | 1500 |
| $\mathrm{~L}-16$ | 1300 |
| $\mathrm{~L}-17$ | 1000 |
| $\mathrm{~L}-23$ | 2000 |
| $\mathrm{~L}-93$ | 500 |

Figure 2.11: Names of all customers who have either an account or an Ioan

| customer_name |
| :---: |
| Adams |
| Curry |
| Hayes |
| Jackson |
| Jones |
| Smith |
| Williams |
| Lindsay |
| Johnson |
| Turner |

Figure 2.12: Customers with an account but no loan

## customer_name

## Johnson Lindsay Turner

Figure 2.13: Result of borrower $|X|$ loan

| customer_name | borrower. loan_number | $\begin{gathered} \text { loan. } \\ \text { loan_number } \end{gathered}$ | branch_name | amount |
| :---: | :---: | :---: | :---: | :---: |
| Adams | L-16 | L-11 | Round Hill | 900 |
| Adams | L-16 | L-14 | Downtown | 1500 |
| Adams | L-16 | L-15 | Perryridge | 1500 |
| Adams | L-16 | L-16 | Perryridge | 1300 |
| Adams | L-16 | L-17 | Downtown | 1000 |
| Adams | L-16 | L-23 | Redwood | 2000 |
| Adams | L-16 | L-93 | Mianus | 500 |
| Curry | L-93 | L-11 | Round Hill | 900 |
| Curry | L-93 | L-14 | Downtown | 1500 |
| Curry | L-93 | L-15 | Perryridge | 1500 |
| Curry | L-93 | L-16 | Perryridge | 1300 |
| Curry | L-93 | L-17 | Downtown | 1000 |
| Curry | L-93 | L-23 | Redwood | 2000 |
| Curry | L-93 | L-93 | Mianus | 500 |
| Hayes | L-15 | L-11 |  | 900 |
| Hayes | L-15 | L-14 |  | 1500 |
| Hayes | L-15 | L-15 |  | 1500 |
| Hayes | L-15 | L-16 |  | 1300 |
| Hayes | L-15 | L-17 |  | 1000 |
| Hayes | L-15 | L-23 |  | 2000 |
| Hayes | L-15 | L-93 |  | 500 |
| ... | $\ldots$ | $\cdots$ | $\cdots$ | $\ldots$ |
| $\cdots$ | $\cdots$ | $\cdots$ | $\ldots$ | $\ldots$ |
| $\cdots$ | ... | .. | $\cdots$ | $\cdots$ |
| Smith | L-23 | L-11 | Round Hill | 900 |
| Smith | L-23 | L-14 | Downtown | 1500 |
| Smith | L-23 | L-15 | Perryridge | 1500 |
| Smith | L-23 | L-16 | Perryridge | 1300 |
| Smith | L-23 | L-17 | Downtown | 1000 |
| Smith | L-23 | L-23 | Redwood | 2000 |
| Smith | L-23 | L-93 | Mianus | 500 |
| Williams | L-17 | L-11 | Round Hill | 900 |
| Williams | L-17 | L-14 | Downtown | 1500 |
| Williams | L-17 | L-15 | Perryridge | 1500 |
| Williams | L-17 | L-16 | Perryridge | 1300 |
| Williams | L-17 | L-17 | Downtown | 1000 |
| Williams | L-17 | L-23 | Redwood | 2000 |
| Williams | L-17 | L-93 | Mianus | 500 |

Figure 2.14

| customer_name | borrower. <br> loan_number | loan. <br> loan_number | branch_name | amount |
| :--- | :---: | :---: | :---: | :---: |
| Adams | L-16 | L-15 | Perryridge | 1500 |
| Adams | L-16 | L-16 | Perryridge | 1300 |
| Curry | L-93 | L-15 | Perryridge | 1500 |
| Curry | L-93 | L-16 | Perryridge | 1300 |
| Hayes | L-15 | L-15 | Perryridge | 1500 |
| Hayes | L-15 | L-16 | Perryridge | 1300 |
| Jackson | L-14 | L-15 | Perryridge | 1500 |
| Jackson | L-14 | L-16 | Perryridge | 1300 |
| Jones | L-17 | L-15 | Perryridge | 1500 |
| Jones | L-17 | L-16 | Perryridge | 1300 |
| Smith | L-11 | L-15 | Perryridge | 1500 |
| Smith | L-11 | L-16 | Perryridge | 1300 |
| Smith | L-23 | L-15 | Perryridge | 1500 |
| Smith | L-23 | L-16 | Perryridge | 1300 |
| Williams | L-17 | L-15 | Perryridge | 1500 |
| Williams | L-17 | L-16 | Perryridge | 1300 |

Figure 2.15

## customer_name

## Adams Hayes

Figure 2.16


Figure 2.17 Largest account balance in the bank


## customer_name

## Curry Smith

## customer_name

## Hayes Jones Smith

Figure 2.20

| Customer_name | loan_number | amount |
| :---: | :---: | ---: |
| Adams | $\mathrm{L}-16$ | 1300 |
| Curry | $\mathrm{L}-93$ | 500 |
| Hayes | $\mathrm{L}-15$ | 1500 |
| Jackson | $\mathrm{L}-14$ | 1500 |
| Jones | $\mathrm{L}-17$ | 1000 |
| Smith | $\mathrm{L}-23$ | 2000 |
| Smith | $\mathrm{L}-11$ | 900 |
| Williams | $\mathrm{L}-17$ | 1000 |

Figure 2.21
branch_name
Brighton Perryridge

Figure 2.22
branch_name
Brighton Downtown

| customer_name | branch_name |
| :---: | :--- |
| Hayes | Perryridge |
| Johnson | Downtown |
| Johnson | Brighton |
| Jones | Brighton |
| Lindsay | Redwood |
| Smith | Mianus |
| Turner | Round Hill |

Figure 2.24: The credit_info relation

| customer_name | limit | credit_balance |
| :---: | :---: | :---: |
| Curry | 2000 | 1750 |
| Hayes | 1500 | 1500 |
| Jones | 6000 | 700 |
| Smith | 2000 | 400 |

Figure 2.25

| customer_name | credit_available |
| :---: | :---: |
| Curry | 250 |
| Jones | 5300 |
| Smith | 1600 |
| Hayes | 0 |

Figure 2.26: The pt_works relation

| employee_name | branch_name | salary |
| :--- | :--- | ---: |
| Adams | Perryridge | 1500 |
| Brown | Perryridge | 1300 |
| Gopal | Perryridge | 5300 |
| Johnson | Downtown | 1500 |
| Loreena | Downtown | 1300 |
| Peterson | Downtown | 2500 |
| Rao | Austin | 1500 |
| Sato | Austin | 1600 |

Figure 2.27 The pt_works relation after regrouping

| employee_name | branch_name | salary |
| :---: | :--- | :---: |
| Rao | Austin | 1500 |
| Sato | Austin | 1600 |
| Johnson | Downtown | 1500 |
| Loreena | Downtown | 1300 |
| Peterson | Downtown | 2500 |
| Adams | Perryridge | 1500 |
| Brown | Perryridge | 1300 |
| Gopal | Perryridge | 5300 |

Figure 2.28

## branch_name sum of salary <br> Austin <br> 3100 <br> Downtown <br> 5300 Perryridge 8100

## Figure 2.29

## branch_name sum_salary $\quad$ max_salary

| Austin | 3100 | 1600 |
| :--- | :--- | :--- |
| Downtown | 5300 | 2500 |
| Perryridge | 8100 | 5300 |

Figure 2.30 The employee and ft_works relations

| employee_name | street | city |
| :---: | :--- | :--- |
| Coyote | Toon | Hollywood |
| Rabbit | Tunnel | Carrotville |
| Smith | Revolver | Death Valley |
| Williams | Seaview | Seattle |
|  |  |  |
| employee_name | branch_name | salary |
| Coyote | Mesa | 1500 |
| Rabbit | Mesa | 1300 |
| Gates | Redmond | 5300 |
| Williams | Redmond | 1500 |

Figure 2.31

| employee_name | street | city | branch_name | salary |
| :---: | :--- | :--- | :--- | :--- |
| Coyote | Toon | Hollywood | Mesa | 1500 |
| Rabbit | Tunnel | Carrotville | Mesa | 1300 |
| Williams | Seaview | Seattle | Redmond | 1500 |

Figure 2.32

| employee_name | street | city | branch_name | salary |
| :--- | :--- | :--- | :---: | :---: |
| Coyote | Toon | Hollywood | Mesa | 1500 |
| Rabbit | Tunnel | Carrotville | Mesa | 1300 |
| Williams | Seaview | Seattle | Redmond | 1500 |
| Smith | Revolver | Death Valley | null | null |

Figure 2.33

| employee_name | street | city | branch_name | salary |
| :---: | :--- | :--- | :--- | :---: |
| Coyote | Toon | Hollywood | Mesa | 1500 |
| Rabbit | Tunnel | Carrotville | Mesa | 1300 |
| Williams | Seaview | Seattle | Redmond | 1500 |
| Gates | null | null | Redmond | 5300 |

Figure 2.34

| employee_name | street | city | branch_name | salary |
| :---: | :--- | :--- | :--- | :--- |
| Coyote | Toon | Hollywood | Mesa | 1500 |
| Rabbit | Tunnel | Carrotville | Mesa | 1300 |
| Williams | Seaview | Seattle | Redmond | 1500 |
| Smith | Revolver | Death Valley | null | null |
| Gates | null | null | Redmond | 5300 |

## Reference

1. https://www.javatpoint.com/dbms-data-model-schema-and-instance
2. https://hirinfotech.com/structured-vs-unstructured-data/


## THANK YOU

