

Unit II

ORTHOGONAL TRANSFORMATION OF SYMMETRIC MATRIX OF A DIAGONAL FORM

The transformation $N^T A N = D$ is known as orthogonal transformation or reduction where N is normalized matrix

D is diagonal matrix whose diagonal elements are eigen values of given matrix

Methods through diagonalized a symmetric matrix by orthogonal transformation

Step 1:

Find the characteristic equation and eigenvalue and eigen vector of a matrix A .

Step 2:

Check orthogonal condition

$$x_1^T x_2 = 0, \quad x_2^T x_3 = 0, \quad x_3^T x_1 = 0$$

Step 3:

The normalized eigen vector of $x = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$

then the normalized vector

$$N = \begin{bmatrix} \frac{x_1}{\lambda(x_1)} \\ \frac{x_2}{\lambda(x_2)} \\ \frac{x_3}{\lambda(x_3)} \end{bmatrix}$$

Step 4: Find modal matrix $N = [N_1 \ N_2 \ N_3]$

Step 5: Find $N^T A N = D$